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m = 2;
n = 3;
InitFiber[m_, n_] := Block[{ff, u, v, x, y, z, w, gg, curves, tubes},
  ff = u^m - v^n /. {u -> x + I y, v -> z + w I};
  {milnorf, milnorg} = Factor[
    (ComplexExpand[{Re[ff], Im[ff]}] /. {x ->  $\frac{\sqrt{2}(-2+x^2+y^2+z^2)}{2+x^2+y^2+z^2}$ , y ->  $\frac{4x}{2+x^2+y^2+z^2}$ ,
      z ->  $\frac{4y}{2+x^2+y^2+z^2}$ , w ->  $\frac{4z}{2+x^2+y^2+z^2}$ }] * (2+x^2+y^2+z^2)^Max[m, n];
  curves = Table[{- $\frac{\text{Sqrt}[2] y}{-\text{Sqrt}[2] + x}$ , - $\frac{\text{Sqrt}[2] z}{-\text{Sqrt}[2] + x}$ , - $\frac{\text{Sqrt}[2] w}{-\text{Sqrt}[2] + x}$ } /.
    {x -> Cos[n u + 2 Pi k / m], y -> Sin[n u + 2 Pi k / m],
      z -> Cos[m u], w -> Sin[m u]}, {k, 0, GCD[m, n] - 1}];
  tubes = Table[MyTube[curves[[i]], .1], {i, 1, Length[curves]}];
  milnorlink =
    Show[Table[ParametricPlot3D[tubes[[i]], {u, 0, 2 Pi}, {v, 0, 2 Pi}, PlotPoints -> 100,
      PlotStyle -> RGBColor[1, (i - 1) / Length[tubes], (i - 1) / Length[tubes]],
      Mesh -> None], {i, 1, Length[tubes]}], PlotRange -> All,
    Background -> Black, Boxed -> False, Axes -> False, ViewPoint -> {5, 0, 0}];
];

MyTube[r_, rad_] := Module[{dr, dr2, n1, b1, cc, tube},
  dr = D[r, u];
  dr2 = D[dr, u];
  n1 = dr2 - (dr . dr2) dr / (dr . dr);
  b1 = Cross[n1, dr];
  cc = Cos[v] n1 + Sin[v] b1;
  tube = r + rad cc / Sqrt[cc . cc];
  Return[tube];
];

DrawFiber[th_, op1_, op2_] := Block[{f1, g1, c1, c2},
  f1 = Cos[th] milnorf + Sin[th] milnorg;
  g1 = Sin[th] milnorf - Cos[th] milnorg;
  c1 = Directive[Specularity[White, 30], Opacity[op1], Green];
  c2 = Directive[Specularity[White, 30], Opacity[op2], Orange];
  Show[ContourPlot3D[{f1 == 0}, {x, -4, 4}, {y, -4, 4},
    {z, -4, 4}, ColorFunction -> Function[{x, y, z, f}, If[g1 > 0, c1, c2]],
    ColorFunctionScaling -> False, Mesh -> None, PlotPoints -> 50, BoundaryStyle -> None,
    Lighting -> Automatic], milnorlink, Boxed -> False, Axes -> False,
    ViewPoint -> {5, 0, 0}, Background -> Black, ImageSize -> {800, 600}]
];

InitFiber[2, 3]

DrawFiber[0, 1, 0]

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tubes = Table[MyTube[curves[[i]], .1], {i, 1, Length[curves]}];
milnorlink =
  Show[Table[ParametricPlot3D[tubes[[i]], {u, 0, 2 Pi}, {v, 0, 2 Pi}, PlotPoints -> 100,
    PlotStyle -> RGBColor[1, (i - 1) / Length[tubes], (i - 1) / Length[tubes]],
    Mesh -> None], {i, 1, Length[tubes]}], PlotRange -> All,
  Background -> Black, Boxed -> False, Axes -> False, ViewPoint -> {5, 0, 0}];

curves = Table[{- Sqrt[2] y / (-Sqrt[2] + x), - Sqrt[2] z / (-Sqrt[2] + x), - Sqrt[2] w / (-Sqrt[2] + x)} /. {x -> Cos[n u + 2 Pi k / m],
  y -> Sin[n u + 2 Pi k / m], z -> Cos[m u], w -> Sin[m u]}, {k, 0, GCD[m, n] - 1}]

ReOrder[{z_, y_, x_}] := {x, y, z}

Show[Table[ParametricPlot3D[tubes[[i]], {u, 0, 2 Pi}, {v, 0, 2 Pi}, PlotPoints -> 100,
  PlotStyle -> RGBColor[1, (i - 1) / Length[tubes], (i - 1) / Length[tubes]], Mesh -> None],
  {i, 1, Length[tubes]}], PlotRange -> All, Background -> Black,
  Boxed -> False, Axes -> False, ViewPoint -> {5, 0, 0}]

ParametricPlot3D[CHANGE[tubes[[1]]],
  {u, 0, 2 Pi}, {v, 0, 2 Pi}, PlotPoints -> 30, MeshStyle -> None]

CHANGE[{x_, y_, z_}] :=
  CoordinateTransformData["Cartesian" -> "Cylindrical", "Mapping", {x, y, z}]

CHANGE[tubes[[1]]] // Simplify

ParametricPlot3D[ReOrder /@ curves, {u, 0, 2 Pi}, AxesLabel -> {"x", "y", "z"}]

knot = Flatten@ (ReOrder /@ curves)

CoordinateTransformData["Cartesian" -> "Cylindrical", "Mapping", knot]

ParametricPlot3D[CoordinateTransformData["Cartesian" -> "Cylindrical", "Mapping", knot],
  {u, 0, 2 Pi}, Exclusions -> True]

Manipulate[
  Show[ParametricPlot3D[curves, {u, 0, 2 Pi}, AxesLabel -> {"x", "y", "z"}],
    Graphics3D[{PointSize[0.05], Point[curves /. u -> U]}],
    Graphics3D@Text[Theta /@ curves /. u -> U], {U, 0, 2 Pi}]

 $\pi/2$  // N

Theta /@ curves

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