

The Euler operator



$$aS(z) := z^{-1} a z \quad G(z) := z^{-1} E z$$

$$G(WZ) = Z^{-1} W^{-1} E(WZ)$$

(More glow formulas at
2008-08/BCH mod. [..])

$$= Z^{-1} W^{-1} E(W) \cdot Z + Z^{-1} W^{-1} W E(Z)$$

$$= G(W) S(Z) + G(Z)$$

$$G(\exp L) = e^{-L} E e^L = J(\text{ad } L) E(L) \quad \text{where } J(x) = \frac{1 - e^{-x}}{x}$$

G is injective except perhaps in degree 1.

How does it determine S ?

Or at least, is there a consistency equation relating G and S ?