

**CoefficientRules**[Series[e<sup>a x</sup>, {x, 0, 3}], a]

$$\{\{\emptyset\} \rightarrow 1 + a x + \frac{a^2 x^2}{2} + \frac{a^3 x^3}{6} + O[x]^4\}$$

**Series**[e<sup>(a+b) x</sup>, {x, 0, 3}]

$$1 + (a + b) x + \frac{1}{2} (a + b)^2 x^2 + \frac{1}{6} (a + b)^3 x^3 + O[x]^4$$

**Series**[e<sup>(a+b) x</sup>, {x, 0, 3}] // **Expand**

$$1 + (a + b) x + \frac{1}{2} (a + b)^2 x^2 + \frac{1}{6} (a + b)^3 x^3 + O[x]^4$$

**Series**[e<sup>(a+b) x</sup>, {x, 0, 3}] // **FullForm**

SeriesData[x, 0, List[1, Plus[a, b], Times[Rational[1, 2], Power[Plus[a, b], 2]], Times[Rational[1, 6], Power[Plus[a, b], 3]]], 0, 4, 1]

**? MapAt**

MapAt[f, expr, n] applies f to the element at position n in expr. If n is negative, the position is counted from the end.

MapAt[f, expr, {i, j, ...}] applies f to the part of expr at position {i, j, ...}.

MapAt[f, expr, {{i1, j1, ...}, {i2, j2, ...}, ...}] applies f to parts of expr at several positions.

MapAt[f, pos] represents an operator form of MapAt that can be applied to an expression. >>

**co**

$$\mathbb{E}_{CU} [\{y_1, a_1, x_1\}_1, \{y_2, a_2, x_2\}_2, \{y_3, a_3, x_3\}_3, \hbar (x_1 y_1 \gamma_{11} + x_2 y_1 \gamma_{12} + x_3 y_1 \gamma_{13} + x_1 y_2 \gamma_{21} + x_2 y_2 \gamma_{22} + x_3 y_2 \gamma_{23} + x_1 y_3 \gamma_{31} + x_2 y_3 \gamma_{32} + x_3 y_3 \gamma_{33} + a_1 t_1 \lambda_{11} + a_2 t_1 \lambda_{12} + a_3 t_1 \lambda_{13} + a_1 t_2 \lambda_{21} + a_2 t_2 \lambda_{22} + a_3 t_2 \lambda_{23} + a_1 t_3 \lambda_{31} + a_2 t_3 \lambda_{32} + a_3 t_3 \lambda_{33}), 1 + O[\epsilon]^2]$$

**co** // m<sub>1,2→1</sub>

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$$\left\{ \left\{ \left\{ x_1, \nu_{4985} \right\}, \left\{ y_2, \omega_{4985} \right\} \right\}, 1 + O[\epsilon]^2, \frac{1}{1 + \delta_{4985} t_2} e^{\frac{-\nu_{4985} \omega_{4985} t_2 + \nu_{4985} x_{n4985} + \omega_{4985} y_{n4985} + \delta_{4985} x_{n4985} y_{n4985}}{1 + \delta_{4985} t_2}} \right\} + \left( e^{\frac{-\nu_{4985} \omega_{4985} t_2 + \nu_{4985} x_{n4985} + \omega_{4985} y_{n4985} + \delta_{4985} x_{n4985} y_{n4985}}{1 + \delta_{4985} t_2}} \right)$$

$$\left( \frac{4 \nu_{4985} \omega_{4985} a_{n4985} + \gamma \nu_{4985}^2 \omega_{4985}^2 t_2 - 2 \gamma \nu_{4985}^2 \omega_{4985} x_{n4985} - 2 \gamma \nu_{4985} \omega_{4985}^2 y_{n4985}}{\epsilon} \right) / \left( 2 (1 + \delta_{4985} t_2) \right) + \frac{1}{24 (1 + \delta_{4985} t_2)} e^{\frac{-\nu_{4985} \omega_{4985} t_2 + \nu_{4985} x_{n4985} + \omega_{4985} y_{n4985} + \delta_{4985} x_{n4985} y_{n4985}}{1 + \delta_{4985} t_2}}$$

