

Pensieve header: Perturbed Alexander-Burau Invariants. Continues Pensieve://2021-12/, but with the perturbation placed ahead of the bulk.

Programs

```
In[ ]:= Once[<< KnotTheory`];
```

Loading KnotTheory` version of February 2, 2020, 10:53:45.2097.
Read more at <http://katlas.org/wiki/KnotTheory>.

```
In[ ]:= PD[GST48] = PD[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3],
  X[4, 44, 5, 43], X[5, 26, 6, 27], X[95, 7, 96, 6], X[7, 1, 8, 96], X[8, 14, 9, 13],
  X[28, 9, 29, 10], X[41, 11, 42, 10], X[11, 43, 12, 42], X[12, 27, 13, 28],
  X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18], X[83, 18, 84, 19],
  X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80],
  X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62],
  X[32, 74, 33, 73], X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36],
  X[70, 38, 71, 37], X[59, 39, 60, 38], X[54, 39, 55, 40], X[55, 45, 56, 44],
  X[45, 59, 46, 58], X[46, 70, 47, 69], X[47, 81, 48, 80], X[91, 49, 92, 48],
  X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52], X[60, 54, 61, 53],
  X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77], X[66, 87, 67, 88],
  X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]];
```

```
In[ ]:= ThinPosition[K_] := Module[{todo, done, pd, c},
  todo = List@@PD@K; done = {}; pd = PD[];
  While[todo != {},
    AppendTo[pd, c = RandomChoice@MaximalBy[todo, Length[done ∩ List@@#] &]];
    todo = DeleteCases[todo, c];
    done = done ∪ List@@c];
  pd]
```

```
In[ ]:= RVK::usage =
  "RVK[xs, rots] represents a Rotational Virtual Knot with a list of n Xp/Xm crossings
  xs and a length 2n list of rotation numbers rots. Crossing
  sites are indexed 1 through 2n, and rots[[k]] is the rotation
  between site k-1 and site k. RVK is also a casting operator
  converting to the RVK presentation from other knot presentations.";
```

```

In[ ]:= RVK[pd_PD] := Module[{n, xs, x, rots, front = {1}, k},
  n = Length@pd; rots = Table[0, {2 n}];
  xs = Cases[pd, x_X := {Xp[x[[4]], x[[1]] PositiveQ@x,
    {Xm[x[[2]], x[[1]] True}}];
  For[k = 1, k ≤ 2 n, ++k,
    If[FreeQ[front, -k],
      front = Flatten@Replace[front, k → (xs /. {
        Xp[k, L_] | Xm[L_, k] := {L + 1, k + 1, -L},
        Xp[L_, k] | Xm[k, L_] := (++rots[[L]]; {-L, k + 1, L + 1}),
        _Xp | _Xm := {}
      }), {1}],
      Cases[front, k | -k] /. {k, -k} := --rots[[k]];
    ]
  ];
  RVK[xs, rots] ];
RVK[K_] := RVK[PD[K]];

```

```

In[ ]:= rot_i[n_] := (*rot_i[n] = *) 
$$\begin{cases} \eta_i & n = 0 \\ C_{\$} \text{rot}_i[n-1] // m_{i, \$ \rightarrow i} & n > 0 \\ \bar{C}_{\$} \text{rot}_i[n+1] // m_{i, \$ \rightarrow i} & n < 0 \end{cases}$$


```

```

In[ ]:= Z[K_] := Z[RVK@K];
Z[rvk_RVK] := Module[{g, done, st, c, x, i, j, k},
  g = 1; done = {}; st = Range[2 Length[rvk[[1]]];
  Do[
    {i, j} = List@@c;
    x = c /. {_Xp := R_{i,j}, _Xm := R_{i,j}};
    Do[x = (rot_0[rvk[[2, k]]] x) // m_{0,k \to k}, {k, {i, j}}];
    g *= x;
    Do[
      If[MemberQ[done, k + 1], g = g // m_{k,k+1 \to k}; st = st /. k + 1 → k];
      If[MemberQ[done, k - 1], g = g // m_{st[[k-1],k \to st[[k-1]]}; st = st /. k → st[[k-1]],
        {k, {i, j}}];
      done = done ∪ {i, j},
      {c, rvk[[1]]}
    ];
    Factor@g
  ]

```

```

In[ ]:= ZF[K_] := Z@ThinPosition@K;

```

```

In[ ]:= $k=1;

