

In[*]:= $\$k = 0;$

$R_{1,2} \bar{R}_{3,4} // m_{1,3 \rightarrow 1} // m_{2,4 \rightarrow 2}$

» EZip called with $\{vs, \mathcal{F}, \mathcal{E}\} =$

$$\left\{ \begin{aligned} & \{P_{1,\$[1]}, P_{1,\$[3]}, P_{2,\$[1]}, P_{2,\$[3]}, P_{3,\$[1]}, P_{3,\$[3]}, \pi_{1,\$[1]}, \pi_{1,\$[3]}, \pi_{2,\$[1]}, \pi_{2,\$[3]}, \pi_{3,\$[1]}, \pi_{3,\$[3]}, \\ & X_{1,\$[1]}, X_{1,\$[3]}, X_{2,\$[1]}, X_{2,\$[3]}, X_{3,\$[1]}, X_{3,\$[3]}, \xi_{1,\$[1]}, \xi_{1,\$[3]}, \xi_{2,\$[1]}, \xi_{2,\$[3]}, \xi_{3,\$[1]}, \xi_{3,\$[3]}, \\ & P_{1,\$[1]} \pi_{1,\$[1]} + P_{1,\$[3]} \pi_{1,\$[3]} + P_{2,\$[1]} \pi_{2,\$[1]} + P_{2,\$[3]} \pi_{2,\$[3]} + P_{3,\$[1]} \pi_{3,\$[1]} + P_{3,\$[3]} \pi_{3,\$[3]} + \\ & X_{1,\$[1]} \xi_{1,\$[1]} + X_{1,\$[3]} \xi_{1,\$[3]} + X_{2,\$[1]} \xi_{2,\$[1]} + X_{2,\$[3]} \xi_{2,\$[3]} + X_{3,\$[1]} \xi_{3,\$[1]} + X_{3,\$[3]} \xi_{3,\$[3]}, \\ & \mathbb{E} \left[\mathbf{1}, p_{1,1} (\pi_{1,\$[1]} + \pi_{1,\$[3]}) + p_{2,1} (\pi_{2,\$[1]} + \pi_{2,\$[3]}) + p_{3,1} (\pi_{3,\$[1]} + \pi_{3,\$[3]}) + (-1 + T_1) (-p_{1,2} + p_{1,\$[1]}) X_{1,2} + \right. \\ & \left. \left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,\$[3]}) X_{1,4} - \pi_{1,\$[3]} \xi_{1,\$[1]} + X_{1,1} (\xi_{1,\$[1]} + \xi_{1,\$[3]}) - \pi_{2,\$[3]} \xi_{2,\$[1]} + \right. \\ & \left. X_{2,1} (\xi_{2,\$[1]} + \xi_{2,\$[3]}) - \pi_{3,\$[3]} \xi_{3,\$[1]} + X_{3,1} (\xi_{3,\$[1]} + \xi_{3,\$[3]}) \right], \in \text{Series}[0] \} \end{aligned} \right\}$$

» EZip1 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \begin{aligned} & \{P_{1,\$[1]}, P_{1,\$[3]}, P_{2,\$[1]}, P_{2,\$[3]}, P_{3,\$[1]}, P_{3,\$[3]}, \pi_{1,\$[1]}, \pi_{1,\$[3]}, \pi_{2,\$[1]}, \pi_{2,\$[3]}, \pi_{3,\$[1]}, \pi_{3,\$[3]}, \\ & X_{1,\$[1]}, X_{1,\$[3]}, X_{2,\$[1]}, X_{2,\$[3]}, X_{3,\$[1]}, X_{3,\$[3]}, \xi_{1,\$[1]}, \xi_{1,\$[3]}, \xi_{2,\$[1]}, \xi_{2,\$[3]}, \xi_{3,\$[1]}, \xi_{3,\$[3]}, \\ & P_{1,\$[1]} \pi_{1,\$[1]} + P_{1,\$[3]} \pi_{1,\$[3]} + P_{2,\$[1]} \pi_{2,\$[1]} + P_{2,\$[3]} \pi_{2,\$[3]} + P_{3,\$[1]} \pi_{3,\$[1]} + P_{3,\$[3]} \pi_{3,\$[3]} + \\ & X_{1,\$[1]} \xi_{1,\$[1]} + X_{1,\$[3]} \xi_{1,\$[3]} + X_{2,\$[1]} \xi_{2,\$[1]} + X_{2,\$[3]} \xi_{2,\$[3]} + X_{3,\$[1]} \xi_{3,\$[1]} + X_{3,\$[3]} \xi_{3,\$[3]}, \mathbf{1}, \\ & P_{1,1} (\pi_{1,\$[1]} + \pi_{1,\$[3]}) + P_{2,1} (\pi_{2,\$[1]} + \pi_{2,\$[3]}) + P_{3,1} (\pi_{3,\$[1]} + \pi_{3,\$[3]}) + (-1 + T_1) (-p_{1,2} + p_{1,\$[1]}) X_{1,2} + \\ & \left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,\$[3]}) X_{1,4} - \pi_{1,\$[3]} \xi_{1,\$[1]} + X_{1,1} (\xi_{1,\$[1]} + \xi_{1,\$[3]}) - \pi_{2,\$[3]} \xi_{2,\$[1]} + \\ & X_{2,1} (\xi_{2,\$[1]} + \xi_{2,\$[3]}) - \pi_{3,\$[3]} \xi_{3,\$[1]} + X_{3,1} (\xi_{3,\$[1]} + \xi_{3,\$[3]}) \right], \in \text{Series}[0] \} \end{aligned} \right\}$$

» EZip2 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \begin{aligned} & \{P_{1,\$[1]}, P_{1,\$[3]}, P_{2,\$[1]}, P_{2,\$[3]}, P_{3,\$[1]}, P_{3,\$[3]}, \pi_{1,\$[1]}, \pi_{1,\$[3]}, \pi_{2,\$[1]}, \pi_{2,\$[3]}, \pi_{3,\$[1]}, \pi_{3,\$[3]}, \\ & X_{1,\$[1]}, X_{1,\$[3]}, X_{2,\$[1]}, X_{2,\$[3]}, X_{3,\$[1]}, X_{3,\$[3]}, \xi_{1,\$[1]}, \xi_{1,\$[3]}, \xi_{2,\$[1]}, \xi_{2,\$[3]}, \xi_{3,\$[1]}, \xi_{3,\$[3]}, \\ & P_{1,\$[1]} \pi_{1,\$[1]} + P_{1,\$[3]} \pi_{1,\$[3]} + P_{2,\$[1]} \pi_{2,\$[1]} + P_{2,\$[3]} \pi_{2,\$[3]} + P_{3,\$[1]} \pi_{3,\$[1]} + \\ & P_{3,\$[3]} \pi_{3,\$[3]} - \pi_{1,\$[3]} \xi_{1,\$[1]} + X_{1,\$[1]} \xi_{1,\$[1]} + X_{1,\$[3]} \xi_{1,\$[3]} - \pi_{2,\$[3]} \xi_{2,\$[1]} + \\ & X_{2,\$[1]} \xi_{2,\$[1]} + X_{2,\$[3]} \xi_{2,\$[3]} - \pi_{3,\$[3]} \xi_{3,\$[1]} + X_{3,\$[1]} \xi_{3,\$[1]} + X_{3,\$[3]} \xi_{3,\$[3]}, \mathbf{1}, \\ & P_{1,1} \pi_{1,\$[1]} + P_{1,1} \pi_{1,\$[3]} + P_{2,1} \pi_{2,\$[1]} + P_{2,1} \pi_{2,\$[3]} + P_{3,1} \pi_{3,\$[1]} + P_{3,1} \pi_{3,\$[3]} + (1 - T_1) p_{1,2} X_{1,2} + \\ & (-1 + T_1) p_{1,\$[1]} X_{1,2} + \frac{(-1 + T_1) p_{1,4} X_{1,4}}{T_1} + \frac{(1 - T_1) p_{1,\$[3]} X_{1,4}}{T_1} + X_{1,1} \xi_{1,\$[1]} + \\ & X_{1,1} \xi_{1,\$[3]} + X_{2,1} \xi_{2,\$[1]} + X_{2,1} \xi_{2,\$[3]} + X_{3,1} \xi_{3,\$[1]} + X_{3,1} \xi_{3,\$[3]}, \in \text{Series}[0] \} \end{aligned} \right\}$$

» EZip3 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \begin{aligned} & \{P_{1,\$[1]}, P_{1,\$[3]}, P_{2,\$[1]}, P_{2,\$[3]}, P_{3,\$[1]}, P_{3,\$[3]}, \pi_{1,\$[1]}, \pi_{1,\$[3]}, \pi_{2,\$[1]}, \pi_{2,\$[3]}, \pi_{3,\$[1]}, \pi_{3,\$[3]}, \\ & X_{1,\$[1]}, X_{1,\$[3]}, X_{2,\$[1]}, X_{2,\$[3]}, X_{3,\$[1]}, X_{3,\$[3]}, \xi_{1,\$[1]}, \xi_{1,\$[3]}, \xi_{2,\$[1]}, \xi_{2,\$[3]}, \xi_{3,\$[1]}, \xi_{3,\$[3]}, \\ & P_{1,\$[1]} \pi_{1,\$[1]} + P_{1,\$[3]} \pi_{1,\$[3]} + P_{2,\$[1]} \pi_{2,\$[1]} + P_{2,\$[3]} \pi_{2,\$[3]} + P_{3,\$[1]} \pi_{3,\$[1]} + \\ & P_{3,\$[3]} \pi_{3,\$[3]} - \pi_{1,\$[3]} \xi_{1,\$[1]} + X_{1,\$[1]} \xi_{1,\$[1]} + X_{1,\$[3]} \xi_{1,\$[3]} - \pi_{2,\$[3]} \xi_{2,\$[1]} + \\ & X_{2,\$[1]} \xi_{2,\$[1]} + X_{2,\$[3]} \xi_{2,\$[3]} - \pi_{3,\$[3]} \xi_{3,\$[1]} + X_{3,\$[1]} \xi_{3,\$[1]} + X_{3,\$[3]} \xi_{3,\$[3]}, \mathbf{1}, \\ & (-1 + T_1) p_{1,1} X_{1,2} + (1 - T_1) p_{1,2} X_{1,2} + \frac{(1 - T_1) p_{1,1} X_{1,4}}{T_1} + \frac{(-1 + T_1) p_{1,4} X_{1,4}}{T_1}, \in \text{Series}[0] \} \end{aligned} \right\}$$

» EZip called with $\{vs, \mathcal{F}, \mathcal{E}\} =$

$$\left\{ \{ p_{1, \$[2]}, p_{1, \$[4]}, p_{2, \$[2]}, p_{2, \$[4]}, p_{3, \$[2]}, p_{3, \$[4]}, \pi_{1, \$[2]}, \pi_{1, \$[4]}, \pi_{2, \$[2]}, \pi_{2, \$[4]}, \pi_{3, \$[2]}, \pi_{3, \$[4]}, \right. \\ x_{1, \$[2]}, x_{1, \$[4]}, x_{2, \$[2]}, x_{2, \$[4]}, x_{3, \$[2]}, x_{3, \$[4]}, \xi_{1, \$[2]}, \xi_{1, \$[4]}, \xi_{2, \$[2]}, \xi_{2, \$[4]}, \xi_{3, \$[2]}, \xi_{3, \$[4]} \}, \\ p_{1, \$[2]} \pi_{1, \$[2]} + p_{1, \$[4]} \pi_{1, \$[4]} + p_{2, \$[2]} \pi_{2, \$[2]} + p_{2, \$[4]} \pi_{2, \$[4]} + p_{3, \$[2]} \pi_{3, \$[2]} + p_{3, \$[4]} \pi_{3, \$[4]} + \\ x_{1, \$[2]} \xi_{1, \$[2]} + x_{1, \$[4]} \xi_{1, \$[4]} + x_{2, \$[2]} \xi_{2, \$[2]} + x_{2, \$[4]} \xi_{2, \$[4]} + x_{3, \$[2]} \xi_{3, \$[2]} + x_{3, \$[4]} \xi_{3, \$[4]}, \\ \mathbb{E} \left[\mathbf{1}, p_{1,2} (\pi_{1, \$[2]} + \pi_{1, \$[4]}) + p_{2,2} (\pi_{2, \$[2]} + \pi_{2, \$[4]}) + p_{3,2} (\pi_{3, \$[2]} + \pi_{3, \$[4]}) + (-\mathbf{1} + T_1) p_{1,1} x_{1, \$[2]} + (1 - T_1) \right. \\ p_{1, \$[2]} x_{1, \$[2]} + \frac{(1 - T_1) p_{1,1} x_{1, \$[4]}}{T_1} + \frac{(-1 + T_1) p_{1, \$[4]} x_{1, \$[4]}}{T_1} - \pi_{1, \$[4]} \xi_{1, \$[2]} + x_{1,2} (\xi_{1, \$[2]} + \xi_{1, \$[4]}) - \\ \left. \pi_{2, \$[4]} \xi_{2, \$[2]} + x_{2,2} (\xi_{2, \$[2]} + \xi_{2, \$[4]}) - \pi_{3, \$[4]} \xi_{3, \$[2]} + x_{3,2} (\xi_{3, \$[2]} + \xi_{3, \$[4]}) \right], \in \text{Series}[0] \left. \right\}$$

» EZip1 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \{ p_{1, \$[2]}, p_{1, \$[4]}, p_{2, \$[2]}, p_{2, \$[4]}, p_{3, \$[2]}, p_{3, \$[4]}, \pi_{1, \$[2]}, \pi_{1, \$[4]}, \pi_{2, \$[2]}, \pi_{2, \$[4]}, \pi_{3, \$[2]}, \pi_{3, \$[4]}, \right. \\ x_{1, \$[2]}, x_{1, \$[4]}, x_{2, \$[2]}, x_{2, \$[4]}, x_{3, \$[2]}, x_{3, \$[4]}, \xi_{1, \$[2]}, \xi_{1, \$[4]}, \xi_{2, \$[2]}, \xi_{2, \$[4]}, \xi_{3, \$[2]}, \xi_{3, \$[4]} \}, \\ p_{1, \$[2]} \pi_{1, \$[2]} + p_{1, \$[4]} \pi_{1, \$[4]} + p_{2, \$[2]} \pi_{2, \$[2]} + p_{2, \$[4]} \pi_{2, \$[4]} + p_{3, \$[2]} \pi_{3, \$[2]} + p_{3, \$[4]} \pi_{3, \$[4]} + \\ x_{1, \$[2]} \xi_{1, \$[2]} + x_{1, \$[4]} \xi_{1, \$[4]} + x_{2, \$[2]} \xi_{2, \$[2]} + x_{2, \$[4]} \xi_{2, \$[4]} + x_{3, \$[2]} \xi_{3, \$[2]} + x_{3, \$[4]} \xi_{3, \$[4]}, \\ \mathbf{1}, p_{1,2} (\pi_{1, \$[2]} + \pi_{1, \$[4]}) + p_{2,2} (\pi_{2, \$[2]} + \pi_{2, \$[4]}) + p_{3,2} (\pi_{3, \$[2]} + \pi_{3, \$[4]}) + \\ (-1 + T_1) p_{1,1} x_{1, \$[2]} + (1 - T_1) p_{1, \$[2]} x_{1, \$[2]} + \frac{(1 - T_1) p_{1,1} x_{1, \$[4]}}{T_1} + \\ \frac{(-1 + T_1) p_{1, \$[4]} x_{1, \$[4]}}{T_1} - \pi_{1, \$[4]} \xi_{1, \$[2]} + x_{1,2} (\xi_{1, \$[2]} + \xi_{1, \$[4]}) - \pi_{2, \$[4]} \xi_{2, \$[2]} + \\ x_{2,2} (\xi_{2, \$[2]} + \xi_{2, \$[4]}) - \pi_{3, \$[4]} \xi_{3, \$[2]} + x_{3,2} (\xi_{3, \$[2]} + \xi_{3, \$[4]}) \right], \in \text{Series}[0] \left. \right\}$$

» EZip2 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \{ p_{1, \$[2]}, p_{1, \$[4]}, p_{2, \$[2]}, p_{2, \$[4]}, p_{3, \$[2]}, p_{3, \$[4]}, \pi_{1, \$[2]}, \pi_{1, \$[4]}, \pi_{2, \$[2]}, \pi_{2, \$[4]}, \pi_{3, \$[2]}, \pi_{3, \$[4]}, \right. \\ x_{1, \$[2]}, x_{1, \$[4]}, x_{2, \$[2]}, x_{2, \$[4]}, x_{3, \$[2]}, x_{3, \$[4]}, \xi_{1, \$[2]}, \xi_{1, \$[4]}, \xi_{2, \$[2]}, \xi_{2, \$[4]}, \xi_{3, \$[2]}, \xi_{3, \$[4]} \}, \\ p_{1, \$[2]} \pi_{1, \$[2]} + (-1 + T_1) p_{1, \$[2]} \pi_{1, \$[4]} + p_{1, \$[4]} \pi_{1, \$[4]} + p_{2, \$[2]} \pi_{2, \$[2]} + p_{2, \$[4]} \pi_{2, \$[4]} + p_{3, \$[2]} \pi_{3, \$[2]} + \\ p_{3, \$[4]} \pi_{3, \$[4]} + (1 - T_1) p_{1, \$[2]} x_{1, \$[2]} + \frac{(1 - 2 T_1 + T_1^2) p_{1, \$[2]} x_{1, \$[4]}}{T_1} + \frac{(-1 + T_1) p_{1, \$[4]} x_{1, \$[4]}}{T_1} - \\ \pi_{1, \$[4]} \xi_{1, \$[2]} + x_{1, \$[2]} \xi_{1, \$[2]} + \frac{(1 - T_1) x_{1, \$[4]} \xi_{1, \$[2]}}{T_1} + x_{1, \$[4]} \xi_{1, \$[4]} - \pi_{2, \$[4]} \xi_{2, \$[2]} + x_{2, \$[2]} \xi_{2, \$[2]} + \\ x_{2, \$[4]} \xi_{2, \$[4]} - \pi_{3, \$[4]} \xi_{3, \$[2]} + x_{3, \$[2]} \xi_{3, \$[2]} + x_{3, \$[4]} \xi_{3, \$[4]}, \mathbf{1}, p_{1,2} \pi_{1, \$[2]} + p_{1,2} \pi_{1, \$[4]} + \\ p_{2,2} \pi_{2, \$[2]} + p_{2,2} \pi_{2, \$[4]} + p_{3,2} \pi_{3, \$[2]} + p_{3,2} \pi_{3, \$[4]} + (-1 + T_1) p_{1,1} x_{1, \$[2]} + \frac{(1 - T_1) p_{1,1} x_{1, \$[4]}}{T_1} + \\ x_{1,2} \xi_{1, \$[2]} + x_{1,2} \xi_{1, \$[4]} + x_{2,2} \xi_{2, \$[2]} + x_{2,2} \xi_{2, \$[4]} + x_{3,2} \xi_{3, \$[2]} + x_{3,2} \xi_{3, \$[4]}, \in \text{Series}[0] \left. \right\}$$

» EZip3 called with $\{vs, \mathcal{F}, \omega, Q, P\} =$

$$\left\{ \{ p_{1, \$[2]}, p_{1, \$[4]}, p_{2, \$[2]}, p_{2, \$[4]}, p_{3, \$[2]}, p_{3, \$[4]}, \pi_{1, \$[2]}, \pi_{1, \$[4]}, \pi_{2, \$[2]}, \pi_{2, \$[4]}, \pi_{3, \$[2]}, \pi_{3, \$[4]}, \right. \\ x_{1, \$[2]}, x_{1, \$[4]}, x_{2, \$[2]}, x_{2, \$[4]}, x_{3, \$[2]}, x_{3, \$[4]}, \xi_{1, \$[2]}, \xi_{1, \$[4]}, \xi_{2, \$[2]}, \xi_{2, \$[4]}, \xi_{3, \$[2]}, \xi_{3, \$[4]} \}, \\ p_{1, \$[2]} \pi_{1, \$[2]} + (-1 + T_1) p_{1, \$[2]} \pi_{1, \$[4]} + p_{1, \$[4]} \pi_{1, \$[4]} + p_{2, \$[2]} \pi_{2, \$[2]} + p_{2, \$[4]} \pi_{2, \$[4]} + p_{3, \$[2]} \pi_{3, \$[2]} + \\ p_{3, \$[4]} \pi_{3, \$[4]} + (1 - T_1) p_{1, \$[2]} x_{1, \$[2]} + \frac{(1 - 2 T_1 + T_1^2) p_{1, \$[2]} x_{1, \$[4]}}{T_1} + \frac{(-1 + T_1) p_{1, \$[4]} x_{1, \$[4]}}{T_1} - \\ \pi_{1, \$[4]} \xi_{1, \$[2]} + x_{1, \$[2]} \xi_{1, \$[2]} + \frac{(1 - T_1) x_{1, \$[4]} \xi_{1, \$[2]}}{T_1} + x_{1, \$[4]} \xi_{1, \$[4]} - \pi_{2, \$[4]} \xi_{2, \$[2]} + \\ x_{2, \$[2]} \xi_{2, \$[2]} + x_{2, \$[4]} \xi_{2, \$[4]} - \pi_{3, \$[4]} \xi_{3, \$[2]} + x_{3, \$[2]} \xi_{3, \$[2]} + x_{3, \$[4]} \xi_{3, \$[4]}, \mathbf{1}, \mathbf{0}, \in \text{Series}[0] \left. \right\}$$

Out[*]=

$$\mathbb{E}_{\{\} \rightarrow \{1,2\}} [1, 0, \in \text{Series}[0]]$$

In[*]:= **\$k = 1;**

$$\mathbf{R}_{1,2} \bar{\mathbf{R}}_{3,4} // \mathbf{m}_{1,3 \rightarrow 1} // \mathbf{m}_{2,4 \rightarrow 2}$$

$$\begin{aligned} & \gg \mathbb{E} \left[1, (-1 + T_1) (-p_{1,2} + p_{1,[1]}) x_{1,2} + \left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,[3]}) x_{1,4}, \right. \\ & \in \text{Series} \left[0, \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,[1]}^2 x_{1,2}^2 - \frac{(-1 - T_1) p_{1,4} p_{1,[3]} x_{1,4}^2}{2 T_1^3} - \right. \\ & \left. \left. \frac{(1 - T_1) p_{1,[3]}^2 x_{1,4}^2}{2 T_1^3} + p_{1,2} p_{1,[1]} x_{1,2} x_{1,[1]} - \frac{p_{1,4} p_{1,[3]} x_{1,4} x_{1,[3]}}{T_1^2} - \frac{(-1 + T_1) p_{1,[3]}^2 x_{1,4} x_{1,[3]}}{T_1^2} \right] \right] \end{aligned}$$

$$\begin{aligned} & \gg \mathbb{E} [1, p_{1,1} (\pi_{1,[1]} + \pi_{1,[3]}) + p_{2,1} (\pi_{2,[1]} + \pi_{2,[3]}) + \\ & p_{3,1} (\pi_{3,[1]} + \pi_{3,[3]}) - \pi_{1,[3]} \xi_{1,[1]} + x_{1,1} (\xi_{1,[1]} + \xi_{1,[3]}) - \pi_{2,[3]} \xi_{2,[1]} + \\ & x_{2,1} (\xi_{2,[1]} + \xi_{2,[3]}) - \pi_{3,[3]} \xi_{3,[1]} + x_{3,1} (\xi_{3,[1]} + \xi_{3,[3]})], \in \text{Series}[0, 0]] \end{aligned}$$

$$\begin{aligned} & \gg \mathbb{E} [1, p_{1,1} (\pi_{1,[1]} + \pi_{1,[3]}) + p_{2,1} (\pi_{2,[1]} + \pi_{2,[3]}) + p_{3,1} (\pi_{3,[1]} + \pi_{3,[3]}) + \\ & (-1 + T_1) (-p_{1,2} + p_{1,[1]}) x_{1,2} + \left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,[3]}) x_{1,4} - \pi_{1,[3]} \xi_{1,[1]} + \\ & x_{1,1} (\xi_{1,[1]} + \xi_{1,[3]}) - \pi_{2,[3]} \xi_{2,[1]} + x_{2,1} (\xi_{2,[1]} + \xi_{2,[3]}) - \pi_{3,[3]} \xi_{3,[1]} + x_{3,1} (\xi_{3,[1]} + \xi_{3,[3]})], \\ & \in \text{Series} \left[0, \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,[1]}^2 x_{1,2}^2 - \frac{(-1 - T_1) p_{1,4} p_{1,[3]} x_{1,4}^2}{2 T_1^3} - \right. \\ & \left. \frac{(1 - T_1) p_{1,[3]}^2 x_{1,4}^2}{2 T_1^3} + p_{1,2} p_{1,[1]} x_{1,2} x_{1,[1]} - \frac{p_{1,4} p_{1,[3]} x_{1,4} x_{1,[3]}}{T_1^2} - \frac{(-1 + T_1) p_{1,[3]}^2 x_{1,4} x_{1,[3]}}{T_1^2} \right] \end{aligned}$$

» EZip called with {vs,F,E} =

$$\begin{aligned} & \left\{ \{ p_{1,[1]}, p_{1,[3]}, p_{2,[1]}, p_{2,[3]}, p_{3,[1]}, p_{3,[3]}, \pi_{1,[1]}, \pi_{1,[3]}, \pi_{2,[1]}, \pi_{2,[3]}, \pi_{3,[1]}, \pi_{3,[3]}, \right. \\ & x_{1,[1]}, x_{1,[3]}, x_{2,[1]}, x_{2,[3]}, x_{3,[1]}, x_{3,[3]}, \xi_{1,[1]}, \xi_{1,[3]}, \xi_{2,[1]}, \xi_{2,[3]}, \xi_{3,[1]}, \xi_{3,[3]} \}, \\ & p_{1,[1]} \pi_{1,[1]} + p_{1,[3]} \pi_{1,[3]} + p_{2,[1]} \pi_{2,[1]} + p_{2,[3]} \pi_{2,[3]} + p_{3,[1]} \pi_{3,[1]} + p_{3,[3]} \pi_{3,[3]} + \\ & x_{1,[1]} \xi_{1,[1]} + x_{1,[3]} \xi_{1,[3]} + x_{2,[1]} \xi_{2,[1]} + x_{2,[3]} \xi_{2,[3]} + x_{3,[1]} \xi_{3,[1]} + x_{3,[3]} \xi_{3,[3]}, \\ & \mathbb{E} [1, p_{1,1} (\pi_{1,[1]} + \pi_{1,[3]}) + p_{2,1} (\pi_{2,[1]} + \pi_{2,[3]}) + p_{3,1} (\pi_{3,[1]} + \pi_{3,[3]}) + \\ & (-1 + T_1) (-p_{1,2} + p_{1,[1]}) x_{1,2} + \left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,[3]}) x_{1,4} - \pi_{1,[3]} \xi_{1,[1]} + \\ & x_{1,1} (\xi_{1,[1]} + \xi_{1,[3]}) - \pi_{2,[3]} \xi_{2,[1]} + x_{2,1} (\xi_{2,[1]} + \xi_{2,[3]}) - \pi_{3,[3]} \xi_{3,[1]} + x_{3,1} (\xi_{3,[1]} + \xi_{3,[3]})], \\ & \in \text{Series} \left[0, \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,[1]}^2 x_{1,2}^2 - \frac{(-1 - T_1) p_{1,4} p_{1,[3]} x_{1,4}^2}{2 T_1^3} - \right. \\ & \left. \frac{(1 - T_1) p_{1,[3]}^2 x_{1,4}^2}{2 T_1^3} + p_{1,2} p_{1,[1]} x_{1,2} x_{1,[1]} - \frac{p_{1,4} p_{1,[3]} x_{1,4} x_{1,[3]}}{T_1^2} - \frac{(-1 + T_1) p_{1,[3]}^2 x_{1,4} x_{1,[3]}}{T_1^2} \right] \end{aligned}$$

» EZip1 called with {vs,F,ω,Q,P} =

$$\left\{ \left\{ p_{1,[1]}, p_{1,[3]}, p_{2,[1]}, p_{2,[3]}, p_{3,[1]}, p_{3,[3]}, \pi_{1,[1]}, \pi_{1,[3]}, \pi_{2,[1]}, \pi_{2,[3]}, \pi_{3,[1]}, \pi_{3,[3]}, \right. \right.$$

$$x_{1,[1]}, x_{1,[3]}, x_{2,[1]}, x_{2,[3]}, x_{3,[1]}, x_{3,[3]}, \xi_{1,[1]}, \xi_{1,[3]}, \xi_{2,[1]}, \xi_{2,[3]}, \xi_{3,[1]}, \xi_{3,[3]}, \left. \right\},$$

$$p_{1,[1]} \pi_{1,[1]} + p_{1,[3]} \pi_{1,[3]} + p_{2,[1]} \pi_{2,[1]} + p_{2,[3]} \pi_{2,[3]} + p_{3,[1]} \pi_{3,[1]} + p_{3,[3]} \pi_{3,[3]} +$$

$$x_{1,[1]} \xi_{1,[1]} + x_{1,[3]} \xi_{1,[3]} + x_{2,[1]} \xi_{2,[1]} + x_{2,[3]} \xi_{2,[3]} + x_{3,[1]} \xi_{3,[1]} + x_{3,[3]} \xi_{3,[3]}, \mathbf{1},$$

$$p_{1,1} (\pi_{1,[1]} + \pi_{1,[3]}) + p_{2,1} (\pi_{2,[1]} + \pi_{2,[3]}) + p_{3,1} (\pi_{3,[1]} + \pi_{3,[3]}) + (-1 + T_1) (-p_{1,2} + p_{1,[1]}) x_{1,2} +$$

$$\left(-1 + \frac{1}{T_1} \right) (-p_{1,4} + p_{1,[3]}) x_{1,4} - \pi_{1,[3]} \xi_{1,[1]} + x_{1,1} (\xi_{1,[1]} + \xi_{1,[3]}) -$$

$$\pi_{2,[3]} \xi_{2,[1]} + x_{2,1} (\xi_{2,[1]} + \xi_{2,[3]}) - \pi_{3,[3]} \xi_{3,[1]} + x_{3,1} (\xi_{3,[1]} + \xi_{3,[3]}) ,$$

$$\in \text{Series} \left[0, \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,[1]}^2 x_{1,2}^2 - \frac{(-1 - T_1) p_{1,4} p_{1,[3]} x_{1,4}^2}{2 T_1^3} - \right.$$

$$\left. \frac{(1 - T_1) p_{1,[3]}^2 x_{1,4}^2}{2 T_1^3} + p_{1,2} p_{1,[1]} x_{1,2} x_{1,[1]} - \frac{p_{1,4} p_{1,[3]} x_{1,4} x_{1,[3]}}{T_1^2} - \frac{(-1 + T_1) p_{1,[3]}^2 x_{1,4} x_{1,[3]}}{T_1^2} \right] \left. \right\}$$

» EZip2 called with {vs,F,ω,Q,P} =

$$\left\{ \left\{ p_{1,[1]}, p_{1,[3]}, p_{2,[1]}, p_{2,[3]}, p_{3,[1]}, p_{3,[3]}, \pi_{1,[1]}, \pi_{1,[3]}, \pi_{2,[1]}, \pi_{2,[3]}, \pi_{3,[1]}, \pi_{3,[3]}, \right. \right.$$

$$x_{1,[1]}, x_{1,[3]}, x_{2,[1]}, x_{2,[3]}, x_{3,[1]}, x_{3,[3]}, \xi_{1,[1]}, \xi_{1,[3]}, \xi_{2,[1]}, \xi_{2,[3]}, \xi_{3,[1]}, \xi_{3,[3]}, \left. \right\},$$

$$p_{1,[1]} \pi_{1,[1]} + p_{1,[3]} \pi_{1,[3]} + p_{2,[1]} \pi_{2,[1]} + p_{2,[3]} \pi_{2,[3]} + p_{3,[1]} \pi_{3,[1]} + p_{3,[3]} \pi_{3,[3]} -$$

$$\pi_{1,[3]} \xi_{1,[1]} + x_{1,[1]} \xi_{1,[1]} + x_{1,[3]} \xi_{1,[3]} - \pi_{2,[3]} \xi_{2,[1]} + x_{2,[1]} \xi_{2,[1]} + x_{2,[3]} \xi_{2,[3]} -$$

$$\pi_{3,[3]} \xi_{3,[1]} + x_{3,[1]} \xi_{3,[1]} + x_{3,[3]} \xi_{3,[3]}, \mathbf{1}, p_{1,1} \pi_{1,[1]} + p_{1,1} \pi_{1,[3]} + p_{2,1} \pi_{2,[1]} +$$

$$p_{2,1} \pi_{2,[3]} + p_{3,1} \pi_{3,[1]} + p_{3,1} \pi_{3,[3]} + (1 - T_1) p_{1,2} x_{1,2} + (-1 + T_1) p_{1,[1]} x_{1,2} + \frac{(-1 + T_1) p_{1,4} x_{1,4}}{T_1} +$$

$$\frac{(1 - T_1) p_{1,[3]} x_{1,4}}{T_1} + x_{1,1} \xi_{1,[1]} + x_{1,1} \xi_{1,[3]} + x_{2,1} \xi_{2,[1]} + x_{2,1} \xi_{2,[3]} + x_{3,1} \xi_{3,[1]} + x_{3,1} \xi_{3,[3]},$$

$$\in \text{Series} \left[0, \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,[1]}^2 x_{1,2}^2 - \frac{(-1 - T_1) p_{1,4} p_{1,[3]} x_{1,4}^2}{2 T_1^3} - \right.$$

$$\left. \frac{(1 - T_1) p_{1,[3]}^2 x_{1,4}^2}{2 T_1^3} + p_{1,2} p_{1,[1]} x_{1,2} x_{1,[1]} - \frac{p_{1,4} p_{1,[3]} x_{1,4} x_{1,[3]}}{T_1^2} - \frac{(-1 + T_1) p_{1,[3]}^2 x_{1,4} x_{1,[3]}}{T_1^2} \right] \left. \right\}$$

» EZip3 called with {vs,F,ω,Q,P} =

$$\left\{ \begin{aligned} & \{ p_{1,\$[1]}, p_{1,\$[3]}, p_{2,\$[1]}, p_{2,\$[3]}, p_{3,\$[1]}, p_{3,\$[3]}, \pi_{1,\$[1]}, \pi_{1,\$[3]}, \pi_{2,\$[1]}, \pi_{2,\$[3]}, \pi_{3,\$[1]}, \pi_{3,\$[3]}, \\ & x_{1,\$[1]}, x_{1,\$[3]}, x_{2,\$[1]}, x_{2,\$[3]}, x_{3,\$[1]}, x_{3,\$[3]}, \xi_{1,\$[1]}, \xi_{1,\$[3]}, \xi_{2,\$[1]}, \xi_{2,\$[3]}, \xi_{3,\$[1]}, \xi_{3,\$[3]} \}, \\ & p_{1,\$[1]} \pi_{1,\$[1]} + p_{1,\$[3]} \pi_{1,\$[3]} + p_{2,\$[1]} \pi_{2,\$[1]} + p_{2,\$[3]} \pi_{2,\$[3]} + p_{3,\$[1]} \pi_{3,\$[1]} + \\ & p_{3,\$[3]} \pi_{3,\$[3]} - \pi_{1,\$[3]} \xi_{1,\$[1]} + x_{1,\$[1]} \xi_{1,\$[1]} + x_{1,\$[3]} \xi_{1,\$[3]} - \pi_{2,\$[3]} \xi_{2,\$[1]} + \\ & x_{2,\$[1]} \xi_{2,\$[1]} + x_{2,\$[3]} \xi_{2,\$[3]} - \pi_{3,\$[3]} \xi_{3,\$[1]} + x_{3,\$[1]} \xi_{3,\$[1]} + x_{3,\$[3]} \xi_{3,\$[3]}, \\ & 1, (-1 + T_1) p_{1,1} x_{1,2} + (1 - T_1) p_{1,2} x_{1,2} + \frac{(1 - T_1) p_{1,1} x_{1,4}}{T_1} + \frac{(-1 + T_1) p_{1,4} x_{1,4}}{T_1}, \\ & \in \text{Series} \left[0, p_{1,1} p_{1,2} x_{1,1} x_{1,2} + p_{1,2} p_{1,\$[1]} x_{1,1} x_{1,2} + \frac{1}{2} (-1 + T_1) p_{1,1}^2 x_{1,2}^2 + \frac{1}{2} (1 - 3 T_1) p_{1,1} p_{1,2} x_{1,2}^2 + \right. \\ & (-1 + T_1) p_{1,1} p_{1,\$[1]} x_{1,2}^2 + \frac{1}{2} (1 - 3 T_1) p_{1,2} p_{1,\$[1]} x_{1,2}^2 + \frac{1}{2} (-1 + T_1) p_{1,\$[1]}^2 x_{1,2}^2 + \frac{(1 - T_1) p_{1,1}^2 x_{1,1} x_{1,4}}{T_1^2} - \\ & \frac{p_{1,1} p_{1,4} x_{1,1} x_{1,4}}{T_1^2} + \frac{(2 - 2 T_1) p_{1,1} p_{1,\$[3]} x_{1,1} x_{1,4}}{T_1^2} - \frac{p_{1,4} p_{1,\$[3]} x_{1,1} x_{1,4}}{T_1^2} + \frac{(1 - T_1) p_{1,\$[3]}^2 x_{1,1} x_{1,4}}{T_1^2} + \\ & \frac{(-1 + T_1) p_{1,1} p_{1,2} x_{1,2} x_{1,4}}{T_1} + \frac{(-1 + T_1) p_{1,2} p_{1,\$[1]} x_{1,2} x_{1,4}}{T_1} + \frac{(-1 + T_1) p_{1,1}^2 x_{1,4}^2}{2 T_1^3} + \\ & \frac{(1 + T_1) p_{1,1} p_{1,4} x_{1,4}^2}{2 T_1^3} + \frac{(-1 + T_1) p_{1,1} p_{1,\$[3]} x_{1,4}^2}{T_1^3} + \frac{(1 + T_1) p_{1,4} p_{1,\$[3]} x_{1,4}^2}{2 T_1^3} + \frac{(-1 + T_1) p_{1,\$[3]}^2 x_{1,4}^2}{2 T_1^3} + \\ & p_{1,1} p_{1,2} x_{1,2} x_{1,\$[1]} + p_{1,2} p_{1,\$[1]} x_{1,2} x_{1,\$[1]} + \frac{(1 - T_1) p_{1,1}^2 x_{1,4} x_{1,\$[3]}}{T_1^2} - \frac{p_{1,1} p_{1,4} x_{1,4} x_{1,\$[3]}}{T_1^2} + \\ & \left. \left. \frac{(2 - 2 T_1) p_{1,1} p_{1,\$[3]} x_{1,4} x_{1,\$[3]}}{T_1^2} - \frac{p_{1,4} p_{1,\$[3]} x_{1,4} x_{1,\$[3]}}{T_1^2} + \frac{(1 - T_1) p_{1,\$[3]}^2 x_{1,4} x_{1,\$[3]}}{T_1^2} \right] \right\} \end{aligned} \right.$$

Out[*]=

\$Aborted

In[*]:= \$k

Out[*]=

1

In[*]:= eSeries[0]

Out[*]=

eSeries[0, 0]

In[*]:= m1,3-1

Out[*]=

$$\mathbb{E}_{\{1,3\} \rightarrow \{1\}} [1, p_{1,1} (\pi_{1,1} + \pi_{1,3}) + p_{2,1} (\pi_{2,1} + \pi_{2,3}) + p_{3,1} (\pi_{3,1} + \pi_{3,3}) - \pi_{1,3} \xi_{1,1} + x_{1,1} (\xi_{1,1} + \xi_{1,3}) - \pi_{2,3} \xi_{2,1} + x_{2,1} (\xi_{2,1} + \xi_{2,3}) - \pi_{3,3} \xi_{3,1} + x_{3,1} (\xi_{3,1} + \xi_{3,3}), \in \text{Series}[0, 0]]$$

In[*]:= E_{1,3} -> {1} [1, p1,1 (pi1,1 + pi1,3) + p2,1 (pi2,1 + pi2,3) + p3,1 (pi3,1 + pi3,3) - pi1,3 xi1,1 +

$$x_{1,1} (\xi_{1,1} + \xi_{1,3}) - \pi_{2,3} \xi_{2,1} + x_{2,1} (\xi_{2,1} + \xi_{2,3}) - \pi_{3,3} \xi_{3,1} + x_{3,1} (\xi_{3,1} + \xi_{3,3}), \in \text{Series}[0]]$$

Out[*]=

$$\mathbb{E}_{\{1,3\} \rightarrow \{1\}} [1, p_{1,1} (\pi_{1,1} + \pi_{1,3}) + p_{2,1} (\pi_{2,1} + \pi_{2,3}) + p_{3,1} (\pi_{3,1} + \pi_{3,3}) - \pi_{1,3} \xi_{1,1} + x_{1,1} (\xi_{1,1} + \xi_{1,3}) - \pi_{2,3} \xi_{2,1} + x_{2,1} (\xi_{2,1} + \xi_{2,3}) - \pi_{3,3} \xi_{3,1} + x_{3,1} (\xi_{3,1} + \xi_{3,3}), \in \text{Series}[0, 0]]$$

In[*]:= **? eSeries**

Out[*]=

Symbol
Global`eSeries
UpValue Definitions
$S1_eSeries \equiv S2_eSeries \wedge := \text{Length}[S1] == \text{Length}[S2] \ \&\& \ \text{Inner}[\text{CF}[\#1] == \text{CF}[\#2] \ \&, S1, S2, \text{And}]$
$S1_eSeries + S2_eSeries \wedge :=$ $eSeries @@ \text{Table}[S1[[k]] + S2[[k]], \{k, \text{Min}[\text{Length}[S1], \text{Length}[S2]]\}]$
$S1_eSeries S2_eSeries \wedge :=$ $eSeries @@ \text{Table}\left[\sum_{j=0}^k S1[[j+1]] S2[[k-j+1]], \{k, 0, \text{Min}[\text{Length}[S1], \text{Length}[S2]] - 1\}\right]$
$c_S_eSeries \wedge := (c \ \#1 \ \&) /@ S$
$\partial_{vs_} S_eSeries \wedge := \text{Function}[s, \partial_{vs} s] /@ S$
DownValue Definitions
$eSeries[0] /; \$k > 0 := eSeries @@ \text{Table}[0, \$k + 1]$
Full Name Global`eSeries