$$\left( -24 \gamma \nu_{4985}^2 \omega_{4985}^2 a_{n4985} + 48 \nu_{4985}^2 \omega_{4985}^2 a_{n4985}^2 - 8 \gamma^2 \nu_{4985}^3 \omega_{4985}^3 t_2 + 24 \gamma \nu_{4985}^3 \omega_{4985}^3 a_{n4985} t_2 + 3 \gamma^2 \nu_{4985}^4 \omega_{4985}^4 t_2^2 + 24 \gamma^2 \nu_{4985}^3 \omega_{4985}^2 x_{n4985} - 48 \gamma \nu_{4985}^3 \omega_{4985}^2 a_{n4985} x_{n4985} - 12 \gamma^2 \nu_{4985}^4 \omega_{4985}^3 t_2 x_{n4985} + 12 \gamma^2 \nu_{4985}^4 \omega_{4985}^2 x_{n4985}^2 + 24 \gamma^2 \nu_{4985}^2 \omega_{4985}^3 y_{n4985} - 48 \gamma \nu_{4985}^2 \omega_{4985}^3 a_{n4985} y_{n4985} - 12 \gamma^2 \nu_{4985}^3 \omega_{4985}^4 t_2 y_{n4985} + 24 \gamma^2 \nu_{4985}^3 \omega_{4985}^3 x_{n4985} y_{n4985} + 12 \gamma^2 \nu_{4985}^2 \omega_{4985}^4 y_{n4985}^2 \right) \epsilon^2 + O[\epsilon]^3 \}$$

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$$\begin{aligned} & \mathbb{E}_{\text{CU}} \left[ \{Y_3, a_3, X_3\}_3, \{Y_1, a_1, Y_{\$133}, a_{\$133}, X_{\$133}, a_2, X_2\}_2, \right. \\ & \frac{1}{1 + \hbar t_2 \gamma_{21}} \left( \hbar X_{\$133} Y_1 \gamma_{11} + \hbar X_2 Y_1 \gamma_{12} + \hbar X_3 Y_1 \gamma_{13} + \hbar X_{\$133} Y_{\$133} \gamma_{21} + \hbar^2 t_2 X_2 Y_1 \gamma_{12} \gamma_{21} + \right. \\ & \hbar^2 t_2 X_3 Y_1 \gamma_{13} \gamma_{21} + \hbar X_2 Y_{\$133} \gamma_{22} - \hbar^2 t_2 X_2 Y_1 \gamma_{11} \gamma_{22} + \hbar X_3 Y_{\$133} \gamma_{23} - \hbar^2 t_2 X_3 Y_1 \gamma_{11} \gamma_{23} + \\ & \hbar X_{\$133} Y_3 \gamma_{31} - \hbar^2 t_2 X_2 Y_3 \gamma_{22} \gamma_{31} - \hbar^2 t_2 X_3 Y_3 \gamma_{23} \gamma_{31} + \hbar X_2 Y_3 \gamma_{32} + \hbar^2 t_2 X_2 Y_3 \gamma_{21} \gamma_{32} + \hbar X_3 Y_3 \gamma_{33} + \\ & \hbar^2 t_2 X_3 Y_3 \gamma_{21} \gamma_{33} + \hbar a_1 t_2 \lambda_{11} + \hbar^2 a_1 t_2^2 \gamma_{21} \lambda_{11} + \hbar a_2 t_2 \lambda_{12} + \hbar^2 a_2 t_2^2 \gamma_{21} \lambda_{12} + \hbar a_3 t_2 \lambda_{13} + \\ & \hbar^2 a_3 t_2^2 \gamma_{21} \lambda_{13} + \hbar a_1 t_2 \lambda_{21} + \hbar^2 a_1 t_2^2 \gamma_{21} \lambda_{21} + \hbar a_2 t_2 \lambda_{22} + \hbar^2 a_2 t_2^2 \gamma_{21} \lambda_{22} + \hbar a_3 t_2 \lambda_{23} + \hbar^2 a_3 t_2^2 \gamma_{21} \lambda_{23} + \\ & \left. \hbar a_1 t_3 \lambda_{31} + \hbar^2 a_1 t_2 t_3 \gamma_{21} \lambda_{31} + \hbar a_2 t_3 \lambda_{32} + \hbar^2 a_2 t_2 t_3 \gamma_{21} \lambda_{32} + \hbar a_3 t_3 \lambda_{33} + \hbar^2 a_3 t_2 t_3 \gamma_{21} \lambda_{33} \right), \\ & \frac{1}{1 + \hbar t_2 \gamma_{21}} + \frac{1}{2(1 + \hbar t_2 \gamma_{21})} \left( 4 \hbar^2 a_{\$133} X_2 Y_1 \gamma_{11} \gamma_{22} - 2 \gamma \hbar^3 X_2 X_{\$133} Y_1^2 \gamma_{11}^2 \gamma_{22} - 2 \gamma \hbar^3 X_2^2 Y_1 Y_{\$133} \gamma_{11} \gamma_{22}^2 + \right. \\ & \gamma \hbar^4 t_2 X_2^2 Y_1^2 \gamma_{11}^2 \gamma_{22}^2 + 4 \hbar^2 a_{\$133} X_3 Y_1 \gamma_{11} \gamma_{23} - 2 \gamma \hbar^3 X_3 X_{\$133} Y_1^2 \gamma_{11}^2 \gamma_{23} - 4 \gamma \hbar^3 X_2 X_3 Y_1 Y_{\$133} \gamma_{11} \gamma_{22} \gamma_{23} + \\ & 2 \gamma \hbar^4 t_2 X_2 X_3 Y_1^2 \gamma_{11}^2 \gamma_{22} \gamma_{23} - 2 \gamma \hbar^3 X_2^2 Y_1 Y_{\$133} \gamma_{11} \gamma_{23}^2 + \gamma \hbar^4 t_2 X_2^2 Y_1^2 \gamma_{11}^2 \gamma_{23}^2 + 4 \hbar^2 a_{\$133} X_2 Y_3 \gamma_{22} \gamma_{31} - \\ & 4 \gamma \hbar^3 X_2 X_{\$133} Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{31} - 2 \gamma \hbar^3 X_2^2 Y_3 Y_{\$133} \gamma_{22}^2 \gamma_{31} + 2 \gamma \hbar^4 t_2 X_2^2 Y_1 Y_3 \gamma_{11} \gamma_{22}^2 \gamma_{31} + 4 \hbar^2 a_{\$133} X_3 Y_3 \gamma_{23} \\ & \gamma_{31} - 4 \gamma \hbar^3 X_3 X_{\$133} Y_1 Y_3 \gamma_{11} \gamma_{23} \gamma_{31} - 4 \gamma \hbar^3 X_2 X_3 Y_3 Y_{\$133} \gamma_{22} \gamma_{23} \gamma_{31} + 4 \gamma \hbar^4 t_2 X_2 X_3 Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} - \\ & 2 \gamma \hbar^3 X_2^2 Y_3 Y_{\$133} \gamma_{23}^2 \gamma_{31} + 2 \gamma \hbar^4 t_2 X_2^2 Y_1 Y_3 \gamma_{11} \gamma_{23}^2 \gamma_{31} - 2 \gamma \hbar^3 X_2 X_{\$133} Y_3^2 \gamma_{22} \gamma_{31}^2 + \gamma \hbar^4 t_2 X_2^2 Y_3^2 \gamma_{22}^2 \gamma_{31}^2 - \\ & \left. 2 \gamma \hbar^3 X_3 X_{\$133} Y_3^2 \gamma_{23} \gamma_{31}^2 + 2 \gamma \hbar^4 t_2 X_2 X_3 Y_3^2 \gamma_{22} \gamma_{23} \gamma_{31}^2 + \gamma \hbar^4 t_2 X_3^2 Y_3^2 \gamma_{23}^2 \gamma_{31}^2 \right) \in + O[\epsilon]^2 \end{aligned}$$

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$$\begin{aligned} & \left\{ \left\{ \{a_1, \nu_{\$5048}\}, \{Y_{\$133}, \omega_{\$5048}\} \right\}, \right. \\ & \frac{1}{1 + \hbar t_2 \gamma_{21}} + \frac{1}{2(1 + \hbar t_2 \gamma_{21})} \left( 4 \hbar^2 a_{\$133} X_2 Y_1 \gamma_{11} \gamma_{22} - 2 \gamma \hbar^3 X_2 X_{\$133} Y_1^2 \gamma_{11}^2 \gamma_{22} - \right. \\ & 2 \gamma \hbar^3 X_2^2 Y_1 Y_{\$133} \gamma_{11} \gamma_{22}^2 + \gamma \hbar^4 t_2 X_2^2 Y_1^2 \gamma_{11}^2 \gamma_{22}^2 + 4 \hbar^2 a_{\$133} X_3 Y_1 \gamma_{11} \gamma_{23} - 2 \gamma \hbar^3 X_3 X_{\$133} Y_1^2 \gamma_{11}^2 \gamma_{23} - \\ & 4 \gamma \hbar^3 X_2 X_3 Y_1 Y_{\$133} \gamma_{11} \gamma_{22} \gamma_{23} + 2 \gamma \hbar^4 t_2 X_2 X_3 Y_1^2 \gamma_{11}^2 \gamma_{22} \gamma_{23} - 2 \gamma \hbar^3 X_2^2 Y_1 Y_{\$133} \gamma_{11} \gamma_{23}^2 + \\ & \gamma \hbar^4 t_2 X_2^2 Y_1^2 \gamma_{11}^2 \gamma_{23}^2 + 4 \hbar^2 a_{\$133} X_2 Y_3 \gamma_{22} \gamma_{31} - 4 \gamma \hbar^3 X_2 X_{\$133} Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{31} - 2 \gamma \hbar^3 X_2^2 Y_3 Y_{\$133} \gamma_{22}^2 \gamma_{31} + \\ & 2 \gamma \hbar^4 t_2 X_2^2 Y_1 Y_3 \gamma_{11} \gamma_{22}^2 \gamma_{31} + 4 \hbar^2 a_{\$133} X_3 Y_3 \gamma_{23} \gamma_{31} - 4 \gamma \hbar^3 X_3 X_{\$133} Y_1 Y_3 \gamma_{11} \gamma_{23} \gamma_{31} - \\ & 4 \gamma \hbar^3 X_2 X_3 Y_3 Y_{\$133} \gamma_{22} \gamma_{23} \gamma_{31} + 4 \gamma \hbar^4 t_2 X_2 X_3 Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} - 2 \gamma \hbar^3 X_2^2 Y_3 Y_{\$133} \gamma_{23}^2 \gamma_{31} + \\ & 2 \gamma \hbar^4 t_2 X_2^2 Y_1 Y_3 \gamma_{11} \gamma_{23}^2 \gamma_{31} - 2 \gamma \hbar^3 X_2 X_{\$133} Y_3^2 \gamma_{22} \gamma_{31}^2 + \gamma \hbar^4 t_2 X_2^2 Y_3^2 \gamma_{22}^2 \gamma_{31}^2 - 2 \gamma \hbar^3 X_3 X_{\$133} Y_3^2 \gamma_{23} \gamma_{31}^2 + \\ & \left. 2 \gamma \hbar^4 t_2 X_2 X_3 Y_3^2 \gamma_{22} \gamma_{23} \gamma_{31}^2 + \gamma \hbar^4 t_2 X_3^2 Y_3^2 \gamma_{23}^2 \gamma_{31}^2 \right) \in + O[\epsilon]^2, e^{\nu_{\$5048} a_{n\$5048} + \epsilon^{-\gamma \nu_{\$5048}} \omega_{n\$5048}} + O[\epsilon]^3 \end{aligned}$$



$$\begin{aligned}
 & \gg \left\{ \left\{ \{y_1, \nu_{5058}\}, \{y_{\$134}, \omega_{5058}\} \right\}, \frac{1}{1 + \hbar t_2 \gamma_{21}} + \frac{1}{2(1 + \hbar t_2 \gamma_{21})} \right. \\
 & e^{-\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \left( 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \hbar^2 a_{\$133} x_2 y_1 \gamma_{11} \gamma_{22} - \right. \\
 & 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_2 x_{\$133} y_1^2 \gamma_{11}^2 \gamma_{22} - 2 \gamma \hbar^3 x_2^2 y_1 y_{\$134} \gamma_{11} \gamma_{22}^2 + \\
 & e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2^2 y_1^2 \gamma_{11}^2 \gamma_{22}^2 + 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \\
 & \hbar^2 a_{\$133} x_3 y_1 \gamma_{11} \gamma_{23} - 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_3 x_{\$133} y_1^2 \gamma_{11}^2 \gamma_{23} - \\
 & 4 \gamma \hbar^3 x_2 x_3 y_1 y_{\$134} \gamma_{11} \gamma_{22} \gamma_{23} + 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2 x_3 y_1^2 \gamma_{11}^2 \gamma_{22} \gamma_{23} - \\
 & 2 \gamma \hbar^3 x_3^2 y_1 y_{\$134} \gamma_{11} \gamma_{23}^2 + e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_3^2 y_1^2 \gamma_{11}^2 \gamma_{23}^2 + \\
 & 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \hbar^2 a_{\$133} x_2 y_3 \gamma_{22} \gamma_{31} - \\
 & 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_2 x_{\$133} y_1 y_3 \gamma_{11} \gamma_{22} \gamma_{31} - \\
 & 2 \gamma \hbar^3 x_2^2 y_3 y_{\$134} \gamma_{22}^2 \gamma_{31} + 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2^2 y_1 y_3 \gamma_{11} \gamma_{22}^2 \gamma_{31} + \\
 & 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \hbar^2 a_{\$133} x_3 y_3 \gamma_{23} \gamma_{31} - \\
 & 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_3 x_{\$133} y_1 y_3 \gamma_{11} \gamma_{23} \gamma_{31} - 4 \gamma \hbar^3 x_2 x_3 y_3 y_{\$134} \gamma_{22} \gamma_{23} \gamma_{31} + \\
 & 4 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2 x_3 y_1 y_3 \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} - \\
 & 2 \gamma \hbar^3 x_3^2 y_3 y_{\$134} \gamma_{23}^2 \gamma_{31} + 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_3^2 y_1 y_3 \gamma_{11} \gamma_{23}^2 \gamma_{31} - \\
 & 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_2 x_{\$133} y_3^2 \gamma_{22} \gamma_{31}^2 + \\
 & e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2^2 y_3^2 \gamma_{22}^2 \gamma_{31}^2 - \\
 & 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^3 x_3 x_{\$133} y_3^2 \gamma_{23} \gamma_{31}^2 + \\
 & 2 e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_2 x_3 y_3^2 \gamma_{22} \gamma_{23} \gamma_{31}^2 + \\
 & e^{\frac{\gamma(h t_2 \lambda_{11} + \hbar^2 t_2^2 \gamma_{21} \lambda_{11} + \hbar t_2 \lambda_{21} + \hbar^2 t_2^2 \gamma_{21} \lambda_{21} + \hbar t_3 \lambda_{31} + \hbar^2 t_2 t_3 \gamma_{21} \lambda_{31})}{1 + \hbar t_2 \gamma_{21}}} \gamma \hbar^4 t_2 x_3^2 y_3^2 \gamma_{23}^2 \gamma_{31}^2 \Big) \epsilon + 0[\epsilon]^2, e^{(\nu_{5058} + \omega_{5058}) y_{n5058}} + 0[\epsilon]^3 \Big\}
 \end{aligned}$$

