```

```
In[ ]:= CCF[ $\mathcal{E}$ _] := ExpandDenominator@ExpandNumerator@Together[ $\mathcal{E}$ ];
```

```
In[ ]:= CF[ $\mathcal{E}$ _List] := CF /@  $\mathcal{E}$ ;
CF[ $\mathcal{E}$ _eSeries] := CF /@  $\mathcal{E}$ ;
CF[ $\mathcal{E}$ _] := Module[
  {vs = Cases[ $\mathcal{E}$ , (p | x |  $\pi$  |  $\xi$ )_ ,  $\infty$ ]  $\cup$  {p | x |  $\pi$  |  $\xi$ }},
  Total[CoefficientRules[Expand[ $\mathcal{E}$ ], vs] /. (ps_ -> c_)  $\Rightarrow$  CCF[c] (Times @@ vsps)
];
CF[ $\mathcal{E}$ _E] := CF /@  $\mathcal{E}$ ;
CF[ $\gamma$ _I] := CF /@  $\gamma$ ;
CF[Esp[_][ $\mathcal{E}$ S_____]] := CF /@ Esp[ $\mathcal{E}$ S];
```

```
In[ ]:= eSeries /: S1_eSeries  $\equiv$  S2_eSeries :=
  Length[S1] == Length[S2]  $\wedge$  Inner[CF[#1] == CF[#2] &, S1, S2, And];
eSeries[0] := eSeries @@ Table[0, {k, 1};
eSeries /: S1_eSeries + S2_eSeries :=
  eSeries @@ Table[S1[[k]] + S2[[k]], {k, Min[Length@S1, Length@S2]};
eSeries /: S1_eSeries * S2_eSeries := eSeries @@
  Table[Sum[S1[[j + 1]] * S2[[k - j + 1]], {j, 0, k}], {k, 0, Min[Length@S1, Length@S2] - 1};
eSeries /: c_ * S_eSeries := (c #) & /@ S;
eSeries /:  $\partial_{vs}$  S_eSeries := (s  $\mapsto$   $\partial_{vs}$  s) /@ S;
```

```
In[ ]:= {p*, x*,  $\pi$ *,  $\xi$ *} = { $\pi$ ,  $\xi$ , p, x};
(vs_List)* := (v  $\mapsto$  v*) /@ vs;
(u_i)* := (u*)i;
```

```
In[ ]:= E /: E[ $\omega$ 1_, Q1_, P1_]  $\equiv$  E[ $\omega$ 2_, Q2_, P2_] := CF[ $\omega$ 1 ==  $\omega$ 2]  $\wedge$  CF[Q1 == Q2]  $\wedge$  (P1  $\equiv$  P2);
E /: E[ $\omega$ 1_, Q1_, P1_] E[ $\omega$ 2_, Q2_, P2_] := E[ $\omega$ 1  $\omega$ 2, Q1 + Q2, P1 + P2];
Ed1 -> r1[ $\mathcal{E}$ 1S_____]  $\equiv$  Ed2 -> r2[ $\mathcal{E}$ 2S_____] ^:= (d1 == d2)  $\wedge$  (r1 == r2)  $\wedge$  (E[ $\mathcal{E}$ 1S]  $\equiv$  E[ $\mathcal{E}$ 2S]);
Ed1 -> r1[ $\mathcal{E}$ 1S_____] Ed2 -> r2[ $\mathcal{E}$ 2S_____] ^:= E[(d1  $\cup$  d2) -> (r1  $\cup$  r2)] @@ (E[ $\mathcal{E}$ 1S] E[ $\mathcal{E}$ 2S]);
```

```
In[ ]:= Zip1_{ } = Identity;
Zip1vs_ @ <mathcal{F}_, E[ $\omega$ _, Q_, P_] > := Module[{I, F, G, u, v},
  I = IdentityMatrix@Length@vs;
  F = Table[ $\partial_{u,v}$   $\mathcal{F}$ , {u, vs*}, {v, vs*}];
  G = Table[ $\partial_{u,v}$  Q, {u, vs}, {v, vs}];
  CF /@ <
    vs* . F . Inverse[I - G . F] . vs* / 2,
    E[PowerExpand@Factor[ $\omega$  Det[I - G . F]-1/2], Q - vs . G . vs / 2, P]
  >
];
```

```
In[ ]:= Zip2_{ } = Identity;
Zip2_{vs_} @ <mathcal{F}_-, \mathbb{E}[\omega_-, Q_-, P_-]> := Module[{F, Y, u, v},
  F = Table[\partial_{u,v} \mathcal{F}, {u, vs*}, {v, vs*}];
  Y = Table[\partial_v Q, {v, vs*}];
  CF / @ <mathcal{F}, \mathbb{E}[\omega, Q - Y.vs + Y.F.Y / 2, P /. Thread[vs \to vs + F.Y]]>
]
```

```
In[ ]:= Zip3_{vs_} @ <mathcal{F}_-, \mathbb{E}[\omega_-, Q_-, P_-]> := Module[{Z, u, v, m, j},
  Z[0] = P;
  For[m = 0, m < 2 $k, ++m,
    Z[m + 1] = CF [
      
$$\frac{1}{2(m+1)}$$

      Sum[\partial_{u,v} \mathcal{F} (\partial_{u,v} Z[m] + Sum[(\partial_u Z[j]) (\partial_v Z[m - j]), {j, 0, m}]), {u, vs}, {v, vs*}]
    ];
  \mathbb{E}[\omega, Q, CF[Sum[Z[m], {m, 0, 2 $k}] /. Table[v \to 0, {v, vs}]]]
]
```

```
In[ ]:= Zip_{vs_} [\mathcal{F}_-, \mathcal{E}_-] := <mathcal{F}, \mathcal{E}> // Zip1_{vs} // Zip2_{vs} // Zip3_{vs}
```

```
In[ ]:= \mathbb{E}_{d1 \to r1} [\mathcal{E}1s\_ ] // \mathbb{E}_{d2 \to r2} [\mathcal{E}2s\_ ] := Module[{is = r1 \cap d2, lvs},
  lvs = Flatten@Table[{x_{\$i}, p_{\$i}}, {i, is}];
  \mathbb{E}_{(d1 \cup \text{Complement}[d2, is]) \to (r2 \cup \text{Complement}[r1, is])} @@ (Zip_{lvs \cup lvs*} [lvs*.lvs, Times[
    \mathbb{E}[\mathcal{E}1s] /. Table[(v : x | p)_i \to v_{\$i}, {i, is}],
    \mathbb{E}[\mathcal{E}2s] /. Table[(v : \xi | \pi)_i \to v_{\$i}, {i, is}]
  ]])
]
```

```
In[ ]:= \eta_{i_-} := \mathbb{E}_{\{i\} \to \{i\}} [1, 0, eSeries[0]];
m_{i_-, j_ \to k_-} := \mathbb{E}_{\{i, j\} \to \{k\}} [1, -\xi_i \pi_j + (\pi_i + \pi_j) p_k + (\xi_i + \xi_j) x_k, eSeries[0]]
```

```
In[ ]:= AllMonomials[{}, 0] = {1};
AllMonomials[{}, d_Integer] /; d > 0 := {};
AllMonomials[{v_-, vs_--}, d_Integer] :=
  Join @@ Table[v^{d-k} AllMonomials[{vs}, k], {k, 0, d}];
AllMonomials[vs_List, {d_}] := Join @@ Table[AllMonomials[vs, k], {k, 0, d}];
```

```
In[ ]:= Basis[js_List, m_] := Flatten@Outer[Times,
  AllMonomials[Table[p_j, {j, js}], m], AllMonomials[Table[x_j, {j, js}], m]];
Basis[js_List, {m_}] := Flatten@Table[Basis[js, k], {k, 0, m}]
```

```
In[ ]:= GenericCombination[bas_, c_] := bas.Table[c_j, {j, Length@bas}];
GenericCombination[bas_, c_k_] := bas.Table[c_{k,j}, {j, Length@bas}];
```

```
In[ ]:= R0_{i,j}_ := E_{i,j} [T^{1/2}, (T - 1) (p_i - p_j) x_j, eSeries @@ Table[0, {k + 1}];
Rp_{i,j}_ := E_{i,j} [1, 0,
  eSeries @@ Prepend[0] @ Table[GenericCombination[Basis[{i, j}, {k + 1}], c_k], {k, $k}]];
R_{i,j}_ := Module[{i1, j1}, Rp_{i1,j1} R0_{i,j} // m_{i1,i} // m_{j1,j}];
```

```
In[ ]:= R0_{i,j}_ := E_{i,j} [T^{-1/2}, (T^{-1} - 1) (p_i - p_j) x_j, eSeries @@ Table[0, {k + 1}];
Rp_{i,j}_ := E_{i,j} [1, 0,
  eSeries @@ Prepend[0] @ Table[GenericCombination[Basis[{i, j}, {k + 1}], d_k], {k, $k}]];
R_{i,j}_ := Module[{i1, j1}, Rp_{i1,j1} R0_{i,j} // m_{i1,i} // m_{j1,j}];
```

```
In[ ]:= C_{i}_ := E_{i} [T^{1/2}, 0,
  eSeries @@ Prepend[0] @ Table[GenericCombination[Basis[{i}, {k + 1}], e_k], {k, $k}]];
C_{i}_ := E_{i} [T^{-1/2}, 0,
  eSeries @@ Prepend[0] @ Table[GenericCombination[Basis[{i}, {k + 1}], f_k], {k, $k}]];
```

