S is convolution inverse of id