Dror Bar-Natan: Talks: MSRI-0808: Projectivization, w-Knots, Kashiwara-Vergne and Alekseev-Torossian: We Mean Business

Trivalent (framed) w-tangles:

further operations: delete, unzip.

 $wTT = CA \left\langle \begin{array}{c} \\ \\ \end{array} \right\rangle / R123, R4 \text{ (for vertices), F, OC.}$ 

=tangles in thick surfaces, modulo stabilization)











Partial Dictionary

 $(R,F) \hookrightarrow (X, L) (r,t) \rightleftharpoons (H, H)$ FF! = 1 -> >

$$F^{-1}((x+y))F = \ell(x)\ell(y)$$

$$F^{23}R^{1/23} = R^{12}R^{13}F^{23} \iff f^{23}$$

$$R^{12,3} = R^{13}R^{23}$$
 $P^{12,3} = R^{13}R^{23} = R^{13}R^{23}$ 

(unforbiding FI makes this automatic)

D=(-12,3)-1(-1,2)-1--13-1,23

The pertagon and the hexagons Follow, with a minor twist, from the fact that we have an unzia behaved invariant of KTG's

Visit!

Edit!

"God created the knots all else in topology is the work of mortals'

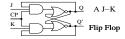
Leopold Kronecker (paraphrased)



This handout and further links are at http://www.math.toronto.edu/~drorbn/Talks/MSRI-0808/

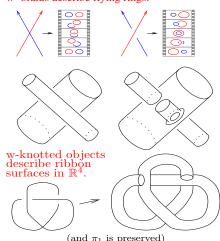
Circuit Algebras \* Have "circuits"

with "ends"



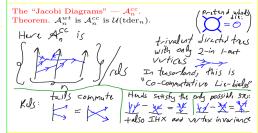
- \* Can be wired arbitrarily.
- \* May have "relations" de-Morgan, etc.

w-braids describe flying rings:



For the Experienced (and sharp-eyed)

The "Chord Diagrams" —  $\mathcal{A}_n^{wt}$ . As we did for into the various mary, to get relations Also switch to "arrow diagram language": The tests comments of the second of the second



The Map  $\alpha: \mathcal{A}_n^{tree} \to \mathcal{A}_n^{cc}$ :

Theorem.  $\alpha$  is an injection on  $\mathcal{A}_n^{tree} \cong \mathcal{U}(\operatorname{sder}_n)$ . Furthermore, there is a simple charactarization of im  $\alpha$ , so we can tell "an arrowless element" when we see it.

The Main Theorem. (approximate, false as stated) F's in  $Sol_0^{\tau}$ are in a bijective correspondance with tree-level associators for ordinary paranthesized tangles (or ordinary knotted trivalent graphs) / with homomorphic expansions for trivalent w-tangles / with solutions of the Kashiwara-Vergne problem.

Extra. Restricted to knots, we get precisely the Alexander polynomial.

Disclaimer. Orientations, rotation numbers, framings, the vertical direction and the cyclic symmetry of the vertex may still make everything uglier. I hope not.