In[*]:= CF /@ {R_{1,2}, R̄_{1,2}, C₁, C̄₁}

Out[*]:= {E_{{1}→{1,2}} [√T, (-1+T) p₁ x₂ + (1-T) p₂ x₂,

∈Series [0, c_{1,1} + p₁ x₁ c_{1,2} + p₁ x₂ (c_{1,2} - T c_{1,2} + T c_{1,3}) + p₂ x₁ c_{1,4} +
 p₂ x₂ (c_{1,4} - T c_{1,4} + T c_{1,5}) + p₁² x₁² c_{1,6} + p₁² x₁ x₂ (2 c_{1,6} - 2 T c_{1,6} + T c_{1,7}) +
 p₁² x₂² (c_{1,6} - 2 T c_{1,6} + T² c_{1,6} + T c_{1,7} - T² c_{1,7} + T² c_{1,8}) + p₁ p₂ x₁² c_{1,9} +
 p₁ p₂ x₁ x₂ (2 c_{1,9} - 2 T c_{1,9} + T c_{1,10}) + p₁ p₂ x₂² (c_{1,9} - 2 T c_{1,9} + T² c_{1,9} + T c_{1,10} - T² c_{1,10} + T² c_{1,11}) +
 p₂² x₁² c_{1,12} + p₂² x₁ x₂ (2 c_{1,12} - 2 T c_{1,12} + T c_{1,13}) +
 p₂² x₂² (c_{1,12} - 2 T c_{1,12} + T² c_{1,12} + T c_{1,13} - T² c_{1,13} + T² c_{1,14})]] ,

E_{{1}→{1,2}} [$\frac{1}{\sqrt{T}}$, $\frac{(1-T) p_1 x_2}{T}$ + $\frac{(-1+T) p_2 x_2}{T}$,

∈Series [0, d_{1,1} + p₁ x₁ d_{1,2} + $\frac{p_1 x_2 (-d_{1,2} + T d_{1,2} + d_{1,3})}{T}$ + p₂ x₁ d_{1,4} + $\frac{p_2 x_2 (-d_{1,4} + T d_{1,4} + d_{1,5})}{T}$ +
 p₁² x₁² d_{1,6} + $\frac{p_1^2 x_1 x_2 (-2 d_{1,6} + 2 T d_{1,6} + d_{1,7})}{T}$ + $\frac{p_1^2 x_2^2 (d_{1,6} - 2 T d_{1,6} + T^2 d_{1,6} - d_{1,7} + T d_{1,7} + d_{1,8})}{T^2}$ +
 p₁ p₂ x₁² d_{1,9} + $\frac{p_1 p_2 x_1 x_2 (-2 d_{1,9} + 2 T d_{1,9} + d_{1,10})}{T}$ +
 $\frac{p_1 p_2 x_2^2 (d_{1,9} - 2 T d_{1,9} + T^2 d_{1,9} - d_{1,10} + T d_{1,10} + d_{1,11})}{T^2}$ + p₂² x₁² d_{1,12} +
 $\frac{p_2^2 x_1 x_2 (-2 d_{1,12} + 2 T d_{1,12} + d_{1,13})}{T}$ + $\frac{p_2^2 x_2^2 (d_{1,12} - 2 T d_{1,12} + T^2 d_{1,12} - d_{1,13} + T d_{1,13} + d_{1,14})}{T^2}$]] ,

E_{{1}→{1}} [√T, 0, ∈Series [0, e_{1,1} + p₁ x₁ e_{1,2} + p₁² x₁² e_{1,3}]] ,

E_{{1}→{1}} [$\frac{1}{\sqrt{T}}$, 0, ∈Series [0, f_{1,1} + p₁ x₁ f_{1,2} + p₁² x₁² f_{1,3}]] }

In[*]:= RMoves := {

(R_{1,2} R_{4,3} R_{5,6} // m_{1,4→1} // m_{2,5→2} // m_{3,6→3}) ≡ (R_{2,3} R_{4,5} R_{1,6} // m_{1,4→1} // m_{2,5→2} // m_{3,6→3}) ,

(R_{1,2} R̄_{3,4} // m_{1,3→1} // m_{2,4→2}) ≡ (η₁ η₂) ,

(C₁ C̄₂ // m_{1,2→1}) ≡ η₁ ,

(R_{1,4} R̄_{5,2} C̄₃ // m_{2,4→2} // m_{1,3→1} // m_{1,5→1}) ≡ C̄₁ η₂ ,

(C₃ R_{1,2} // m_{2,3→2} // m_{2,1→1}) ≡ (C̄₃ R_{1,2} // m_{1,3→1} // m_{1,2→1}) ,

(C̄₂ R_{1,3} // m_{1,2→1} // m_{1,3→1}) ≡ η₁ , (C̄₂ R̄_{3,1} // m_{1,2→1} // m_{1,3→1}) ≡ η₁ ,

(C₂ R̄_{1,3} // m_{1,2→1} // m_{1,3→1}) ≡ η₁ , (C₂ R_{3,1} // m_{1,2→1} // m_{1,3→1}) ≡ η₁

}

In[*]:= Short [RMoves, 10]

Out[*]//Short=

$$\begin{aligned} & \{ 3 c_{1,1} + 2 p_1 x_1 c_{1,2} + p_2 x_1 c_{1,4} + p_3 x_1 c_{1,4} + \ll 34 \gg + \\ & p_2^2 x_3^2 (T^2 c_{1,6} - 2 T^3 c_{1,6} + T^4 c_{1,6} + T^3 c_{1,7} - T^4 c_{1,7} + T^4 c_{1,8} + c_{1,12} - 2 T c_{1,12} + \\ & T^2 c_{1,12} + T c_{1,13} - 2 T^2 c_{1,13} + T^3 c_{1,13} + T^2 c_{1,14} - 2 T^3 c_{1,14} + T^4 c_{1,14}) + \\ & p_1^2 x_3^2 (2 c_{1,6} - 6 T c_{1,6} + 8 T^2 c_{1,6} - 6 T^3 c_{1,6} + 2 T^4 c_{1,6} + 2 T c_{1,7} - 5 T^2 c_{1,7} + 5 T^3 c_{1,7} - \\ & 2 T^4 c_{1,7} + 2 T^2 c_{1,8} - 4 T^3 c_{1,8} + 3 T^4 c_{1,8} + c_{1,9} - 4 T c_{1,9} + 6 T^2 c_{1,9} - 4 T^3 c_{1,9} + T^4 c_{1,9} + T c_{1,10} - \\ & 3 T^2 c_{1,10} + 3 T^3 c_{1,10} - T^4 c_{1,10} + T^2 c_{1,11} - 2 T^3 c_{1,11} + T^4 c_{1,11} + c_{1,12} - 4 T c_{1,12} + 6 T^2 c_{1,12} - \\ & 4 T^3 c_{1,12} + T^4 c_{1,12} + T c_{1,13} - 3 T^2 c_{1,13} + 3 T^3 c_{1,13} - T^4 c_{1,13} + T^2 c_{1,14} - 2 T^3 c_{1,14} + T^4 c_{1,14}) + \\ & p_3^2 x_3^2 (2 T^2 c_{1,12} - 4 T^3 c_{1,12} + 2 T^4 c_{1,12} + 2 T^3 c_{1,13} - 2 T^4 c_{1,13} + 2 T^4 c_{1,14}) = \\ & 3 c_{1,1} + 2 p_1 x_1 c_{1,2} + p_1 x_2 (\ll 1 \gg) + \ll 41 \gg + p_2^2 x_3^2 (\ll 1 \gg) + p_3^2 x_3^2 (\ll 1 \gg), \\ & \ll 7 \gg, \ll 1 \gg \} \end{aligned}$$

Solving for R, C, \$k = 1

In[*]:= \$k = 1;

{R1,2, C1}

unknowns = Cases [{R1,2, R1,2, C1, C1}, (c | d | e | f) \$k,_, infinity] // Union

$$\begin{aligned} \text{Out[*]} = & \{ E_{\{ \} \rightarrow \{1,2\}} [\sqrt{T}, (-1 + T) p_1 x_2 + (1 - T) p_2 x_2, \\ & \in \text{Series} [\theta, c_{1,1} + p_1 x_1 c_{1,2} + p_1 x_2 (c_{1,2} - T c_{1,2} + T c_{1,3}) + p_2 x_1 c_{1,4} + \\ & p_2 x_2 (c_{1,4} - T c_{1,4} + T c_{1,5}) + p_1^2 x_1^2 c_{1,6} + p_1^2 x_1 x_2 (2 c_{1,6} - 2 T c_{1,6} + T c_{1,7}) + \\ & p_1^2 x_2^2 (c_{1,6} - 2 T c_{1,6} + T^2 c_{1,6} + T c_{1,7} - T^2 c_{1,7} + T^2 c_{1,8}) + p_1 p_2 x_1^2 c_{1,9} + \\ & p_1 p_2 x_1 x_2 (2 c_{1,9} - 2 T c_{1,9} + T c_{1,10}) + p_1 p_2 x_2^2 (c_{1,9} - 2 T c_{1,9} + T^2 c_{1,9} + T c_{1,10} - T^2 c_{1,10} + T^2 c_{1,11}) + \\ & p_2^2 x_1^2 c_{1,12} + p_2^2 x_1 x_2 (2 c_{1,12} - 2 T c_{1,12} + T c_{1,13}) + \\ & p_2^2 x_2^2 (c_{1,12} - 2 T c_{1,12} + T^2 c_{1,12} + T c_{1,13} - T^2 c_{1,13} + T^2 c_{1,14})]] , \\ & E_{\{ \} \rightarrow \{1\}} [\sqrt{T}, \theta, \in \text{Series} [\theta, e_{1,1} + p_1 x_1 e_{1,2} + p_1^2 x_1^2 e_{1,3}]]] \} \end{aligned}$$

