

```

SetDirectory["C:/drorbn/AcademicPensieve/Projects/Arrow_Diagrams_and_g1(N)"];
<< "Arrow_Diagrams_and_g1(N).m"

diag = Diag[ar[1, 3], ar[4, 2]]
Diag[ar[1, 3], ar[4, 2]]

t1 = List @@ Expand[(Times @@ diag) /. ar[p_, q_] :>
    LTAt[p, q] + 1/2 (EQAt[p, q] - CAt[p] + CAt[q] - CAt[])
]
{
$$\begin{aligned} & \frac{\text{CAt}[]^2}{4}, \frac{1}{4} \text{CAt}[] \text{CAt}[1], -\frac{1}{4} \text{CAt}[] \text{CAt}[2], -\frac{1}{4} \text{CAt}[1] \text{CAt}[2], -\frac{1}{4} \text{CAt}[] \text{CAt}[3], \\ & \frac{1}{4} \text{CAt}[2] \text{CAt}[3], \frac{1}{4} \text{CAt}[] \text{CAt}[4], \frac{1}{4} \text{CAt}[1] \text{CAt}[4], -\frac{1}{4} \text{CAt}[3] \text{CAt}[4], \\ & -\frac{1}{4} \text{CAt}[] \text{EQAt}[1, 3], \frac{1}{4} \text{CAt}[2] \text{EQAt}[1, 3], -\frac{1}{4} \text{CAt}[4] \text{EQAt}[1, 3], -\frac{1}{4} \text{CAt}[] \text{EQAt}[4, 2], \\ & -\frac{1}{4} \text{CAt}[1] \text{EQAt}[4, 2], \frac{1}{4} \text{CAt}[3] \text{EQAt}[4, 2], \frac{1}{4} \text{EQAt}[1, 3] \text{EQAt}[4, 2], -\frac{1}{2} \text{CAt}[] \text{LTAt}[1, 3], \\ & \frac{1}{2} \text{CAt}[2] \text{LTAt}[1, 3], -\frac{1}{2} \text{CAt}[4] \text{LTAt}[1, 3], \frac{1}{2} \text{EQAt}[4, 2] \text{LTAt}[1, 3], -\frac{1}{2} \text{CAt}[] \text{LTAt}[4, 2], \\ & -\frac{1}{2} \text{CAt}[1] \text{LTAt}[4, 2], \frac{1}{2} \text{CAt}[3] \text{LTAt}[4, 2], \frac{1}{2} \text{EQAt}[1, 3] \text{LTAt}[4, 2], \text{LTAt}[1, 3] \text{LTAt}[4, 2] \end{aligned}\}$$

dirss = - $\frac{1}{4} \text{CAt}[4] \text{EQAt}[1, 3]$ 

$$-\frac{1}{4} \text{CAt}[4] \text{EQAt}[1, 3]$$


coeff = dirss /. (_CAt | _EQAt | _LTAt)  $\rightarrow$  1;
k = 0;
w = Table[1, {2 Length[diag]}];
ltpairs = {};
dirs /. {
    LTAt[p_, q_] :> (
        w[[p]] = e[i = ++k, j = ++k];
        w[[q]] = e[j, i];
        AppendTo[ltpairs, {i, j}];
    ),
    EQAt[p_, q_] :> (w[[p]] = w[[q]] = e[i = ++k, i];),
    CAt[p_] :> (
        w[[p]] = e[i = ++k, i];
        coeff *= h[i];
    ),
    CAt[] :> (coeff *= h[++k]^2)
};
w = DeleteCases[w, 1];
{coeff, k, ltpairs, w}

{- $\frac{h[1]}{4}, 2, \{\}, \{e[2, 2], e[2, 2], e[1, 1]\}\}$ 
```

```
OrderTypes[k, ltpairs]
{{2, 1}, {1, 1}, {1, 2}}

ot = {2, 1}
{2, 1}

coeff /. h[i_] :> h[ot[[i]]]
- h[2]
4

w@@w /. e[i_, j_] :> alpha[ot[[i]], ot[[j]]]
w[101, 101, 202]
```

```

combfact = Binomial[n, Max[ot]]


$$\frac{1}{2} (-1 + n) n$$


Clear[UGLnBiAlg];
UGLnBiAlg[diag_Diag] := UGLnBiAlg[diag] = Module[
  {allterms, s, LTAt, EQAt, CAT, m1, m2, dirs, coeff, k, ltpairs, w, allots},
  allterms = List @@ Expand[(Times @@ diag) /. ar[p_, q_] :>
    LTAt[p, q] + 1/2 (EQAt[p, q] - CAT[p] + CAT[q] - CAT[])]
  ];
s = Sum[
  dirs = allterms[[m1]];
  coeff = dirs /. (_CAT | _EQAt | _LTAt) :> 1;
  k = 0;
  w = Table[1, {2 Length[diag]}];
  ltpairs = {};
  dirs /. {
    LTAt[p_, q_] :> (
      w[[p]] = e[i = ++k, j = ++k];
      w[[q]] = e[j, i];
      AppendTo[ltpairs, {i, j}];
    ),
    EQAt[p_, q_] :> (w[[p]] = w[[q]] = e[i = ++k, i]),
    CAT[p_] :> (
      w[[p]] = e[i = ++k, i];
      coeff *= h[i];
    ),
    CAT[] :> (coeff *= h[++k]^2);
  };
  w = DeleteCases[w, 1];
  allots = OrderTypes[k, ltpairs];
  Sum[
    ot = allots[[m2]];
    Times[
      (* Binomial[n, Max[ot]], *)
      n^Max[ot],
      coeff /. h[i_] :> h[ot[[i]]],
      W @@ w /. e[i_, j_] :> alpha[ot[[i]], ot[[j]]]
    ],
    {m2, Length[allots]}
  ], {m1, Length[allterms]}
];
CanonicalForm[Expand[s]]
];
UGLnBiAlg[expr_] := Expand[expr /. diag_Diag :> UGLnBiAlg[diag]];

diag
Diag[ar[1, 3], ar[4, 2]]

