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DeclareAlgebra[U_Symbol, opts_Rule] :=
Module[{gp, sr, cp, CE, pow,
  gs = Generators /. {opts}, cs = Centralis /. {opts}},
  (#u = U@#) & /@ gs;
gp = Alternatives @@ gs; gp = gp | gp_;
(* gen's pattern *)
sr = Thread[gs → Range@Length@gs]; (* sorting rule *)
cp = Alternatives @@ cs; (* cent's pattern *)
CE[ε_] := Collect[ε, _U,
  (Expand[#] /.  $\hbar^d$  /; d > $TnD => 0) &];
U_i_[ε_] :=
  ε /. {t : cp => t_i, u_U => Replace[u, x_ => x_i, 1]};
U_i_[NCM[]] := U[];
B[U@(x_)_i, U@(y_)_i] :=
  B[U@x_i, U@y_i] = U_i@B[U@x, U@y];
B[U@(x_)_i, U@(y_)_j] /; i != j := 0;
B[U@y_, U@x_] := CE[-B[U@x, U@y]];
x_ ** U[] := x; U[] ** x_ := x;
(a_.*x_U) ** (b_.*y_U) :=
  If[ab == 0, 0, CE[ab(x**y)]];
U[xx___, x_] ** U[y_, yy___] :=
  If[OrderedQ[{x, y} /. sr], U[xx, x, y, yy],
    U@xx ** (U@y ** U@x + B[U@x, U@y]) ** U@yy];
U[{c_. * (L : gp)^n_, r___} /; FreeQ[c, gp] :=
  CE[c U@Table[L, {n}] ** U@{r}];
U[{c_. * L : gp, r___} := CE[c U[L] ** U@{r}];
U[{c_, r___} /; FreeQ[c, gp] := CE[c U@{r}];
U@{} = U[];
U@{L_Plus, r___} := CE[U@{#, r} & /@ L];
U@{L_, r___} := U@{Expand[L], r};
U[ε_NonCommutativeMultiply] := U /@ ε;
O_U[poly_, specs___] := Module[{sp, null, vs, us},
  sp = Replace[{specs}, L_List => L_null, {1}];
  vs = Join@@(First /@ sp);
  us = Join@@(sp /. L_s_ => (L /. x_i_ => x_s));
  CE[Total[
    CoefficientRules[poly, vs] /. (p_ → c_) => c U@(us^p)
  ]] /. x_null => x
];
pow[ε_, 0] = U[]; pow[ε_, n_] := pow[ε, n - 1] ** ε;
S_U[ε_, ss___Rule] := CE@Total[
  CoefficientRules[ε, First /@ {ss}] /.
    (p_ → c_) =>
      c NCM@@ MapThread[pow, {Last /@ {ss}, p}]];
S_i_[c_. * u_U] :=
  CE[(c /. S_i[U, Centralis])
  DeleteCases[u, _i] **
  U_i[NCM@@ Reverse@Cases[u, x_i_ => S@U@x]]];
]

```