## Dror Bar-Natan: Talks: Cornell-150925: $\omega := http://drorbn.net/C15$

Abstract. Much as we can understand 3-dimensional objects by staring at their pictures and x-ray images and slices in 2dimensions, so can we understand 4-dimensional objects by staring at their pictures and x-ray images and slices in 3dimensions, capitalizing on the fact that we understand 3dimensions pretty well. So we will spend some time staring at and understanding various 2-dimensional views of a 3dimensional elephant, and then even more simply, various 2dimensional views of some 3-dimensional knots. This achieved, we'll take the leap and visualize some 4-dimensional knots by their various traces in 3-dimensional space, and if we'll still have time, we'll prove that these knots are really knotted.

## Warmup: Flatlanders View an Elephant.



2-Knots / 4D Knots. Formally, "a differentiable embedding of  $S^2$  in  $\mathbb{R}^4$ modulo differentiable deformations of such". A 4D knot by Carter and Saito  $\omega/CS$ 

"broken surface diagram"



Riddle. Is  $\lambda(K)$  always a power of 3?

**Proof sketch.** It is enough to show that for each Reidemeister move, there is an end-colours-preserving bijection between the colourings of the two sides. E.g.:



Video and more at http://www.math.toronto.edu/~drorbn/Talks/Cornell-150925/. Similar talks at .../CUMC-1307/, .../CUMC-1307/