

Find everything at <http://drorbn.net/syd3>

The graph consists of nodes labeled with blue and red numbers. The nodes are arranged in a roughly rectangular layout. The edges are directed and labeled with red numbers. The graph shows a complex set of connections between the nodes, with some nodes having multiple incoming and outgoing edges. The overall structure suggests a complex network flow or a complex dependency graph.

$$Out[\bullet]=\{100, 81, 32400, 676, Zsuzsi^2\}$$

In[]:= **t1** = **K** /. **X**[**i_**, **j_**, **k_**, **l_**] → **A** * **p**[**i**, **j**] * **p**[**k**, **l**] + **B** * **p**[**i**, **l**] **p**[**j**, **k**]

Out[]:= **PD**[**A** **p**[**1**, **5**] **p**[**2**, **4**] + **B** **p**[**1**, **4**] **p**[**5**, **2**],
B **p**[**3**, **6**] **p**[**5**, **2**] + **A** **p**[**5**, **3**] **p**[**6**, **2**], **B** **p**[**1**, **4**] **p**[**3**, **6**] + **A** **p**[**3**, **1**] **p**[**4**, **6**]]

In[]:= **t1**

Out[]:= **PD**[**A** **p**[**1**, **5**] **p**[**2**, **4**] + **B** **p**[**1**, **4**] **p**[**5**, **2**],
B **p**[**3**, **6**] **p**[**5**, **2**] + **A** **p**[**5**, **3**] **p**[**6**, **2**], **B** **p**[**1**, **4**] **p**[**3**, **6**] + **A** **p**[**3**, **1**] **p**[**4**, **6**]]

In[]:= **Expand**[(**a** + **b**) (**a** - **b**)]

Out[]:= **a**² - **b**²

In[]:= **Factor**[**a**² - **b**²]

Out[]:= (**a** - **b**) (**a** + **b**)

In[]:= **Expand**[**t1**]

Out[]:= **PD**[**A** **p**[**1**, **5**] **p**[**2**, **4**] + **B** **p**[**1**, **4**] **p**[**5**, **2**],
B **p**[**3**, **6**] **p**[**5**, **2**] + **A** **p**[**5**, **3**] **p**[**6**, **2**], **B** **p**[**1**, **4**] **p**[**3**, **6**] + **A** **p**[**3**, **1**] **p**[**4**, **6**]]

In[]:= **Factor**[**a**² - **b**²] // **FullForm**

Out[]//FullForm= **Times**[**Plus**[**a**, **Times**[-**1**, **b**]], **Plus**[**a**, **b**]]

In[]:= **t2** = **Expand**[**t1** /. **PD** → **Times**]

Out[]:= **A** **B**² **p**[**1**, **4**] **p**[**1**, **5**] **p**[**2**, **4**] **p**[**3**, **6**]² **p**[**5**, **2**] + **A**² **B** **p**[**1**, **5**] **p**[**2**, **4**] **p**[**3**, **1**] **p**[**3**, **6**] **p**[**4**, **6**] **p**[**5**, **2**] +
B³ **p**[**1**, **4**]² **p**[**3**, **6**]² **p**[**5**, **2**]² + **A** **B**² **p**[**1**, **4**] **p**[**3**, **1**] **p**[**3**, **6**] **p**[**4**, **6**] **p**[**5**, **2**]² +
A² **B** **p**[**1**, **4**] **p**[**1**, **5**] **p**[**2**, **4**] **p**[**3**, **6**] **p**[**5**, **3**] **p**[**6**, **2**] +
A³ **p**[**1**, **5**] **p**[**2**, **4**] **p**[**3**, **1**] **p**[**4**, **6**] **p**[**5**, **3**] **p**[**6**, **2**] +
A **B**² **p**[**1**, **4**]² **p**[**3**, **6**] **p**[**5**, **2**] **p**[**5**, **3**] **p**[**6**, **2**] + **A**² **B** **p**[**1**, **4**] **p**[**3**, **1**] **p**[**4**, **6**] **p**[**5**, **2**] **p**[**5**, **3**] **p**[**6**, **2**]

In[]:= {**7**, **1**} /. {{**0**, **n_**} → **n**, {**k_**, **n_**} → {**k** - **1**, **n** * **k**}}

Out[]:= {**6**, **7**}

In[]:= {**7**, **1**} //. {{**0**, **n_**} → **n**, {**k_**, **n_**} → {**k** - **1**, **n** * **k**}}

Out[]:= **5040**

In[]:= **t3** = **t2** //. **p**[**i_**, **j_**] **p**[**j_**, **k_**] → **p**[**i**, **k**]

Out[]:= **A**² **B** **p**[**1**, **4**]² + **A**³ **p**[**2**, **2**] **p**[**3**, **3**] + **A**² **B** **p**[**3**, **6**]² + **A** **B**² **p**[**1**, **4**]² **p**[**3**, **6**]² + **A**² **B** **p**[**5**, **2**]² +
A **B**² **p**[**1**, **4**]² **p**[**5**, **2**]² + **A** **B**² **p**[**3**, **6**]² **p**[**5**, **2**]² + **B**³ **p**[**1**, **4**]² **p**[**3**, **6**]² **p**[**5**, **2**]²