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$$\begin{aligned}
 & \mathbb{E}_{\text{CU}} \left[ \{Y_3, a_3, X_3\}_3, \{Y_1, Y_{\$20}, a_{\$20}, a_{\$19}, X_{\$19}, a_2, X_2\}_2, \right. \\
 & \frac{1}{1 + \hbar t_2 \gamma_{21}} e^{-\gamma \hbar t_2 \lambda_{11} - \gamma \hbar t_2 \lambda_{21} - \gamma \hbar t_3 \lambda_{31}} \left( e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_{\$19} Y_1 \gamma_{11} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_2 Y_1 \gamma_{12} + \right. \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_3 Y_1 \gamma_{13} + \hbar X_{\$19} Y_{\$20} \gamma_{21} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_2 Y_1 \gamma_{12} \gamma_{21} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_3 Y_1 \gamma_{13} \gamma_{21} + \hbar X_2 Y_{\$20} \gamma_{22} - e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_2 Y_1 \gamma_{11} \gamma_{22} + \\
 & \hbar X_3 Y_{\$20} \gamma_{23} - e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_3 Y_1 \gamma_{11} \gamma_{23} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_{\$19} Y_3 \gamma_{31} - \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_2 Y_3 \gamma_{22} \gamma_{31} - e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_3 Y_3 \gamma_{23} \gamma_{31} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_2 Y_3 \gamma_{32} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_2 Y_3 \gamma_{21} \gamma_{32} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar X_3 Y_3 \gamma_{33} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 X_3 Y_3 \gamma_{21} \gamma_{33} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_{\$20} t_2 \lambda_{11} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$20} t_2^2 \gamma_{21} \lambda_{11} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_2 t_2 \lambda_{12} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_2 t_2^2 \gamma_{21} \lambda_{12} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_3 t_2 \lambda_{13} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_3 t_2^2 \gamma_{21} \lambda_{13} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_{\$20} t_2 \lambda_{21} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$20} t_2^2 \gamma_{21} \lambda_{21} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_2 t_2 \lambda_{22} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_2 t_2^2 \gamma_{21} \lambda_{22} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_3 t_2 \lambda_{23} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_3 t_2^2 \gamma_{21} \lambda_{23} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_{\$20} t_3 \lambda_{31} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$20} t_2 t_3 \gamma_{21} \lambda_{31} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_2 t_3 \lambda_{32} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_2 t_2 t_3 \gamma_{21} \lambda_{32} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar a_3 t_3 \lambda_{33} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_3 t_2 t_3 \gamma_{21} \lambda_{33} \Big), \\
 & \frac{1}{1 + \hbar t_2 \gamma_{21}} + \frac{1}{2(1 + \hbar t_2 \gamma_{21})} e^{-\gamma \hbar t_2 \lambda_{11} - \gamma \hbar t_2 \lambda_{21} - \gamma \hbar t_3 \lambda_{31}} \\
 & \left( 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$19} X_2 Y_1 \gamma_{11} \gamma_{22} - 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_2 X_{\$19} Y_1^2 \gamma_{11}^2 \gamma_{22} - \right. \\
 & 2 \gamma \hbar^3 X_2^2 Y_1 Y_{\$20} \gamma_{11} \gamma_{22}^2 + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2^2 Y_1^2 \gamma_{11}^2 \gamma_{22}^2 + \\
 & 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$19} X_3 Y_1 \gamma_{11} \gamma_{23} - 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_3 X_{\$19} Y_1^2 \gamma_{11}^2 \gamma_{23} - \\
 & 4 \gamma \hbar^3 X_2 X_3 Y_1 Y_{\$20} \gamma_{11} \gamma_{22} \gamma_{23} + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2 X_3 Y_1^2 \gamma_{11}^2 \gamma_{22} \gamma_{23} - \\
 & 2 \gamma \hbar^3 X_3^2 Y_1 Y_{\$20} \gamma_{11} \gamma_{23}^2 + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_3^2 Y_1^2 \gamma_{11}^2 \gamma_{23}^2 + \\
 & 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$19} X_2 Y_3 \gamma_{22} \gamma_{31} - 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_2 X_{\$19} Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{31} - \\
 & 2 \gamma \hbar^3 X_2^2 Y_3 Y_{\$20} \gamma_{22}^2 \gamma_{31} + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2^2 Y_1 Y_3 \gamma_{11} \gamma_{22}^2 \gamma_{31} + \\
 & 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 a_{\$19} X_3 Y_3 \gamma_{23} \gamma_{31} - 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_3 X_{\$19} Y_1 Y_3 \gamma_{11} \gamma_{23} \gamma_{31} - \\
 & 4 \gamma \hbar^3 X_2 X_3 Y_3 Y_{\$20} \gamma_{22} \gamma_{23} \gamma_{31} + 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2 X_3 Y_1 Y_3 \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} - \\
 & 2 \gamma \hbar^3 X_3^2 Y_3 Y_{\$20} \gamma_{23}^2 \gamma_{31} + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_3^2 Y_1 Y_3 \gamma_{11} \gamma_{23}^2 \gamma_{31} - \\
 & 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_2 X_{\$19} Y_3^2 \gamma_{22} \gamma_{31}^2 + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2^2 Y_3^2 \gamma_{22}^2 \gamma_{31}^2 - \\
 & 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 X_3 X_{\$19} Y_3^2 \gamma_{23} \gamma_{31}^2 + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_2 X_3 Y_3^2 \gamma_{22} \gamma_{23} \gamma_{31}^2 + \\
 & \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^4 t_2 X_3^2 Y_3^2 \gamma_{23}^2 \gamma_{31}^2 \right) \epsilon + O[\epsilon]^2 ]
 \end{aligned}$$















$$\begin{aligned}
 & Y_{\$21} \gamma_{11} \gamma_{22}^2 \gamma_{31} + 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar^2 a_{\$24} x_3 y_3 \gamma_{23} \gamma_{31} - \\
 & 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 x_3 x_{\$25} y_3 y_{\$21} \gamma_{11} \gamma_{23} \gamma_{31} - 4 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \\
 & \gamma \hbar^3 x_3 x_{\$25} y_3 y_{\$21} \gamma_{22} \gamma_{23} \gamma_{31} + 4 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \\
 & \hbar^4 t_2 x_3 x_{\$25} y_3 y_{\$21} \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} - 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \hbar^3 x_3^2 y_3 y_{\$21} \gamma_{23}^2 \gamma_{31} + \\
 & 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \hbar^4 t_2 x_3^2 y_3 y_{\$21} \gamma_{11} \gamma_{23}^2 \gamma_{31} - \\
 & 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 x_{\$25}^2 y_3^2 \gamma_{22} \gamma_{31}^2 + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \\
 & \gamma \hbar^4 t_2 x_{\$25}^2 y_3^2 \gamma_{22}^2 \gamma_{31}^2 - 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \hbar^3 x_3 x_{\$25} y_3^2 \gamma_{23} \gamma_{31}^2 + \\
 & 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \hbar^4 t_2 x_3 x_{\$25} y_3^2 \gamma_{22} \gamma_{23} \gamma_{31}^2 + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \hbar^4 t_2 x_3^2 y_3^2 \gamma_{23}^2 \gamma_{31}^2 \in + 0[\epsilon]^2, -2];
 \end{aligned}$$

Expand@Collect[Q, {x\_, y\_, a\_}, CC] /. CC -> ExpandDenominator@\*ExpandNumerator@\*Together

$$\begin{aligned}
 & (x_{\$25} y_{\$21} (e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar \gamma_{11} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar \gamma_{12} + \\
 & \hbar \gamma_{21} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar^2 t_2 \gamma_{12} \gamma_{21} + \\
 & e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar \gamma_{22} - e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar^2 t_2 \gamma_{11} \gamma_{22})) / \\
 & (e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} + \\
 & e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21}) + \\
 & (x_3 y_{\$21} (e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar \gamma_{13} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 \gamma_{13} \gamma_{21} + \\
 & \hbar \gamma_{23} - e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar^2 t_2 \gamma_{11} \gamma_{23})) / \\
 & (e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar t_2 \gamma_{21}) + \\
 & (x_{\$25} y_3 (\hbar \gamma_{31} - e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar^2 t_2 \gamma_{22} \gamma_{31} + \\
 & e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar \gamma_{32} + e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar^2 t_2 \gamma_{21} \gamma_{32})) / \\
 & (e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} + e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21}) + \\
 & x_3 y_3 (-\hbar^2 t_2 \gamma_{23} \gamma_{31} + \hbar \gamma_{33} + \hbar^2 t_2 \gamma_{21} \gamma_{33})) + \\
 & 1 + \hbar t_2 \gamma_{21} \\
 & a_{\$24} (\hbar t_2 \lambda_{11} + \hbar t_2 \lambda_{12} + \hbar t_2 \lambda_{21} + \hbar t_2 \lambda_{22} + \hbar t_3 \lambda_{31} + \hbar t_3 \lambda_{32}) + \\
 & a_3 (\hbar t_2 \lambda_{13} + \hbar t_2 \lambda_{23} + \hbar t_3 \lambda_{33})
 \end{aligned}$$

Expand@Collect[Normal@P, {x\_, y\_, a\_}, CC] /.