```

**UGLnBiAlg[diag]**

$$\begin{aligned}
& \frac{1}{4} n h[1]^2 RW[] - \frac{1}{2} n^2 h[1] RW[101] + \frac{1}{2} n^2 h[1]^2 RW[101] + \frac{1}{2} n^2 h[2] RW[101] + \\
& \frac{1}{2} n^2 h[2]^2 RW[101] + \frac{1}{2} n^3 h[2]^2 RW[101] + \frac{1}{2} n^3 h[3]^2 RW[101] + \frac{1}{2} n^2 h[1] RW[202] - \\
& \frac{1}{2} n^2 h[1]^2 RW[202] + \frac{1}{2} n^3 h[1]^2 RW[202] - \frac{1}{2} n^2 h[2] RW[202] - \frac{1}{2} n^2 h[2]^2 RW[202] - \\
& \frac{1}{2} n^3 h[3]^2 RW[202] - \frac{1}{2} n^3 h[1]^2 RW[303] - \frac{1}{2} n^3 h[2]^2 RW[303] - \frac{1}{2} n^2 RW[101, 101] - \\
& \frac{1}{2} n h[1]^2 RW[101, 101] - \frac{1}{2} n^2 h[2]^2 RW[101, 101] + n^2 RW[101, 202] + 2 n^2 RW[102, 201] - \\
& n^3 RW[102, 201] - n^2 h[1]^2 RW[102, 201] - n^2 h[2]^2 RW[102, 201] - n^3 h[3]^2 RW[102, 201] + \\
& 2 n^3 RW[103, 301] - n^3 h[2]^2 RW[103, 301] - \frac{1}{2} n^2 RW[202, 202] - \frac{1}{2} n^2 h[1]^2 RW[202, 202] - \\
& n^3 RW[203, 302] - n^3 h[1]^2 RW[203, 302] - \frac{1}{2} n^2 RW[101, 101, 101] + \frac{1}{2} n^2 RW[101, 101, 202] - \\
& \frac{1}{2} n^3 RW[101, 101, 202] + \frac{1}{2} n^3 RW[101, 101, 303] - 2 n^2 RW[101, 102, 201] - \\
& n^3 RW[101, 102, 201] - n^3 RW[101, 103, 301] - \frac{1}{2} n^2 RW[101, 202, 202] - \frac{1}{2} n^3 RW[101, 202, 202] - \\
& 2 n^3 RW[101, 203, 302] - n^4 RW[101, 203, 302] - n^4 RW[101, 204, 402] - \frac{1}{2} n^3 RW[101, 303, 303] - \\
& n^4 RW[101, 304, 403] + 2 n^2 RW[102, 201, 202] - n^3 RW[102, 201, 202] + 2 n^3 RW[102, 201, 303] - \\
& n^4 RW[102, 201, 303] + n^4 RW[102, 201, 404] + n^3 RW[102, 203, 301] - n^3 RW[103, 201, 302] - \\
& n^4 RW[103, 202, 301] + n^3 RW[103, 301, 303] + n^4 RW[103, 301, 404] - n^4 RW[104, 202, 401] + \\
& n^4 RW[104, 303, 401] + \frac{1}{2} n^2 RW[202, 202, 202] + \frac{1}{2} n^3 RW[202, 202, 303] + n^3 RW[202, 203, 302] + \\
& \frac{1}{2} n^3 RW[202, 303, 303] + n^4 RW[202, 304, 403] + n^3 RW[203, 302, 303] + n^4 RW[203, 302, 404] + \\
& n^4 RW[204, 303, 402] + \frac{1}{4} n RW[101, 101, 101, 101] + n^2 RW[101, 101, 102, 201] + \\
& \frac{1}{2} n^2 RW[101, 101, 202, 202] + n^3 RW[101, 101, 203, 302] + n^2 RW[102, 102, 201, 201] + \\
& 2 n^3 RW[102, 103, 201, 301] + n^2 RW[102, 201, 202, 202] + 2 n^3 RW[102, 201, 203, 302] + \\
& n^3 RW[102, 201, 303, 303] + 2 n^4 RW[102, 201, 304, 403] + n^3 RW[103, 202, 202, 301] + \\
& 2 n^3 RW[103, 203, 301, 302] + 2 n^4 RW[103, 204, 301, 402] + 2 n^4 RW[104, 203, 302, 401]
\end{aligned}$$

**rels = R /@ Diagrams[R6T]**

$$\begin{aligned}
& \{ \text{Diag}[ar[1, 2], ar[3, 4]] + \text{Diag}[ar[1, 3], ar[2, 4]] - 2 \text{Diag}[ar[1, 4], ar[2, 3]], \\
& \text{Diag}[ar[1, 2], ar[4, 3]] - \text{Diag}[ar[1, 3], ar[2, 4]] + \\
& \text{Diag}[ar[1, 4], ar[2, 3]] - \text{Diag}[ar[1, 4], ar[3, 2]], -\text{Diag}[ar[1, 3], ar[2, 4]] + \\
& \text{Diag}[ar[1, 4], ar[2, 3]] - \text{Diag}[ar[1, 4], ar[3, 2]] + \text{Diag}[ar[2, 1], ar[3, 4]], \\
& -\text{Diag}[ar[2, 1], ar[3, 4]] + \text{Diag}[ar[2, 3], ar[4, 1]] + \text{Diag}[ar[3, 1], ar[4, 2]] - \\
& \text{Diag}[ar[3, 2], ar[4, 1]], -\text{Diag}[ar[1, 2], ar[4, 3]] + \\
& \text{Diag}[ar[2, 3], ar[4, 1]] + \text{Diag}[ar[3, 1], ar[4, 2]] - \text{Diag}[ar[3, 2], ar[4, 1]], \\
& -\text{Diag}[ar[2, 1], ar[4, 3]] - \text{Diag}[ar[3, 1], ar[4, 2]] + 2 \text{Diag}[ar[3, 2], ar[4, 1]] \}
\end{aligned}$$

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UGLnBiAlg[rels]
{0, 0, 0, 0, 0, 0}

Print[# → Short[UGLnBiAlg[#], 3]] & /@ Diagrams[3 ar]

Diag[ar[1, 2], ar[3, 4], ar[5, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
 $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <>605>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[3, 4], ar[6, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1849>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[4, 3], ar[5, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1849>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[4, 3], ar[6, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
 $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <>2325>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[3, 5], ar[4, 6]] →
 $-\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] + <>601>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[3, 5], ar[6, 4]] →
 $-\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] + <>2091>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[4, 6], ar[5, 3]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <>2092>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[1, 2], ar[5, 3], ar[6, 4]] → <>2388>> + 6 n6 RW[<>1] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[3, 6], ar[4, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
   $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <>604>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[3, 6], ar[5, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
   $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1849>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[4, 5], ar[6, 3]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{1}{4}$  n2 h[1]2 RW[101] +  $\frac{1}{2}$  n3 h[1]2 RW[101] +
   $\frac{1}{4}$  n2 h[2]2 RW[101] +  $\frac{3}{4}$  n3 h[2]2 RW[101] + <>1919>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 2], ar[5, 4], ar[6, 3]] → <>2401>> + 6 n6 RW[<>1] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 1], ar[3, 4], ar[5, 6]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
   $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1849>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 1], ar[3, 4], ar[6, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
   $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <>2325>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 1], ar[4, 3], ar[5, 6]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
   $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <>2325>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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$$\text{Diag}[\text{ar}[2, 1], \text{ar}[4, 3], \text{ar}[6, 5]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{3}{4} n^2 h[1]^2 \text{RW}[101] - \frac{3}{4} n^2 h[2]^2 \text{RW}[101] -$$

$$\frac{3}{4} n^3 h[2]^2 \text{RW}[101] - \frac{3}{4} n^3 h[3]^2 \text{RW}[101] + <>2450> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[3, 5], \text{ar}[4, 6]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{4} n^2 h[1]^2 \text{RW}[101] - \frac{1}{4} n^2 h[2]^2 \text{RW}[101] -$$

$$\frac{1}{4} n^3 h[2]^2 \text{RW}[101] - \frac{1}{4} n^3 h[3]^2 \text{RW}[101] + <>1832> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[3, 5], \text{ar}[6, 4]] \rightarrow$$

$$-\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{2} n^2 h[1]^2 \text{RW}[101] + <>2625> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[4, 6], \text{ar}[5, 3]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{2} n^2 h[1]^2 \text{RW}[101] -$$

$$\frac{1}{4} n^2 h[1]^3 \text{RW}[101] + <>2626> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[5, 3], \text{ar}[6, 4]] \rightarrow$$

$$<>2523> + 6 <>1> \text{RW}[<>1>] + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[3, 6], \text{ar}[4, 5]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{4} n^2 h[1]^2 \text{RW}[101] - \frac{1}{4} n^2 h[2]^2 \text{RW}[101] -$$

$$\frac{1}{4} n^3 h[2]^2 \text{RW}[101] - \frac{1}{4} n^3 h[3]^2 \text{RW}[101] + <>1815> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[3, 6], \text{ar}[5, 4]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{2} n^2 h[1]^2 \text{RW}[101] - \frac{1}{2} n^2 h[2]^2 \text{RW}[101] -$$

$$\frac{1}{2} n^3 h[2]^2 \text{RW}[101] - \frac{1}{2} n^3 h[3]^2 \text{RW}[101] + <>2328> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 1], \text{ar}[4, 5], \text{ar}[6, 3]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + \frac{1}{2} n^3 h[1]^2 \text{RW}[101] + \frac{1}{2} n^3 h[2]^2 \text{RW}[101] +$$

$$\frac{1}{2} n^4 h[2]^2 \text{RW}[101] + \frac{1}{2} n^3 h[3]^2 \text{RW}[101] + <>2433> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

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Diag[ar[2, 1], ar[5, 4], ar[6, 3]] → <<2536>> + <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 4], ar[5, 6]] →
  -  $\frac{1}{8} nh[1]^2 RW[] + \frac{3}{8} nh[1]^2 RW[101, 101]$  + <<601>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 4], ar[6, 5]] → -  $\frac{1}{8} nh[1]^2 RW[] - \frac{1}{4} n^2 h[1]^2 RW[101] - \frac{1}{4} n^2 h[2]^2 RW[101] -$ 
   $\frac{1}{4} n^3 h[2]^2 RW[101] - \frac{1}{4} n^3 h[3]^2 RW[101]$  + <<1832>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[4, 2], ar[5, 6]] →
  -  $\frac{1}{8} nh[1]^2 RW[] - \frac{1}{4} n^2 h[1]^2 RW[101]$  + <<2091>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[4, 2], ar[6, 5]] →
  -  $\frac{1}{8} nh[1]^2 RW[] - \frac{1}{2} n^2 h[1]^2 RW[101]$  + <<2625>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 5], ar[4, 6]] → -  $\frac{1}{8} nh[1]^2 RW[] + \frac{3}{8} nh[1]^2 RW[101, 101] + \frac{3}{8} n^2 h[2]^2 RW[101, 101] +$ 
   $\frac{1}{2} n^2 RW[102, 201] - \frac{1}{2} n^2 h[1]^2 RW[102, 201]$  + <<621>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 5], ar[6, 4]] →
  -  $\frac{1}{8} nh[1]^2 RW[] - \frac{1}{4} n^2 h[1]^2 RW[101]$  + <<2099>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[4, 6], ar[5, 2]] → -  $\frac{1}{8} nh[1]^2 RW[] - \frac{1}{2} n^2 h[1] h[2] RW[101] - \frac{1}{4} n^3 h[2]^2 RW[101] -$ 
   $\frac{1}{4} n^3 h[3]^2 RW[101] - \frac{1}{4} n^3 h[1]^2 RW[202]$  + <<1965>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[1, 3], ar[5, 2], ar[6, 4]] → - $\frac{1}{8}$  n h[1]2 RW[] + n2 h[1] RW[101] + n3 h[1] RW[101] -
 $\frac{7}{4}$  n2 h[1]2 RW[101] - n3 h[1]2 RW[101] + <>2689>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 6], ar[4, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
 $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <>576>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[2, 6], ar[5, 4]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1836>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[4, 5], ar[6, 2]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1] RW[101] -  $\frac{1}{2}$  n3 h[1] RW[101] +
 $\frac{1}{4}$  n2 h[1]2 RW[101] +  $\frac{1}{2}$  n3 h[1]2 RW[101] + <>2185>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 3], ar[5, 4], ar[6, 2]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{1}{2}$  n2 h[1] RW[101] +  $\frac{1}{2}$  n3 h[1] RW[101] -
n2 h[1]2 RW[101] -  $\frac{1}{2}$  n3 h[1]2 RW[101] + <>2665>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 4], ar[3, 1], ar[5, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <>2092>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 4], ar[3, 1], ar[6, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <>2626>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 1], ar[4, 2], ar[5, 6]] → <>2388>> + 6 n6 RW[<>1>>] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[3, 1], ar[4, 2], ar[6, 5]] →
<<2523>> + 6 <<1>> RW[<<1>>] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[3, 1], ar[4, 6]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <<2100>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[3, 1], ar[6, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
 $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <<2450>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 1], ar[4, 6], ar[5, 2]] → <<2696>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 1], ar[5, 2], ar[6, 4]] → <<2576>> + <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[3, 1], ar[4, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <<2059>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[3, 1], ar[5, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <<2638>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 1], ar[4, 5], ar[6, 2]] → -  $\frac{1}{8}$  n h[1]2 RW[] + 2 n2 RW[101] + 5 n3 RW[101] +
3 n4 RW[101] +  $\frac{1}{2}$  n2 h[1] RW[101] + <<2477>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 1], ar[5, 4], ar[6, 2]] → <<2533>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[1, 4], ar[2, 3], ar[5, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
 $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <>604> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[2, 3], ar[6, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1815> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[3, 2], ar[5, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1849> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[3, 2], ar[6, 5]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
 $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <>2328> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[2, 5], ar[3, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +  $\frac{3}{8}$  n2 h[2]2 RW[101, 101] +
n2 h[1]2 RW[102, 201] -  $\frac{1}{2}$  n2 h[1] h[2] RW[102, 201] + <>626> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[2, 5], ar[6, 3]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] +
 $\frac{1}{2}$  n2 h[1]3 RW[101] + <>2129> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 4], ar[3, 6], ar[5, 2]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1] h[2] RW[101] -  $\frac{1}{4}$  n3 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[3]2 RW[101] -  $\frac{1}{4}$  n3 h[1]2 RW[202] + <>1961> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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$$\text{Diag}[\text{ar}[1, 4], \text{ar}[5, 2], \text{ar}[6, 3]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + 2 n^2 h[1] \text{RW}[101] + 2 n^3 h[1] \text{RW}[101] -$$

$$\frac{3}{2} n^2 h[1]^2 \text{RW}[101] - n^3 h[1]^2 \text{RW}[101] + <>2679>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[1, 4], \text{ar}[2, 6], \text{ar}[3, 5]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + \frac{3}{8} n h[1]^2 \text{RW}[101, 101] + \frac{3}{8} n^2 h[2]^2 \text{RW}[101, 101] -$$

$$\frac{1}{2} n^2 h[1] \text{RW}[102, 201] + \frac{1}{2} n^2 h[1]^2 \text{RW}[102, 201] + <>630>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[1, 4], \text{ar}[2, 6], \text{ar}[5, 3]] \rightarrow$$

$$-\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{4} n^2 h[1]^2 \text{RW}[101] + <>2086>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[1, 4], \text{ar}[3, 5], \text{ar}[6, 2]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] - \frac{1}{2} n^2 h[1] \text{RW}[101] - \frac{1}{2} n^3 h[1] \text{RW}[101] +$$

$$\frac{1}{4} n^2 h[1]^2 \text{RW}[101] + \frac{1}{2} n^3 h[1]^2 \text{RW}[101] + <>2196>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[1, 4], \text{ar}[5, 3], \text{ar}[6, 2]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + \frac{3}{2} n^2 h[1] \text{RW}[101] + \frac{3}{2} n^3 h[1] \text{RW}[101] -$$

$$n^2 h[1]^2 \text{RW}[101] - \frac{1}{2} n^3 h[1]^2 \text{RW}[101] + <>2691>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 3], \text{ar}[4, 1], \text{ar}[5, 6]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + \frac{1}{4} n^2 h[1]^2 \text{RW}[101] + \frac{1}{2} n^3 h[1]^2 \text{RW}[101] +$$

$$\frac{1}{4} n^2 h[2]^2 \text{RW}[101] + \frac{3}{4} n^3 h[2]^2 \text{RW}[101] + <>1919>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[2, 3], \text{ar}[4, 1], \text{ar}[6, 5]] \rightarrow -\frac{1}{8} n h[1]^2 \text{RW}[] + \frac{1}{2} n^3 h[1]^2 \text{RW}[101] + \frac{1}{2} n^3 h[2]^2 \text{RW}[101] +$$

$$\frac{1}{2} n^4 h[2]^2 \text{RW}[101] + \frac{1}{2} n^3 h[3]^2 \text{RW}[101] + <>2433>> + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

$$\text{Diag}[\text{ar}[3, 2], \text{ar}[4, 1], \text{ar}[5, 6]] \rightarrow <>2401>> + 6 n^6 \text{RW}[<>1>>] + 6 n^5 \text{RW}[105, 205, 304, 403, 501, 502] +$$

$$6 n^6 \text{RW}[105, 206, 304, 403, 501, 602] + 6 n^6 \text{RW}[106, 203, 302, 405, 504, 601] +$$

$$6 n^6 \text{RW}[106, 204, 305, 402, 503, 601] + 6 n^6 \text{RW}[106, 205, 304, 403, 502, 601]$$

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Diag[ar[3, 2], ar[4, 1], ar[6, 5]] → <<2536>> + <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[3, 6], ar[4, 1]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -
   $\frac{1}{2}$  n2 h[1]3 RW[101] +  $\frac{1}{2}$  n2 h[1] h[2] RW[101] + <<2130>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[4, 1], ar[6, 3]] →
-  $\frac{1}{8}$  n h[1]2 RW[] + 2 n2 RW[101] + <<2472>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 6], ar[4, 1], ar[5, 2]] →
-  $\frac{1}{8}$  n h[1]2 RW[] - 2 n2 h[1] RW[101] - 2 n3 h[1] RW[101] -  $\frac{3}{2}$  n2 h[1]2 RW[101] -
  n3 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[1]3 RW[101] + <<2673>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[4, 1], ar[5, 2], ar[6, 3]] → -  $\frac{1}{8}$  n h[1]2 RW[] - 10 n2 RW[101] - 22 n3 RW[101] - 12 n4 RW[101] -
  4 n2 h[1]2 RW[101] - 3 n3 h[1]2 RW[101] + <<2569>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[3, 5], ar[4, 1]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -
   $\frac{1}{2}$  n2 h[1]3 RW[101] +  $\frac{1}{2}$  n2 h[1] h[2] RW[101] + <<2103>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[4, 1], ar[5, 3]] → <<2708>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 5], ar[4, 1], ar[6, 2]] →
-  $\frac{1}{8}$  n h[1]2 RW[] + 4 n2 RW[101] + 7 n3 RW[101] + <<2727>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[4, 1], ar[5, 3], ar[6, 2]] → -  $\frac{1}{8}$  n h[1]2 RW[] - 8 n2 RW[101] - 17 n3 RW[101] -
  9 n4 RW[101] +  $\frac{1}{2}$  n2 h[1] RW[101] + <<2589>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[1, 5], ar[2, 3], ar[4, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +  $\frac{3}{8}$  n2 h[2]2 RW[101, 101] -
 $\frac{1}{2}$  n2 h[1] RW[102, 201] -  $\frac{3}{4}$  n2 h[1]2 RW[102, 201] + <>572>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[2, 3], ar[6, 4]] →
- $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] + <>2059>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[3, 2], ar[4, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
 $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <>1837>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[3, 2], ar[6, 4]] →
- $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] + <>2637>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[2, 4], ar[3, 6]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
 $\frac{3}{8}$  n2 h[2]2 RW[101, 101] +  $\frac{1}{2}$  n2 h[1] RW[102, 201] + <>632>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[2, 4], ar[6, 3]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] +
 $\frac{1}{2}$  n2 h[1]3 RW[101] + <>2103>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[3, 6], ar[4, 2]] → - $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
 $\frac{1}{4}$  n2 h[1]3 RW[101] + <>2087>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 5], ar[4, 2], ar[6, 3]] → - $\frac{1}{8}$  n h[1]2 RW[] + n2 h[1] RW[101] + n3 h[1] RW[101] -
 $\frac{5}{4}$  n2 h[1]2 RW[101] - n3 h[1]2 RW[101] + <>2701>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[1, 5], ar[2, 6], ar[3, 4]] →

$$-\frac{1}{8} nh[1]^2 RW[] + \frac{3}{8} nh[1]^2 RW[101, 101] + <<616>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[1, 5], ar[2, 6], ar[4, 3]] →  $-\frac{1}{8} nh[1]^2 RW[] - \frac{1}{4} n^2 h[1]^2 RW[101] - \frac{1}{4} n^2 h[2]^2 RW[101] -$ 

$$\frac{1}{4} n^3 h[2]^2 RW[101] - \frac{1}{4} n^3 h[3]^2 RW[101] + <<1829>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[1, 5], ar[3, 4], ar[6, 2]] →  $-\frac{1}{8} nh[1]^2 RW[] - \frac{1}{2} n^2 h[1] RW[101] - \frac{1}{2} n^3 h[1] RW[101] +$ 

$$\frac{1}{4} n^2 h[1]^2 RW[101] + \frac{1}{2} n^3 h[1]^2 RW[101] + <<2171>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[1, 5], ar[4, 3], ar[6, 2]] →  $-\frac{1}{8} nh[1]^2 RW[] + \frac{1}{2} n^2 h[1] RW[101] + \frac{1}{2} n^3 h[1] RW[101] -$ 

$$\frac{1}{2} n^2 h[1]^2 RW[101] - \frac{1}{2} n^3 h[1]^2 RW[101] + <<2663>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[2, 3], ar[4, 6], ar[5, 1]] →  $-\frac{1}{8} nh[1]^2 RW[] + \frac{1}{2} n^2 h[1] RW[101] +$ 

$$\frac{1}{2} n^3 h[1] RW[101] + \frac{1}{4} n^2 h[1]^2 RW[101] + <<2191>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[2, 3], ar[5, 1], ar[6, 4]] →

$$-\frac{1}{8} nh[1]^2 RW[] + 2 n^2 RW[101] + 5 n^3 RW[101] + <<2480>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$

Diag[ar[3, 2], ar[4, 6], ar[5, 1]] →

$$-\frac{1}{8} nh[1]^2 RW[] - \frac{1}{2} n^2 h[1] RW[101] - \frac{1}{2} n^3 h[1] RW[101] - n^2 h[1]^2 RW[101] -$$


$$\frac{1}{2} n^3 h[1]^2 RW[101] - \frac{1}{4} n^2 h[1]^3 RW[101] + <<2665>> + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$$


$$6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$$


$$6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601]$$


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Diag[ar[3, 2], ar[5, 1], ar[6, 4]] → - $\frac{1}{8}$  n h[1]2 RW[] - 2 n2 RW[101] - 5 n3 RW[101] -
3 n4 RW[101] +  $\frac{1}{2}$  n2 h[1] RW[101] + <>2525>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 4], ar[3, 6], ar[5, 1]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{1}{2}$  n2 h[1] RW[101] +
 $\frac{1}{2}$  n3 h[1] RW[101] +  $\frac{1}{4}$  n2 h[1]2 RW[101] + <>2203>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 4], ar[5, 1], ar[6, 3]] → - $\frac{1}{8}$  n h[1]2 RW[] + 4 n2 RW[101] + 7 n3 RW[101] +
3 n4 RW[101] +  $\frac{1}{2}$  n2 h[1] RW[101] + <>2722>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 6], ar[4, 2], ar[5, 1]] →
- $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{3}{2}$  n2 h[1] RW[101] -  $\frac{3}{2}$  n3 h[1] RW[101] - n2 h[1]2 RW[101] -
 $\frac{1}{2}$  n3 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[1]3 RW[101] + <>2685>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[4, 2], ar[5, 1], ar[6, 3]] → <>2597>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[3, 4], ar[5, 1]] → - $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{1}{2}$  n2 h[1] RW[101] +
 $\frac{1}{2}$  n3 h[1] RW[101] +  $\frac{1}{4}$  n2 h[1]2 RW[101] + <>2176>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 6], ar[4, 3], ar[5, 1]] →
- $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1] RW[101] -  $\frac{1}{2}$  n3 h[1] RW[101] - n2 h[1]2 RW[101] -
 $\frac{1}{2}$  n3 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[1]3 RW[101] + <>2661>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 4], ar[5, 1], ar[6, 2]] →
- $\frac{1}{8}$  n h[1]2 RW[] + 4 n2 RW[101] + 10 n3 RW[101] + <>2397>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

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Diag[ar[4, 3], ar[5, 1], ar[6, 2]] → <<2562>> + 6 n6 <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 3], ar[4, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
   $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <<597>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 3], ar[5, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
   $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <<1818>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[3, 2], ar[4, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
   $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <<1818>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[3, 2], ar[5, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{2}$  n2 h[1]2 RW[101] -  $\frac{1}{2}$  n2 h[2]2 RW[101] -
   $\frac{1}{2}$  n3 h[2]2 RW[101] -  $\frac{1}{2}$  n3 h[3]2 RW[101] + <<2328>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 4], ar[3, 5]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
   $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <<611>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 4], ar[5, 3]] →
  -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] + <<2062>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[3, 5], ar[4, 2]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -
   $\frac{1}{4}$  n2 h[1]3 RW[101] + <<2063>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

```

```

Diag[ar[1, 6], ar[4, 2], ar[5, 3]] → <<2404>> + 6 n6 RW[<<1>>] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 5], ar[3, 4]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{3}{8}$  n h[1]2 RW[101, 101] +
   $\frac{3}{8}$  n2 h[2]2 RW[101, 101] + <<561>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[2, 5], ar[4, 3]] → -  $\frac{1}{8}$  n h[1]2 RW[] -  $\frac{1}{4}$  n2 h[1]2 RW[101] -  $\frac{1}{4}$  n2 h[2]2 RW[101] -
   $\frac{1}{4}$  n3 h[2]2 RW[101] -  $\frac{1}{4}$  n3 h[3]2 RW[101] + <<1818>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[3, 4], ar[5, 2]] → -  $\frac{1}{8}$  n h[1]2 RW[] +  $\frac{1}{4}$  n2 h[1]2 RW[101] +  $\frac{1}{2}$  n3 h[1]2 RW[101] +
   $\frac{1}{4}$  n2 h[2]2 RW[101] +  $\frac{3}{4}$  n3 h[2]2 RW[101] + <<1914>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[1, 6], ar[4, 3], ar[5, 2]] → <<2410>> + 6 n6 RW[<<1>>] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 3], ar[4, 5], ar[6, 1]] →
  -  $\frac{1}{8}$  n h[1]2 RW[] - n2 RW[101] - 3 n3 RW[101] - 2 n4 RW[101] +  $\frac{3}{4}$  n2 h[1]2 RW[101] + n3 h[1]2 RW[101] +
    <<1923>> + 6 n6 RW[105, 204, 306, 402, 501, 603] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
    6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
    6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 3], ar[5, 4], ar[6, 1]] →
  -  $\frac{1}{8}$  n h[1]2 RW[] + n2 RW[101] + 3 n3 RW[101] + <<2383>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
    6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
    6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 2], ar[4, 5], ar[6, 1]] →
  -  $\frac{1}{8}$  n h[1]2 RW[] + n2 RW[101] + 3 n3 RW[101] + <<2383>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
    6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
    6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 2], ar[5, 4], ar[6, 1]] →
  <<2529>> + 6 n6 RW[105, 204, 306, 402, 501, 603] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
  6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
  6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

```

```

Diag[ar[2, 4], ar[3, 5], ar[6, 1]] → - $\frac{1}{8}$  n h[1]2 RW[] - n2 RW[101] - n3 RW[101] +  $\frac{3}{4}$  n2 h[1]2 RW[101] +
n3 h[1]2 RW[101] +  $\frac{3}{4}$  n2 h[2]2 RW[101] + <<1936>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 4], ar[5, 3], ar[6, 1]] →
- $\frac{1}{8}$  n h[1]2 RW[] + 3 n2 RW[101] + 6 n3 RW[101] + 3 n4 RW[101] + n2 h[1] RW[101] + <<2715>> +
6 n6 RW[105, 204, 306, 402, 501, 603] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 5], ar[4, 2], ar[6, 1]] → - $\frac{1}{8}$  n h[1]2 RW[] + 3 n2 RW[101] + 6 n3 RW[101] +
<<2717>> + 6 n6 RW[105, 204, 306, 402, 501, 603] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[4, 2], ar[5, 3], ar[6, 1]] → <<2561>> + 6 n6 <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[3, 4], ar[6, 1]] →
- $\frac{1}{8}$  n h[1]2 RW[] - n2 RW[101] - 2 n3 RW[101] - n4 RW[101] +  $\frac{3}{4}$  n2 h[1]2 RW[101] + n3 h[1]2 RW[101] +
<<1937>> + 6 n6 RW[105, 204, 306, 402, 501, 603] + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[2, 5], ar[4, 3], ar[6, 1]] →
- $\frac{1}{8}$  n h[1]2 RW[] + n2 RW[101] + 2 n3 RW[101] + <<2398>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[3, 4], ar[5, 2], ar[6, 1]] → - $\frac{1}{8}$  n h[1]2 RW[] + 3 n2 RW[101] + 7 n3 RW[101] + 4 n4 RW[101] +
 $\frac{1}{2}$  n3 h[1]2 RW[101] +  $\frac{1}{2}$  n3 h[2]2 RW[101] + <<2449>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

