

Pensieve header: Computing the Log of the Kink.

Startup

```
Date[]
SetDirectory["C:\\drorbn\\AcademicPensieve\\Projects\\FullDoPeGDO"];
Once[<< KnotTheory`];
Once[Get@"..\\Profile\\Profile.m"];
BeginProfile[];
$k = 1;
<< Engine.m
<< Objects.m
<< KT.m
HL[ε_] := Style[ε, Background -> If[TrueQ@ε, Green, Red]]];
```

Out[*]= {2021, 8, 20, 19, 22, 15.0584421}

Loading KnotTheory` version of February 2, 2020, 10:53:45.2097.

Read more at <http://katlas.org/wiki/KnotTheory>.

This is Profile.m of <http://www.drorbn.net/AcademicPensieve/Projects/Profile/>.

This version: April 2020. Original version: July 1994.

Log[Kink]

In[*]= **R_{1,2}**

$$\text{Out[*]} = \mathbb{E}_{\{i\} \rightarrow \{1,2\}} \left[\hbar a_i b_i + \hbar x_i y_i, -\frac{1}{4} \hbar^3 x_i^2 y_i^2 \right]$$

In[*]= **dm_{1,2→3}**

$$\text{Out[*]} = \mathbb{E}_{\{1,2\} \rightarrow \{3\}} \left[a_3 (\alpha_1 + \alpha_2) + b_3 \beta_1 + b_3 \beta_2 + y_3 \eta_1 + \frac{y_3 \eta_2}{\mathcal{A}_1} + \frac{x_3 \xi_1}{\mathcal{A}_2} - \frac{(-1 + B_3) \eta_2 \xi_1}{\hbar} + x_3 \xi_2, \right. \\ \left. -\frac{y_3 \beta_1 \eta_2}{\mathcal{A}_1} - \frac{x_3 \beta_2 \xi_1}{\mathcal{A}_2} + a_3 B_3 \eta_2 \xi_1 + \frac{\hbar x_3 y_3 \eta_2 \xi_1}{\mathcal{A}_1 \mathcal{A}_2} - \frac{(-1 + 3 B_3) y_3 \eta_2^2 \xi_1}{2 \mathcal{A}_1} - \frac{(-1 + 3 B_3) x_3 \eta_2 \xi_1^2}{2 \mathcal{A}_2} + \frac{(-1 + B_3) \times (-1 + 3 B_3) \eta_2^2 \xi_1^2}{4 \hbar} \right]$$

In[*]= **Kink_i**

$$\text{Out[*]} = \mathbb{E}_{\{i\} \rightarrow \{i\}} \left[\frac{\hbar b_i}{2} + \hbar a_i b_i + \hbar x_i y_i, \frac{\hbar a_i}{2} - \frac{1}{4} \hbar^3 x_i^2 y_i^2 \right]$$

In[*]= **Block** [{\$k = 0}, **Log_{dm}**[Kink_i]]

Solve: Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information.

$$\text{Out[*]} = \mathbb{U}_{\{i\} \rightarrow \{i\}} \left[\frac{\hbar b_i}{2} + \hbar a_i b_i - \frac{\hbar^2 b_i x_i y_i}{-1 + B_i} \right]$$

In[*]:= **Timing@Block** [{**\$k = 1**}, **Log_{dm}**[**Kink_i**]]

Solve: Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information.

$$\text{Out[*]} = \left\{ 12.7188, \mathbb{U}_{\{\} \rightarrow \{i\}} \left[\frac{\hbar b_i}{2} + \hbar a_i b_i - \frac{\hbar^2 b_i x_i y_i}{-1 + B_i}, \right. \right. \\ \left. \left. \frac{\hbar a_i}{2} - \frac{\hbar^2 a_i (-1 + B_i + \hbar b_i B_i) x_i y_i}{(-1 + B_i)^2} + \frac{\hbar^3 (-2 + \hbar b_i + 2 B_i + \hbar b_i B_i) x_i^2 y_i^2}{2 (-1 + B_i)^3} \right] \right\}$$

In[*]:= **Timing@Block** [{**\$k = 2**}, **Log_{dm}**[**Kink_i**]]

Solve: Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information.

$$\text{Out[*]} = \left\{ 815.594, \mathbb{U}_{\{\} \rightarrow \{i\}} \left[\frac{\hbar b_i}{2} + \hbar a_i b_i - \frac{\hbar^2 b_i x_i y_i}{-1 + B_i}, \right. \right. \\ \left. \left. \frac{\hbar a_i}{2} - \frac{\hbar^2 a_i (-1 + B_i + \hbar b_i B_i) x_i y_i}{(-1 + B_i)^2} + \frac{\hbar^3 (-2 + \hbar b_i + 2 B_i + \hbar b_i B_i) x_i^2 y_i^2}{2 (-1 + B_i)^3}, \right. \right. \\ \left. \left. - \frac{\hbar^3 a_i^2 B_i (-2 + \hbar b_i + 2 B_i + \hbar b_i B_i) x_i y_i}{2 (-1 + B_i)^3} - \frac{\hbar^4 (-1 - 4 B_i + 4 \hbar b_i B_i + 5 B_i^2 + 2 \hbar b_i B_i^2) x_i^2 y_i^2}{2 (-1 + B_i)^4} + \right. \right. \\ \left. \left. \frac{\hbar^4 a_i (-1 - 4 B_i + 4 \hbar b_i B_i + 5 B_i^2 + 2 \hbar b_i B_i^2) x_i^2 y_i^2}{2 (-1 + B_i)^4} - \frac{\hbar^5 (-3 + \hbar b_i + 4 \hbar b_i B_i + 3 B_i^2 + \hbar b_i B_i^2) x_i^3 y_i^3}{3 (-1 + B_i)^5} \right] \right\}$$

In[*]:= **Timing@Block**[{**\$k = 3**}, **Log_{dm}**[**Kink_i**]]

Solve: Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information.

$$\text{Out[*]} = \left\{ 38376.3, \mathbb{U}_{\{i\} \rightarrow \{i\}} \left[\frac{\hbar b_i}{2} + \hbar a_i b_i - \frac{\hbar^2 b_i x_i y_i}{-1 + B_i}, \right. \right. \\
 \frac{\hbar a_i}{2} - \frac{\hbar^2 a_i (-1 + B_i + \hbar b_i B_i) x_i y_i}{(-1 + B_i)^2} + \frac{\hbar^3 (-2 + \hbar b_i + 2 B_i + \hbar b_i B_i) x_i^2 y_i^2}{2 (-1 + B_i)^3}, \\
 - \frac{\hbar^3 a_i^2 B_i (-2 + \hbar b_i + 2 B_i + \hbar b_i B_i) x_i y_i}{2 (-1 + B_i)^3} - \frac{\hbar^4 (-1 - 4 B_i + 4 \hbar b_i B_i + 5 B_i^2 + 2 \hbar b_i B_i^2) x_i^2 y_i^2}{2 (-1 + B_i)^4} + \\
 \frac{\hbar^4 a_i (-1 - 4 B_i + 4 \hbar b_i B_i + 5 B_i^2 + 2 \hbar b_i B_i^2) x_i^2 y_i^2}{2 (-1 + B_i)^4} - \frac{\hbar^5 (-3 + \hbar b_i + 4 \hbar b_i B_i + 3 B_i^2 + \hbar b_i B_i^2) x_i^3 y_i^3}{3 (-1 + B_i)^5}, \\
 - \frac{\hbar^4 a_i^3 B_i (-3 + \hbar b_i + 4 \hbar b_i B_i + 3 B_i^2 + \hbar b_i B_i^2) x_i y_i}{6 (-1 + B_i)^4} - \\
 \frac{2 \hbar^5 a_i B_i (-3 + \hbar b_i + 4 \hbar b_i B_i + 3 B_i^2 + \hbar b_i B_i^2) x_i^2 y_i^2}{(-1 + B_i)^5} + \\
 \frac{\hbar^5 a_i^2 B_i (-3 + \hbar b_i + 4 \hbar b_i B_i + 3 B_i^2 + \hbar b_i B_i^2) x_i^2 y_i^2}{(-1 + B_i)^5} + \\
 \frac{\hbar^5 (-\hbar b_i - 96 B_i + 37 \hbar b_i B_i + 24 B_i^2 + 109 \hbar b_i B_i^2 + 72 B_i^3 + 23 \hbar b_i B_i^3) x_i^2 y_i^2}{24 (-1 + B_i)^5} + \\
 \frac{2 \hbar^6 (-1 - 18 B_i + 9 \hbar b_i B_i + 9 B_i^2 + 18 \hbar b_i B_i^2 + 10 B_i^3 + 3 \hbar b_i B_i^3) x_i^3 y_i^3}{3 (-1 + B_i)^6} - \\
 \frac{\hbar^6 a_i (-1 - 18 B_i + 9 \hbar b_i B_i + 9 B_i^2 + 18 \hbar b_i B_i^2 + 10 B_i^3 + 3 \hbar b_i B_i^3) x_i^3 y_i^3}{3 (-1 + B_i)^6} + \\
 \left. \left. \frac{\hbar^7 (-11 + 3 \hbar b_i - 27 B_i + 27 \hbar b_i B_i + 27 B_i^2 + 27 \hbar b_i B_i^2 + 11 B_i^3 + 3 \hbar b_i B_i^3) x_i^4 y_i^4}{12 (-1 + B_i)^7} \right] \right\}$$