CC → ExpandDenominator@\*ExpandNumerator@\*Together

$$\begin{aligned}
& \frac{1}{1 + \hbar t_2 \gamma_{21}} + \frac{2 \in \hbar^2 a_{\$24} X_{\$25} Y_{\$21} \gamma_{11} \gamma_{22}}{1 + \hbar t_2 \gamma_{21}} + \\
& \left( X_{\$25}^2 Y_{\$21}^2 \left( -2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^3 \gamma_{11}^2 \gamma_{22} - 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^3 \gamma_{11} \gamma_{22}^2 + \right. \right. \\
& \left. \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{11}^2 \gamma_{22}^2 \right) \right) / \\
& \left( 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right) + \frac{2 \in \hbar^2 a_{\$24} x_3 y_{\$21} \gamma_{11} \gamma_{23}}{1 + \hbar t_2 \gamma_{21}} + \\
& \left( x_3 X_{\$25} Y_{\$21}^2 \left( -e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^3 \gamma_{11}^2 \gamma_{23} - 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^3 \gamma_{11} \gamma_{22} \gamma_{23} + \right. \right. \\
& \left. \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{11}^2 \gamma_{22} \gamma_{23} \right) \right) / \\
& \left( e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} + \right. \\
& \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right) + \\
& \left( x_3^2 Y_{\$21}^2 \left( -2 \gamma \in \hbar^3 \gamma_{11} \gamma_{23}^2 + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^4 t_2 \gamma_{11}^2 \gamma_{23}^2 \right) \right) / \\
& \left( 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar t_2 \gamma_{21} \right) + \\
& \frac{2 \in \hbar^2 a_{\$24} X_{\$25} Y_3 \gamma_{22} \gamma_{31}}{1 + \hbar t_2 \gamma_{21}} + \frac{2 \in \hbar^2 a_{\$24} x_3 y_3 \gamma_{23} \gamma_{31}}{1 + \hbar t_2 \gamma_{21}} + \\
& \frac{\gamma \in \hbar^4 t_2 x_3^2 y_3^2 \gamma_{23}^2 \gamma_{31}^2}{2 + 2 \hbar t_2 \gamma_{21}} + \\
& \left( X_{\$25}^2 Y_3 Y_{\$21} \left( -2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^3 \gamma_{11} \gamma_{22} \gamma_{31} - e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^3 \gamma_{22}^2 \gamma_{31} + \right. \right. \\
& \left. \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{11} \gamma_{22}^2 \gamma_{31} \right) \right) / \\
& \left( e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} + \right. \\
& \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right) + \\
& \left( x_3 X_{\$25} Y_3 Y_{\$21} \left( -2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^3 \gamma_{11} \gamma_{23} \gamma_{31} - 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^3 \right. \right. \\
& \left. \left. \gamma_{22} \gamma_{23} \gamma_{31} + 2 e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{11} \gamma_{22} \gamma_{23} \gamma_{31} \right) \right) / \\
& \left( e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} + \right. \\
& \left. e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{31} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right) + \\
& \left( x_3^2 Y_3 Y_{\$21} \left( -\gamma \in \hbar^3 \gamma_{23}^2 \gamma_{31} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \gamma \in \hbar^4 t_2 \gamma_{11} \gamma_{23}^2 \gamma_{31} \right) \right) / \\
& \left( e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} + e^{\gamma \hbar t_2 \lambda_{11} + \gamma \hbar t_2 \lambda_{21} + \gamma \hbar t_3 \lambda_{31}} \hbar t_2 \gamma_{21} \right) + \\
& \left( X_{\$25}^2 Y_3^2 \left( -2 \gamma \in \hbar^3 \gamma_{22} \gamma_{31}^2 + e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{22}^2 \gamma_{31}^2 \right) \right) / \\
& \left( 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} + 2 e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right) + \\
& \left( x_3 X_{\$25} Y_3^2 \left( -\gamma \in \hbar^3 \gamma_{23} \gamma_{31}^2 + e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \gamma \in \hbar^4 t_2 \gamma_{22} \gamma_{23} \gamma_{31}^2 \right) \right) / \\
& \left( e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} + e^{\gamma \hbar t_2 \lambda_{12} + \gamma \hbar t_2 \lambda_{22} + \gamma \hbar t_3 \lambda_{32}} \hbar t_2 \gamma_{21} \right)
\end{aligned}$$