Diag[ar[4, 3], ar[5, 2], ar[6, 1]] → <<2508>> + <<1>> + 6 n5 RW[105, 205, 304, 403, 501, 502] +
6 n6 RW[105, 206, 304, 403, 501, 602] + 6 n6 RW[106, 203, 302, 405, 504, 601] +
6 n6 RW[106, 204, 305, 402, 503, 601] + 6 n6 RW[106, 205, 304, 403, 502, 601]

```

```

{Null, Null, Null,
 Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null,
 Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null,
 Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null,
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 Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null,
 Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null, Null}

```

```

rels3 = R /@ Diagrams [R6T + 1 ar];
Expand[UGLnBiAlg [rels3]]

```

```

{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}

```

```

vs = UGLnBiAlg /@ Diagrams [3 ar]

```

A very large output was generated. Here is a sample of it:

```

{-  $\frac{1}{8} n h[1]^2 RW[] + \frac{3}{8} n h[1]^2 RW[101, 101] + \frac{3}{8} n^2 h[2]^2 RW[101, 101] + 4 n^2 RW[102, 201] -$ 
  $\frac{9}{4} n^2 h[1]^2 RW[102, 201] - \frac{9}{4} n^2 h[2]^2 RW[102, 201] - \frac{9}{4} n^3 h[3]^2 RW[102, 201] + <>595> +$ 
  $6 n^5 RW[105, 204, 304, 402, 403, 501] + 6 n^5 RW[105, 204, 305, 402, 501, 503] +$ 
  $6 n^6 RW[105, 204, 306, 402, 501, 603] + 6 n^5 RW[105, 205, 304, 403, 501, 502] +$ 
  $6 n^6 RW[105, 206, 304, 403, 501, 602] + 6 n^6 RW[106, 203, 302, 405, 504, 601] +$ 
  $6 n^6 RW[106, 204, 305, 402, 503, 601] + 6 n^6 RW[106, 205, 304, 403, 502, 601], <>1>, <>1>, <>114>, <>1>, <>11>, <>2512> + <>1> + 6 n^6 RW[106, 205, 304, 403, 502, 601]}$ 

```

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```

MonomialsIn[expr_] /; ! MemberQ[{List, Plus, Times}, Head[expr]] := {expr};
MonomialsIn[p_Times] := {Replace[p, c_?NumberQ :> 1, {1}]};
MonomialsIn[l_List] := Union @@ (MonomialsIn /@ l);
MonomialsIn[s_Plus] := MonomialsIn[List @@ s];

ts = MonomialsIn[vs]

```

A very large output was generated. Here is a sample of it:

```

{n h[1]^2 RW[], n^2 RW[101], n^3 RW[101], n^4 RW[101], n^2 h[1] RW[101], n^3 h[1] RW[101],
 n^2 h[1]^2 RW[101], n^3 h[1]^2 RW[101], n^2 h[1]^3 RW[101], n^2 h[2] RW[101], n^3 h[2] RW[101],
 <>1913>, n^6 RW[105, 203, 302, 406, 501, 604], n^5 RW[105, 204, 303, 303, 402, 501],
 n^5 RW[105, 204, 304, 402, 403, 501], n^5 RW[105, 204, 305, 402, 501, 503],
 n^6 RW[105, 204, 306, 402, 501, 603], n^5 RW[105, 205, 304, 403, 501, 502],
 n^6 RW[105, 206, 304, 403, 501, 602], n^6 RW[106, 203, 302, 405, 504, 601],
 n^6 RW[106, 204, 305, 402, 503, 601], n^6 RW[106, 205, 304, 403, 502, 601]}

```

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```
rule = Dispatch[Thread[ts → Array[b, {Length[ts]}]]]
```

A very large output was generated. Here is a sample of it:

```
Dispatch[{n h[1]^2 RW[] → b[1], n^2 RW[101] → b[2], n^3 RW[101] → b[3], n^4 RW[101] → b[4],  
n^2 h[1] RW[101] → b[5], n^3 h[1] RW[101] → b[6], n^2 h[1]^2 RW[101] → b[7],  
n^3 h[1]^2 RW[101] → b[8], <<1918>>, n^5 RW[105, 204, 304, 402, 403, 501] → b[1927],  
n^5 RW[105, 204, 305, 402, 501, 503] → b[1928],  
n^6 RW[105, 204, 306, 402, 501, 603] → b[1929],  
n^5 RW[105, 205, 304, 403, 501, 502] → b[1930],  
n^6 RW[105, 206, 304, 403, 501, 602] → b[1931],  
n^6 RW[106, 203, 302, 405, 504, 601] → b[1932],  
n^6 RW[106, 204, 305, 402, 503, 601] → b[1933],  
n^6 RW[106, 205, 304, 403, 502, 601] → b[1934]}, -<<14>>-]
```

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```
mat = SparseArray[  
Join @@ Table[  
v = vs[[i]];  
Table[  
t = v[[j]];  
c = t /. {_h → 1, _RW → 1, n → 1};  
{i, Replace[t/c, rule] /. b[k_] :> k} → c,  
{j, Length[v]}  
],  
,  
{i, Length[vs]}  
],  
{Length[vs1], Length[ts]}  
]  
  
SparseArray[<171 210>, {120, 1934}]
```

```
MatrixRank[mat]
```