

Study $Ay = b$ where A & b are ^{cont.} functions
of $x \in \mathbb{B}^n$.

Is there a continuous solution?

Example. Solve

$$x^2 F_1 + y^2 F_2 + xyz^2 F_3 = xyz$$

for the F_i 's.

Can't! Looking at $(x, 0, z)$ get $F_1(x, 0, z) = 0$

likewise $F_2(0, y, z) = 0$

$$\text{so } F_1(0, 0, z) = F_2(0, 0, z) = 0$$

but when $(x, x, z) \rightarrow (0, 0, z)$ get

$$F_3(0, 0, z) = \frac{1}{z} \text{ not cont. at } z=0.$$