

$$(a,b) \cdot (c,d) := (ac-bd, bc+ad)$$

$$-(a,b) := (-a, -b)$$

$$(a,b)^{-1} := \left(\frac{a}{a^2+b^2}, \frac{-b}{a^2+b^2} \right)$$

if $(a,b) \neq (0,0)$
 $\Leftrightarrow a \neq 0 \wedge b \neq 0$

$$\begin{aligned} \tau: \mathbb{R} &\longrightarrow \mathbb{C} \quad \text{by } (a \mapsto (a,0)) \\ \tau &\mapsto (7,0) \end{aligned}$$

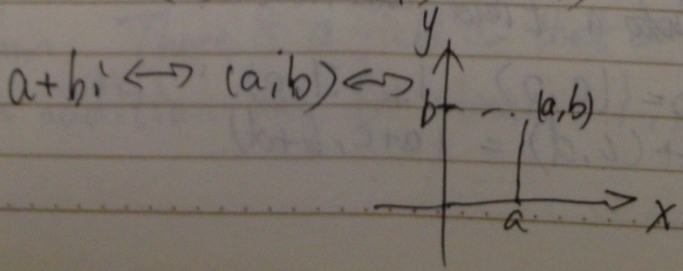
$a, b, c \in \mathbb{R}$

$$\tau(a \cdot b) = \tau(a) \cdot \tau(b)$$

$$\tau(a+b) = \tau(a) + \tau(b)$$

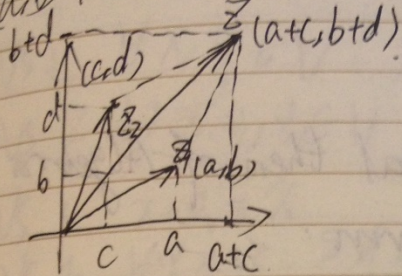
Then \mathbb{C} is a field, $i^2 = -1$, $\tau: \mathbb{R} \rightarrow \mathbb{C}$
has the two desired property.

$$\begin{aligned} 3+7i &= (3,0) + (-7,0) \cdot (0,1) \\ &= (3,0) + (7 \cdot 0 - 0 \cdot 1, 7 \cdot 1 + 0 \cdot 0) \\ &= (3,0) + (0,7) = (3,7) \end{aligned}$$



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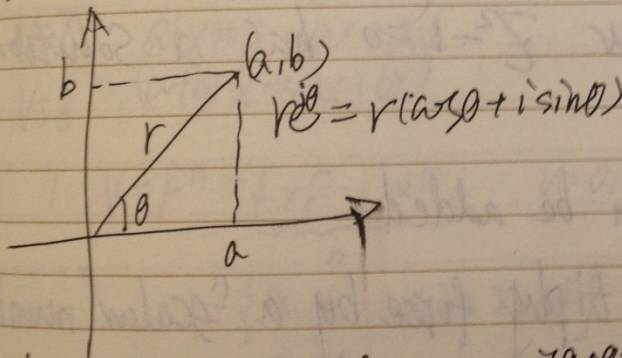
$$(a+ib) + (c+id) = (a+c) + i(b+d)$$



9.22

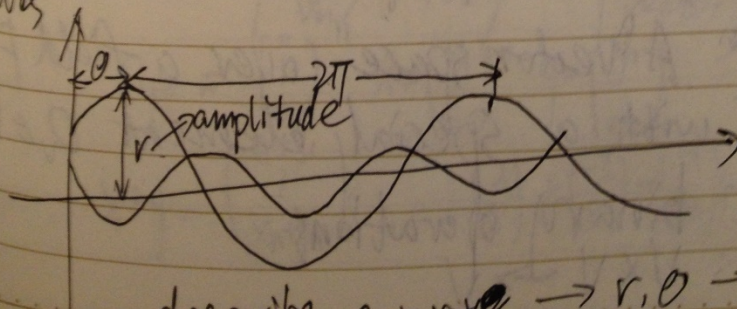
$$(a+ib) \neq 0 \Leftrightarrow a \neq 0 \vee (b \neq 0) \Leftrightarrow a^2 + b^2 > 0$$

Polar Coordinates



claim $r_1 e^{i\theta_1} \cdot r_2 e^{i\theta_2} = r_1 r_2 e^{i(\theta_1 + \theta_2)}$

waves



Ohm's Law

$$V = R \cdot I$$

Thm "The fundamental theorem of Algebra"

Any eqn of the form:

$$a_n z^n + a_{n-1} z^{n-1} + \dots + a_0 = 0$$

When $a_i \in \mathbb{C}$ and $a_n \neq 0$ has a solution

$$z \in \mathbb{C}$$

In particular $z^2 - 1 = 0$ has a solution

Forces can be added

can multiply force by a "scalar" number

No "multiplication" of forces

Definition A "vector space" over a field F is a set V with a special element $0_v \in V$ and two binary operations:

$$+ : V \times V \rightarrow V$$

$$\times : F \times V \rightarrow V$$