In[]:= **t4** = **t3** /. {**p**[**i_**, **i_**] → **d**, **p**[**i_**, **j_**]² → **d**}

Out[]:= **3** **A**² **B** **d** + **A**³ **d**² + **3** **A** **B**² **d**² + **B**³ **d**³

In[]:= **t5** = **Expand**[**t4** /. {**B** → **1/A**, **d** → -**A**² - **1/A**²}]

Out[]:= - $\frac{1}{A^9} + \frac{1}{A} + A^3 + A^7$

In[]:= **Knots**

Out[]:= $\{ \text{Knot}[3, 1] \rightarrow \text{PD}[X[1, 4, 2, 5], X[3, 6, 4, 1], X[5, 2, 6, 3]], \dots 248 \dots, \\ \text{GST48} \rightarrow \text{PD}[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3], X[4, 44, 5, 43], \dots 40 \dots, \\ X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]] \}$

large output

show less

show more

show all

set size limit...

In[]:= **Knot[3, 1] /. Knots**

Out[]:= $\text{PD}[X[1, 4, 2, 5], X[3, 6, 4, 1], X[5, 2, 6, 3]]$

In[]:= **Knot[10, 165] /. Knots**

Out[]:= $\text{PD}[X[1, 6, 2, 7], X[7, 18, 8, 19], X[3, 9, 4, 8], X[17, 3, 18, 2], X[5, 15, 6, 14], \\ X[9, 17, 10, 16], X[15, 11, 16, 10], X[11, 5, 12, 4], X[20, 14, 1, 13], X[12, 20, 13, 19]]$

In[]:= **K = Knot[10, 73] /. Knots;**

t1 = K /. X[i_, j_, k_, l_] → A * p[i, j] * p[k, l] + B * p[i, l] p[j, k];

t2 = Expand[t1 /. PD → Times];

t3 = t2 /. {p[i_, j_] p[j_, k_] → p[i, k], p[i_, j_] p[k_, j_] → p[i, k]};

t4 = t3 /. {p[i_, i_] → d, p[i_, j_] ^2 → d};

Expand[t4 /. {B → 1/A, d → -A^2 - 1/A^2}]

Out[]:= $\frac{1}{A^{22}} - \frac{3}{A^{18}} + \frac{3}{A^{14}} - \frac{4}{A^{10}} + \frac{2}{A^6} - \frac{1}{A^2} - A^2 + 3 A^6 - 4 A^{10} + 3 A^{14} - 2 A^{18} + A^{22}$

In[]:= **K = GST48 /. Knots**

Out[]:= $\text{PD}[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3], X[4, 44, 5, 43], X[5, 26, 6, 27], \\ X[95, 7, 96, 6], X[7, 1, 8, 96], X[8, 14, 9, 13], X[28, 9, 29, 10], X[41, 11, 42, 10], \\ X[11, 43, 12, 42], X[12, 27, 13, 28], X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18], \\ X[83, 18, 84, 19], X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80], \\ X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62], X[32, 74, 33, 73], \\ X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36], X[70, 38, 71, 37], X[59, 39, 60, 38], \\ X[54, 39, 55, 40], X[55, 45, 56, 44], X[45, 59, 46, 58], X[46, 70, 47, 69], \\ X[47, 81, 48, 80], X[91, 49, 92, 48], X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52], \\ X[60, 54, 61, 53], X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77], \\ X[66, 87, 67, 88], X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]]$

In[]:= **Length[K]**

Out[]:= 48

In[]:= **K = GST48 /. Knots;**

t1 = K /. X[i_, j_, k_, l_] → A * p[i, j] * p[k, l] + B * p[i, l] p[j, k];

t2 = Expand[t1 /. PD → Times];

t3 = t2 /. {p[i_, j_] p[j_, k_] → p[i, k],

p[i_, j_] p[k_, j_] → p[i, k], p[j_, i_] p[j_, k_] → p[i, k]};

t4 = t3 /. {p[i_, i_] → d, p[i_, j_] ^2 → d};

Expand[t4 /. {B → 1/A, d → -A^2 - 1/A^2}]

Out[]:= \$Aborted

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In[ ]:= K = Knot[8, 17] /. Knots;
SetAttributes[p, Orderless];
t1 = K /. X[i_, j_, k_, l_] -> A * p[i, j] * p[k, l] + B * p[i, l] p[j, k];
t2 = Expand[t1 /. PD -> Times];
t3 = t2 /. {p[i_, j_] p[j_, k_] -> p[i, k]};
t4 = t3 /. {p[i_, i_] -> d, p[i_, j_]^2 -> d};
Expand[t4 /. {B -> 1/A, d -> -A^2 - 1/A^2}]

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$$\text{Out[]} = -\frac{1}{A^{18}} + \frac{2}{A^{14}} - \frac{2}{A^{10}} + \frac{1}{A^6} - \frac{1}{A^2} - A^2 + A^6 - 2A^{10} + 2A^{14} - A^{18}$$

Our blackboard:

