Goal. In either $U$, compute $F=\mathbb{e}^{-\eta y} e^{\xi x} e^{\eta y} \mathbb{e}^{-\xi x}$. First compute $G=\mathbb{e}^{\xi x} y \mathbb{e}^{-\xi x}$, a finite sum. Now $F$ satisfies the ODE
$\partial_{\eta} F=\partial_{\eta}\left(e^{-\eta y} e^{\eta G}\right)=-y F+F G$ with initial conditions $F(\eta=0)=1$. So
we set it up and solve:

