

Pensieve Header: Shrinking the Logos.

$$\begin{aligned} \Delta\theta[k_-] := & -\frac{1}{2} (-1 + t_k) \left(\alpha^2 \beta^2 + 4 \alpha \beta \delta (1 + (-1 + t_k) \delta) + 2 \delta^2 (1 + (-1 + t_k) \delta)^2 \right) + \\ & 2 (1 + (-1 + t_k) \delta)^2 (\alpha \beta + \delta + (-1 + t_k) \delta^2) c_k - \\ & \beta (1 + 2 (-1 + t_k) \delta) (\alpha \beta + 2 \delta (1 + (-1 + t_k) \delta)) u_k + 2 \beta \delta (1 + (-1 + t_k) \delta)^2 c_k u_k - \\ & \frac{1}{2} \beta^2 \delta (2 + 3 (-1 + t_k) \delta) u_k^2 + \alpha (\alpha \beta + 2 \delta (1 + (-1 + t_k) \delta)) w_k + 2 \alpha \delta (1 + (-1 + t_k) \delta)^2 c_k w_k - \\ & 2 (-1 + t_k) \delta^2 (\alpha \beta + \delta (1 + (-1 + t_k) \delta)) u_k w_k + 2 \delta^2 (1 + (-1 + t_k) \delta)^2 c_k u_k w_k - \\ & \beta \delta^2 (1 + 2 (-1 + t_k) \delta) u_k^2 w_k + \frac{1}{2} \alpha^2 \delta (2 + (-1 + t_k) \delta) w_k^2 + \alpha \delta^2 u_k w_k^2 - \frac{1}{2} (-1 + t_k) \delta^4 u_k^2 w_k^2; \end{aligned}$$

$$\begin{aligned} \Delta[k_-] := & (1 - t_k) (\alpha^2 \beta^2 + 4 \alpha \beta \delta v^{-1} + 2 \delta^2 v^{-2}) / 2 + 2 v^{-2} (\alpha \beta + \delta v^{-1}) c_k - \\ & \beta (2 v^{-1} - 1) (\alpha \beta + 2 \delta v^{-1}) u_k + 2 \beta \delta v^{-2} c_k u_k - \beta^2 \delta (3 v^{-1} - 1) u_k^2 / 2 + \\ & \alpha (\alpha \beta + 2 \delta v^{-1}) w_k + 2 \alpha \delta v^{-2} c_k w_k - 2 (t_k - 1) \delta^2 (\alpha \beta + \delta v^{-1}) u_k w_k + 2 \delta^2 v^{-2} c_k u_k w_k - \\ & \beta \delta^2 (2 v^{-1} - 1) u_k^2 w_k + \alpha^2 \delta (1 + v^{-1}) w_k^2 / 2 + \alpha \delta^2 u_k w_k^2 - (t_k - 1) \delta^4 u_k^2 w_k^2 / 2; \end{aligned}$$

$$\text{Simplify}[\Delta\theta[k] = (\Delta[k] /. v \rightarrow (1 + (t_k - 1) \delta)^{-1})]$$

True

$\Delta[k]$

$$\begin{aligned} & \frac{2 (\alpha \beta + \frac{\delta}{v}) c_k}{v^2} + \frac{1}{2} \left(\alpha^2 \beta^2 + \frac{2 \delta^2}{v^2} + \frac{4 \alpha \beta \delta}{v} \right) (1 - t_k) - \beta \left(-1 + \frac{2}{v} \right) \left(\alpha \beta + \frac{2 \delta}{v} \right) u_k + \\ & \frac{2 \beta \delta c_k u_k}{v^2} - \frac{1}{2} \beta^2 \delta \left(-1 + \frac{3}{v} \right) u_k^2 + \alpha \left(\alpha \beta + \frac{2 \delta}{v} \right) w_k + \frac{2 \alpha \delta c_k w_k}{v^2} + \frac{2 \delta^2 c_k u_k w_k}{v^2} - \\ & 2 \delta^2 \left(\alpha \beta + \frac{\delta}{v} \right) (-1 + t_k) u_k w_k - \beta \delta^2 \left(-1 + \frac{2}{v} \right) u_k^2 w_k + \frac{1}{2} \alpha^2 \delta \left(1 + \frac{1}{v} \right) w_k^2 + \alpha \delta^2 u_k w_k^2 - \frac{1}{2} \delta^4 (-1 + t_k) u_k^2 w_k^2 \end{aligned}$$

$\text{Simplify}[\Delta[k]]$

$$\begin{aligned} & \frac{1}{2 v^3} \left(4 c_k (\delta + \alpha \beta v + \alpha \delta v w_k + \delta v u_k (\beta + \delta w_k)) + \right. \\ & v \left(2 \delta^2 + 4 \alpha \beta \delta v + \alpha^2 \beta^2 v^2 + 4 \alpha \delta v w_k + 2 \alpha^2 \beta v^2 w_k + \alpha^2 \delta v w_k^2 + \right. \\ & \left. \left. \alpha^2 \delta v^2 w_k^2 + \delta v u_k^2 (\beta^2 (-3 + v) + 2 \beta \delta (-2 + v) w_k + \delta^3 v w_k^2) + \right. \right. \\ & \left. \left. 2 u_k (\beta (-2 + v) (2 \delta + \alpha \beta v) + 2 \delta^2 v (\delta + \alpha \beta v) w_k + \alpha \delta^2 v^2 w_k^2) - \right. \right. \\ & \left. \left. t_k (2 \delta^2 + 4 \alpha \beta \delta v + \alpha^2 \beta^2 v^2 + 4 \delta^2 v (\delta + \alpha \beta v) u_k w_k + \delta^4 v^2 u_k^2 w_k^2) \right) \right) \end{aligned}$$