

$\Theta[K\_]$  :=

Module [ {Cs,  $\varphi$ , n, A, s, i, j, k,  $\Delta$ , G, v,  $\alpha$ ,  
 $\beta$ , gEval, c, z},

{Cs,  $\varphi$ } = Rot [K]; n = Length [Cs];

A = IdentityMatrix [2 n + 1];

Cases [Cs, {s\_, i\_, j\_}  $\Rightarrow$

$\left( A[[\{i, j\}, \{i + 1, j + 1\}]] += \begin{pmatrix} -T^s & T^s & -1 \\ \theta & & -1 \end{pmatrix} \right) ]$ ;

$\Delta = T^{(-\text{Total}[\varphi] - \text{Total}[\text{Cs}[[\text{All}, 1]])] / 2} \text{Det} [A]$ ;

G = Inverse [A];

gEval [ $\mathcal{E}$ \_] :=

Factor [ $\mathcal{E} / . \mathbf{g}_{v, \alpha, \beta} \Rightarrow (G[[\alpha, \beta]] / . T \rightarrow T_v)$ ];

z = gEval [ $\sum_{k1=1}^n \sum_{k2=1}^n \theta[\text{Cs}[[k1]], \text{Cs}[[k2]]]$ ];

z += gEval [ $\sum_{k=1}^n R_1 @@ \text{Cs}[[k]]$ ];

z += gEval [ $\sum_{k=1}^{2^n} R_1[\varphi[[k]], k]$ ];

{ $\Delta$ , ( $\Delta / . T \rightarrow T_1$ ) ( $\Delta / . T \rightarrow T_2$ ) ( $\Delta / . T \rightarrow T_3$ ) z} //

Factor ];