

Pensieve header: Games with the centre of the ybox algebra.

## Startup

```
In[ ]:= Date[]
SetDirectory["C:\\drorbn\\AcademicPensieve\\Projects\\FullDoPeGDO"];
Once[<< KnotTheory`];
Once[Get@"./Profile/Profile.m"];
BeginProfile[];
$k = 1;
<< Engine.m
<< Objects.m
<< KT.m
```

```
Out[ ]:= {2021, 8, 3, 9, 44, 32.9501403}
```

Loading KnotTheory` version of February 2, 2020, 10:53:45.2097.

Read more at <http://katlas.org/wiki/KnotTheory>.

This is Profile.m of <http://www.drorbn.net/AcademicPensieve/Projects/Profile/>.

This version: April 2020. Original version: July 1994.

```
In[ ]:= $k = 2; (* ħ=γ=1; *)
```

```
In[ ]:= HL[ε_] := Style[ε, Background → If[TrueQ@ε, Green, Red]];
```

## Games

```
In[ ]:= Kink1
```

```
Out[ ]:= E_{{}→{1}} [  $\frac{\hbar b_1}{2} + \hbar a_1 b_1 + \hbar x_1 y_1, \frac{\hbar a_1}{2} - \frac{1}{4} \hbar^3 x_1^2 y_1^2, \frac{1}{9} \hbar^5 x_1^3 y_1^3 ]$ 
```

In[\*]:= Z[Knot[7, 1]]

» 4

$$\begin{aligned}
 \text{Out[*]} = & \mathbb{E}_{\{\} \rightarrow \{1\}} \left[ -4 t \hbar + \text{Log} \left[ \frac{T^7}{1 - T + T^2 - T^3 + T^4 - T^5 + T^6} \right], \right. \\
 & \frac{2 a (-1 + T) \times (1 + T) \times (3 - 2 T + 4 T^2 - 2 T^3 + 3 T^4) \hbar}{1 - T + T^2 - T^3 + T^4 - T^5 + T^6} + \\
 & \frac{(-1 + T) \times (6 - 5 T + 9 T^2 - 7 T^3 + 9 T^4 - 6 T^5 + 6 T^6 - 3 T^7 + 3 T^8 - T^9 + T^{10}) \hbar}{(1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^2} - \\
 & \frac{2 \times (1 + T) \times (3 - 2 T + 4 T^2 - 2 T^3 + 3 T^4) \times y \hbar^2}{1 - T + T^2 - T^3 + T^4 - T^5 + T^6}, \\
 & \frac{2 a^2 T (1 - 3 T + 6 T^2 - 3 T^3 + T^4) \times (1 - T + T^2 - 8 T^3 + T^4 - T^5 + T^6) \hbar^2}{(1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^2} + \\
 & (2 a T (1 - 7 T + 21 T^2 - 51 T^3 + 102 T^4 - 186 T^5 + 219 T^6 - 214 T^7 + \\
 & \quad 186 T^8 - 146 T^9 + 103 T^{10} - 66 T^{11} + 38 T^{12} - 19 T^{13} + 9 T^{14} - 3 T^{15} + T^{16}) \hbar^2) / \\
 & (1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^3 + \frac{1}{2 (1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^4} \\
 & (-1 + T) T (-1 + 10 T - 31 T^2 + 85 T^3 - 181 T^4 + 361 T^5 - 472 T^6 + 580 T^7 - 581 T^8 + 564 T^9 - 460 T^{10} + \\
 & \quad 380 T^{11} - 276 T^{12} + 205 T^{13} - 132 T^{14} + 88 T^{15} - 49 T^{16} + 29 T^{17} - 13 T^{18} + 7 T^{19} - 2 T^{20} + T^{21}) \hbar^2 - \\
 & \frac{4 a T (-4 + 2 T - 12 T^2 + 10 T^3 - 28 T^4 + 28 T^5 - 7 T^6 + 10 T^7 + 2 T^8 + 2 T^9 + 3 T^{10}) \times y \hbar^3}{(1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^2} + \\
 & \frac{1}{(1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^3} 2 \times (1 + T) \times (-9 + 21 T - 42 T^2 + 62 T^3 - 88 T^4 + 108 T^5 - 134 T^6 + \\
 & \quad 127 T^7 - 112 T^8 + 65 T^9 - 22 T^{10} - 32 T^{11} + 52 T^{12} - 50 T^{13} + 38 T^{14} - 21 T^{15} + 9 T^{16}) \times y \hbar^3 + \\
 & \left. \frac{(3 + 9 T + 9 T^2 + 31 T^3 + 14 T^4 + 70 T^5 + 14 T^6 + 31 T^7 + 9 T^8 + 9 T^9 + 3 T^{10}) \times^2 y^2 \hbar^4}{(1 - T + T^2 - T^3 + T^4 - T^5 + T^6)^2} \right]
 \end{aligned}$$

In[\*]:= **Z[Knot[8, 17]]**

**KnotTheory**: Loading precomputed data in PD4Knots`.

» 6

$$\begin{aligned}
 \text{Out[*]} = & \mathbb{E}_{\{\} \rightarrow \{1\}} \left[ -t \hbar + \text{Log} \left[ -\frac{T^4}{1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6} \right], \right. \\
 & \frac{(-1 + T) \times (1 + T) \times (1 - T + T^2) \times (3 - 5T + 3T^2) \hbar}{1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6} + \\
 & \frac{2a(-1 + T) \times (1 + T) \times (1 - T + T^2) \times (3 - 5T + 3T^2) \hbar}{1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6} - \\
 & \frac{2 \times (1 + T) \times (1 - T + T^2) \times (3 - 5T + 3T^2) \times y \hbar^2}{1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6}, \\
 & \frac{2aT(4 - 32T + 131T^2 - 304T^3 + 476T^4 - 548T^5 + 476T^6 - 304T^7 + 131T^8 - 32T^9 + 4T^{10}) \hbar^2}{(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^2} + \\
 & \frac{2a^2T(4 - 32T + 131T^2 - 304T^3 + 476T^4 - 548T^5 + 476T^6 - 304T^7 + 131T^8 - 32T^9 + 4T^{10}) \hbar^2}{(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^2} + \\
 & \left. \frac{((-1 + T)^2 T(4 - 42T + 219T^2 - 680T^3 + 1483T^4 - 2481T^5 + 3315T^6 - 3643T^7 + 3315T^8 - 2481T^9 + 1483T^{10} - 680T^{11} + 219T^{12} - 42T^{13} + 4T^{14}) \hbar^2}{2(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^3} + \right. \\
 & \frac{2 \times (-1 + T)(1 + T)^2(1 - T + T^2)^2(3 - 5T + 3T^2)^2 \times y \hbar^3}{(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^2} - \\
 & \frac{4aT(-7 + 42T - 136T^2 + 250T^3 - 312T^4 + 274T^5 - 164T^6 + 54T^7 + 5T^8 - 10T^9 + 3T^{10}) \times y \hbar^3}{(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^2} + \\
 & \left. \frac{(3 - 37T^2 + 153T^3 - 261T^4 + 325T^5 - 261T^6 + 153T^7 - 37T^8 + 3T^{10}) \times x^2 y^2 \hbar^4}{(1 - 4T + 8T^2 - 11T^3 + 8T^4 - 4T^5 + T^6)^2} \right]
 \end{aligned}$$