Out[*] = {c1,1, c1,2, c1,3, c1,4, c1,5, c1,6, c1,7, c1,8, c1,9, c1,10, c1,11, c1,12, c1,13, c1,14, d1,1, d1,2, d1,3, d1,4, d1,5, d1,6, d1,7, d1,8, d1,9, d1,10, d1,11, d1,12, d1,13, d1,14, e1,1, e1,2, e1,3, f1,1, f1,2, f1,3}

In[]:= Short [errors = CCF /@ Cases [RMoves, a_ == b_ => a - b], 25]

Out[]//Short=

$$\left\{ \begin{aligned} & p_1 x_3 c_{1,2} - T p_1 x_3 c_{1,2} + T p_1 x_3 c_{1,3} - T^2 p_1 x_3 c_{1,3} - p_2 x_1 c_{1,4} + T p_2 x_1 c_{1,4} + p_3 x_1 c_{1,4} - T p_3 x_1 c_{1,4} + \\ & p_1 x_2 c_{1,4} - T p_1 x_2 c_{1,4} - p_2 x_2 c_{1,4} + 2 T p_2 x_2 c_{1,4} - T^2 p_2 x_2 c_{1,4} - T p_3 x_2 c_{1,4} + T^2 p_3 x_2 c_{1,4} + \\ & p_1 x_3 c_{1,4} - 2 T p_1 x_3 c_{1,4} + T^2 p_1 x_3 c_{1,4} + T p_2 x_3 c_{1,4} - T^2 p_2 x_3 c_{1,4} + T p_1 x_3 c_{1,5} - T^2 p_1 x_3 c_{1,5} - \\ & 2 p_1^2 x_1 x_2 c_{1,6} + 2 T p_1^2 x_1 x_2 c_{1,6} + 2 T p_1 p_2 x_2^2 c_{1,6} - 2 T^2 p_1 p_2 x_2^2 c_{1,6} + 2 T p_1^2 x_1 x_3 c_{1,6} - \\ & 2 T^2 p_1^2 x_1 x_3 c_{1,6} + 2 p_1^2 x_2 x_3 c_{1,6} - 6 T p_1^2 x_2 x_3 c_{1,6} + 6 T^2 p_1^2 x_2 x_3 c_{1,6} - 2 T^3 p_1^2 x_2 x_3 c_{1,6} + \\ & 4 T p_1 p_2 x_2 x_3 c_{1,6} - 8 T^2 p_1 p_2 x_2 x_3 c_{1,6} + 4 T^3 p_1 p_2 x_2 x_3 c_{1,6} + p_1^2 x_3^2 c_{1,6} - 4 T p_1^2 x_3^2 c_{1,6} + \\ & 7 T^2 p_1^2 x_3^2 c_{1,6} - 6 T^3 p_1^2 x_3^2 c_{1,6} + 2 T^4 p_1^2 x_3^2 c_{1,6} + 2 T p_1 p_2 x_3^2 c_{1,6} - 6 T^2 p_1 p_2 x_3^2 c_{1,6} + 6 T^3 p_1 p_2 x_3^2 c_{1,6} - \\ & 2 T^4 p_1 p_2 x_3^2 c_{1,6} + 2 T p_1^2 x_2 x_3 c_{1,7} - 4 T^2 p_1^2 x_2 x_3 c_{1,7} + 2 T^3 p_1^2 x_2 x_3 c_{1,7} + \ll 207 \gg + 6 T^3 p_1 p_3 x_3^2 c_{1,12} - \\ & 2 T^4 p_1 p_3 x_3^2 c_{1,12} - 2 T p_2 p_3 x_3^2 c_{1,12} + 6 T^2 p_2 p_3 x_3^2 c_{1,12} - 6 T^3 p_2 p_3 x_3^2 c_{1,12} + 2 T^4 p_2 p_3 x_3^2 c_{1,12} + \\ & T^2 p_2^2 x_1 x_3 c_{1,13} - T^3 p_2^2 x_1 x_3 c_{1,13} - 2 T^2 p_2 p_3 x_1 x_3 c_{1,13} + 2 T^3 p_2 p_3 x_1 x_3 c_{1,13} + T^2 p_2^2 x_1 x_3 c_{1,13} - \\ & T^3 p_2^2 x_1 x_3 c_{1,13} + T p_1^2 x_2 x_3 c_{1,13} - 2 T^2 p_1^2 x_2 x_3 c_{1,13} + T^3 p_1^2 x_2 x_3 c_{1,13} + T p_2^2 x_2 x_3 c_{1,13} - \\ & 2 T^3 p_2^2 x_2 x_3 c_{1,13} + T^4 p_2^2 x_2 x_3 c_{1,13} + 2 T^2 p_1 p_3 x_2 x_3 c_{1,13} - 2 T^3 p_1 p_3 x_2 x_3 c_{1,13} - 2 T^2 p_2 p_3 x_2 x_3 c_{1,13} + \\ & 4 T^3 p_2 p_3 x_2 x_3 c_{1,13} - 2 T^4 p_2 p_3 x_2 x_3 c_{1,13} - T^3 p_3^2 x_2 x_3 c_{1,13} + T^4 p_3^2 x_2 x_3 c_{1,13} + T p_1^2 x_3^2 c_{1,13} - \\ & 3 T^2 p_1^2 x_3^2 c_{1,13} + 3 T^3 p_1^2 x_3^2 c_{1,13} - T^4 p_1^2 x_3^2 c_{1,13} + T^2 p_2^2 x_3^2 c_{1,13} - 2 T^3 p_2^2 x_3^2 c_{1,13} + T^4 p_2^2 x_3^2 c_{1,13} + \\ & 2 T^2 p_1 p_3 x_3^2 c_{1,13} - 4 T^3 p_1 p_3 x_3^2 c_{1,13} + 2 T^4 p_1 p_3 x_3^2 c_{1,13} - 2 T^2 p_2 p_3 x_3^2 c_{1,13} + 4 T^3 p_2 p_3 x_3^2 c_{1,13} - \\ & 2 T^4 p_2 p_3 x_3^2 c_{1,13} + 2 T^2 p_2^2 x_2 x_3 c_{1,14} - 2 T^3 p_2^2 x_2 x_3 c_{1,14} + T^2 p_1^2 x_3^2 c_{1,14} - 2 T^3 p_1^2 x_3^2 c_{1,14} + T^4 p_1^2 x_3^2 c_{1,14} + \\ & 2 T^3 p_1 p_3 x_3^2 c_{1,14} - 2 T^4 p_1 p_3 x_3^2 c_{1,14} - 2 T^3 p_2 p_3 x_3^2 c_{1,14} + 2 T^4 p_2 p_3 x_3^2 c_{1,14}, \ll 7 \gg, \left. \begin{aligned} & \ll 1 \gg \\ & \ll 1 \gg \end{aligned} \right\} \end{aligned}$$

In[]:= Short [

eqns =

Thread[0 == Union @@ (CoefficientRules[#, {x1, x2, x3, p1, p2, p3}][[; , 2] & /@ errors)], 10]

Out[]//Short=

$$\left\{ \begin{aligned} & \theta = c_{1,4} - T c_{1,4}, \theta = -c_{1,4} + T c_{1,4}, \theta = T c_{1,4} - T^2 c_{1,4}, \\ & \theta = -c_{1,4} + 2 T c_{1,4} - T^2 c_{1,4}, \theta = -T c_{1,4} + T^2 c_{1,4}, \ll 74 \gg, \\ & \theta = -c_{1,6} + \frac{c_{1,6}}{T^2} + \frac{c_{1,7}}{T} - T c_{1,7} + c_{1,8} - T^2 c_{1,8} - c_{1,9} + \frac{c_{1,9}}{T^2} + \frac{c_{1,10}}{T} - T c_{1,10} + \\ & c_{1,11} - T^2 c_{1,11} - c_{1,12} + \frac{c_{1,12}}{T^2} + \frac{c_{1,13}}{T} - T c_{1,13} + c_{1,14} - T^2 c_{1,14} + \frac{e_{1,3}}{T^2} - T^2 f_{1,3}, \\ & \theta = c_{1,6} + T c_{1,7} + T^2 c_{1,8} + c_{1,9} + T c_{1,10} + T^2 c_{1,11} + c_{1,12} + T c_{1,13} + T^2 c_{1,14} + T^2 f_{1,3}, \\ & \theta = T^2 d_{1,6} + T d_{1,7} + d_{1,8} + T^2 d_{1,9} + T d_{1,10} + d_{1,11} + T^2 d_{1,12} + T d_{1,13} + d_{1,14} + T^2 f_{1,3}, \\ & \theta = T^2 c_{1,8} - T c_{1,11} + T^2 c_{1,11} + c_{1,14} - 2 T c_{1,14} + T^2 c_{1,14} + d_{1,6} - 2 T d_{1,6} + T^2 d_{1,6} - d_{1,7} + \\ & T d_{1,7} + d_{1,8} + f_{1,3} - 2 T f_{1,3} + T^2 f_{1,3}, \theta = d_{1,1} + d_{1,2} - T d_{1,2} - d_{1,3} + 2 d_{1,6} - 4 T d_{1,6} + \\ & 2 T^2 d_{1,6} - 2 d_{1,7} + 2 T d_{1,7} + 2 d_{1,8} + f_{1,1} + f_{1,2} - T f_{1,2} + 2 f_{1,3} - 4 T f_{1,3} + 2 T^2 f_{1,3} \end{aligned} \right\}$$

In[*]:= **{sol} = Solve[eqns, unknowns]**

Solve: Equations may not give solutions for all "solve" variables.

$$\text{Out[*]} = \left\{ \left\{ \begin{aligned}
 c_{1,1} &\rightarrow -\frac{c_{1,2}}{2} - \frac{c_{1,5}}{2}, c_{1,3} \rightarrow -\frac{c_{1,2}}{T} - c_{1,5}, c_{1,4} \rightarrow \theta, c_{1,6} \rightarrow \theta, c_{1,8} \rightarrow -\frac{(1-T)c_{1,7}}{T} - \frac{(1-T)c_{1,10}}{2T}, \\
 c_{1,9} &\rightarrow \theta, c_{1,11} \rightarrow -c_{1,7} - \frac{(1+T)c_{1,10}}{2T}, c_{1,12} \rightarrow \theta, c_{1,13} \rightarrow \theta, c_{1,14} \rightarrow \theta, \\
 d_{1,1} &\rightarrow \frac{c_{1,2}}{2} + \frac{c_{1,5}}{2}, d_{1,2} \rightarrow -c_{1,2}, d_{1,3} \rightarrow Tc_{1,2} + c_{1,5}, d_{1,4} \rightarrow \theta, d_{1,5} \rightarrow -c_{1,5}, d_{1,6} \rightarrow \theta, \\
 d_{1,7} &\rightarrow -Tc_{1,7} - (-1+T)c_{1,10}, d_{1,8} \rightarrow -\left((T-T^2)c_{1,7}\right) - \frac{1}{2}(-1+3T-2T^2)c_{1,10}, \\
 d_{1,9} &\rightarrow \theta, d_{1,10} \rightarrow -c_{1,10}, d_{1,11} \rightarrow Tc_{1,7} - \frac{1}{2}(1-3T)c_{1,10}, d_{1,12} \rightarrow \theta, d_{1,13} \rightarrow \theta, d_{1,14} \rightarrow \theta, \\
 e_{1,1} &\rightarrow -\frac{c_{1,2}}{2} - \frac{c_{1,5}}{2}, e_{1,2} \rightarrow -c_{1,10}, e_{1,3} \rightarrow \theta, f_{1,1} \rightarrow \frac{c_{1,2}}{2} + \frac{c_{1,5}}{2}, f_{1,2} \rightarrow c_{1,10}, f_{1,3} \rightarrow \theta \end{aligned} \right\} \right\}$$

In[*]:= **sol /. (a_ -> b_) :-> (a = b)**

$$\text{Out[*]} = \left\{ -\frac{c_{1,2}}{2} - \frac{c_{1,5}}{2}, -\frac{c_{1,2}}{T} - c_{1,5}, \theta, \theta, -\frac{(1-T)c_{1,7}}{T} - \frac{(1-T)c_{1,10}}{2T}, \theta, \right. \\
 \left. -c_{1,7} - \frac{(1+T)c_{1,10}}{2T}, \theta, \theta, \theta, \frac{c_{1,2}}{2} + \frac{c_{1,5}}{2}, -c_{1,2}, Tc_{1,2} + c_{1,5}, \theta, -c_{1,5}, \theta, \right. \\
 \left. -Tc_{1,7} - (-1+T)c_{1,10}, -\left((T-T^2)c_{1,7}\right) - \frac{1}{2}(-1+3T-2T^2)c_{1,10}, \theta, -c_{1,10}, \right. \\
 \left. Tc_{1,7} - \frac{1}{2}(1-3T)c_{1,10}, \theta, \theta, \theta, -\frac{c_{1,2}}{2} - \frac{c_{1,5}}{2}, -c_{1,10}, \theta, \frac{c_{1,2}}{2} + \frac{c_{1,5}}{2}, c_{1,10}, \theta \right\}$$

In[*]:= **CF /@ {Rp_{1,2}, R̄p_{1,2}, C₁, C̄₁}**

$$\text{Out[*]} = \left\{ \begin{aligned}
 &E_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \right. \\
 &\quad \in \text{Series} \left[\theta, p_1 x_1 c_{1,2} + \frac{1}{2}(-c_{1,2} - c_{1,5}) + p_2 x_2 c_{1,5} + \frac{p_1 x_2 (-c_{1,2} - Tc_{1,5})}{T} + p_1^2 x_1 x_2 c_{1,7} + \right. \\
 &\quad \left. p_1 p_2 x_1 x_2 c_{1,10} + \frac{p_1 p_2 x_2^2 (-2Tc_{1,7} - c_{1,10} - Tc_{1,10})}{2T} + \frac{p_1^2 x_2^2 (-2c_{1,7} + 2Tc_{1,7} - c_{1,10} + Tc_{1,10})}{2T} \right], \\
 &E_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, -p_1 x_1 c_{1,2} - p_2 x_2 c_{1,5} + \frac{1}{2}(c_{1,2} + c_{1,5}) + p_1 x_2 (Tc_{1,2} + c_{1,5}) - \right. \right. \\
 &\quad \left. p_1 p_2 x_1 x_2 c_{1,10} + p_1^2 x_1 x_2 (-Tc_{1,7} + c_{1,10} - Tc_{1,10}) + \frac{1}{2} p_1 p_2 x_2^2 (2Tc_{1,7} - c_{1,10} + 3Tc_{1,10}) + \right. \\
 &\quad \left. \frac{1}{2} p_1^2 x_2^2 (-2Tc_{1,7} + 2T^2 c_{1,7} + c_{1,10} - 3Tc_{1,10} + 2T^2 c_{1,10}) \right], \\
 &E_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{1}{2}(-c_{1,2} - c_{1,5}) - p_1 x_1 c_{1,10} \right], \right. \\
 &E_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, \theta, \in \text{Series} \left[\theta, \frac{1}{2}(c_{1,2} + c_{1,5}) + p_1 x_1 c_{1,10} \right] \right] \left. \right\}
 \end{aligned}$$

In[*]:= **Factor** /@ **CF** [**Last**@**ZF**@**Knot** [**6**, **1**] - **Last**@**ZF**@**Knot** [**9**, **46**]]

KnotTheory: Loading precomputed data in PD4Knots`.

Out[*]:= $\in \text{Series} \left[\theta, \frac{2(-1+T)^2(1-4T+T^2)c_{1,10}}{(-2+T)^2(-1+2T)^2} \right]$

In[*]:= **Cases** [{**Rp**_{1,2}, **Rp**_{1,2}, **C**₁, **C**₁ }, (**c** | **d** | **e** | **f**)_{\$k,_}, ∞] // **Union**

Out[*]:= { **C**_{1,2}, **C**_{1,5}, **C**_{1,7}, **C**_{1,10} }

In[*]:= **CF** /@ ({**Rp**_{1,2}, **Rp**_{1,2}, **C**₁, **C**₁ } / . { **c**_{1,10} → -1/2, **c**_{1,2} → θ , **c**_{1,5} → θ })

Out[*]:= $\left\{ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, \right. \right. \right. \\ \left. \left. \left. -\frac{1}{2} p_1 p_2 x_1 x_2 + p_1^2 x_1 x_2 c_{1,7} + \frac{p_1 p_2 x_2^2 (1+T-4T c_{1,7})}{4T} + \frac{p_1^2 x_2^2 (1-T-4 c_{1,7}+4T c_{1,7})}{4T} \right] \right], \right. \\ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{1}{2} p_1^2 x_1 x_2 (-1+T-2T c_{1,7}) + \right. \right. \\ \left. \left. \frac{1}{4} p_1 p_2 x_2^2 (1-3T+4T c_{1,7}) + \frac{1}{4} p_1^2 x_2^2 (-1+3T-2T^2-4T c_{1,7}+4T^2 c_{1,7}) \right] \right], \\ \left. \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2} \right] \right], \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1 x_1 \right] \right] \right\}$

In[*]:= **CF** /@ ({**Rp**_{1,2}, **Rp**_{1,2}, **C**₁, **C**₁ } / . { **c**_{1,10} → -1/2, **c**_{1,2} → θ , **c**_{1,5} → θ , **c**_{1,7} → 1/2 })

Out[*]:= $\left\{ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, \frac{1}{2} p_1^2 x_1 x_2 - \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{(-1+T) p_1^2 x_2^2}{4T} + \frac{(1-T) p_1 p_2 x_2^2}{4T} \right] \right], \right. \\ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1^2 x_1 x_2 + \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{1}{4} (-1+T) p_1^2 x_2^2 + \frac{1}{4} (1-T) p_1 p_2 x_2^2 \right] \right], \\ \left. \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2} \right] \right], \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1 x_1 \right] \right] \right\}$

In[*]:= { **c**_{1,10} = -1/2, **c**_{1,2} = θ , **c**_{1,5} = θ , **c**_{1,7} = 1/2 };

CF /@ { **R**_{1,2}, **R**_{1,2}, **C**₁, **C**₁ }

Out[*]:= $\left\{ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[\sqrt{T}, (-1+T) p_1 x_2 + (1-T) p_2 x_2, \right. \right. \\ \left. \left. \in \text{Series} \left[\theta, \frac{1}{2} T p_1^2 x_1 x_2 - \frac{1}{2} T p_1 p_2 x_1 x_2 + \frac{1}{4} (T-T^2) p_1^2 x_2^2 + \frac{1}{4} (-T+T^2) p_1 p_2 x_2^2 \right] \right], \right. \\ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[\frac{1}{\sqrt{T}}, \frac{(1-T) p_1 x_2}{T} + \frac{(-1+T) p_2 x_2}{T}, \right. \\ \left. \in \text{Series} \left[\theta, -\frac{p_1^2 x_1 x_2}{2T} + \frac{p_1 p_2 x_1 x_2}{2T} + \frac{(1-T) p_1^2 x_2^2}{4T^2} + \frac{(-1+T) p_1 p_2 x_2^2}{4T^2} \right] \right], \\ \left. \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2} \right] \right], \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1 x_1 \right] \right] \right\}$

$$\text{In[*]} := \text{CF}[\mathbf{R}_{1,2} / \cdot \mathbf{T} \rightarrow \mathbf{T}^{-1}]$$

$$\text{Out[*]} = \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[\sqrt{\frac{1}{\mathbf{T}}}, \frac{(1-\mathbf{T}) p_1 x_2}{\mathbf{T}} + \frac{(-1+\mathbf{T}) p_2 x_2}{\mathbf{T}}, \right. \\ \left. \in \text{Series} \left[\mathbf{0}, \frac{p_1^2 x_1 x_2}{2 \mathbf{T}} - \frac{p_1 p_2 x_1 x_2}{2 \mathbf{T}} + \frac{(-1+\mathbf{T}) p_1^2 x_2^2}{4 \mathbf{T}^2} + \frac{(1-\mathbf{T}) p_1 p_2 x_2^2}{4 \mathbf{T}^2} \right] \right]$$

$$\text{In[*]} := \text{RMoves}$$

$$\text{Out[*]} = \{\text{True}, \text{True}, \text{True}, \text{True}, \text{True}, \text{True}, \text{True}, \text{True}, \text{True}\}$$

The isomorphism with Γ -calculus

$$\text{In[*]} := \Gamma[\mathbb{E}_{\{\} \rightarrow \text{is}}[\omega, \mathbf{Q}, _]] := \text{CF@}\Gamma[\omega^{-1}, \text{Sum}[p_i x_i, \{\mathbf{i}, \text{is}\}] - \mathbf{Q}] \\ \mathbb{E}[\Gamma[\omega, \mathbf{A}]] := \text{Module}[\{\text{is} = \text{Union@Cases}[\mathbf{A}, p_i \rightarrow \mathbf{i}, \infty]\}, \\ \text{CF@}\mathbb{E}_{\{\} \rightarrow \text{is}}[\omega^{-1}, \text{Sum}[p_i x_i, \{\mathbf{i}, \text{is}\}] - \mathbf{A}, \text{eSeries}[\mathbf{0}]]]$$

$$\text{In[*]} := \{\mathbf{R}_{i,j}, \mathbf{R}_{i,j} // \Gamma, \mathbf{R}_{i,j} // \Gamma // \mathbb{E}\} // \text{Column}$$

$$\mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\sqrt{\mathbf{T}}, (-1+\mathbf{T}) p_i x_j + (1-\mathbf{T}) p_j x_j, \right. \\ \left. \in \text{Series} \left[\mathbf{0}, \frac{1}{2} \mathbf{T} p_i^2 x_i x_j - \frac{1}{2} \mathbf{T} p_i p_j x_i x_j + \frac{1}{4} (\mathbf{T} - \mathbf{T}^2) p_i^2 x_j^2 + \frac{1}{4} (-\mathbf{T} + \mathbf{T}^2) p_i p_j x_j^2 \right] \right] \\ \text{Out[*]} = \Gamma \left[\frac{1}{\sqrt{\mathbf{T}}}, p_i x_i + (1-\mathbf{T}) p_i x_j + \mathbf{T} p_j x_j \right] \\ \mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\sqrt{\mathbf{T}}, (-1+\mathbf{T}) p_i x_j + (1-\mathbf{T}) p_j x_j, \in \text{Series}[\mathbf{0}, \mathbf{0}] \right]$$

$$\text{In[*]} := \gamma \mathbf{1} = \Gamma \left[\omega, \{x_i, x_j, x_r\} \cdot \begin{pmatrix} \alpha & \beta & \theta \\ \gamma & \delta & \epsilon \\ \phi & \psi & \xi \end{pmatrix} \cdot \{p_i, p_j, p_r\} \right] // \mathbb{E}$$

$$\text{Out[*]} = \mathbb{E}_{\{\} \rightarrow \{i,j,r\}} \left[\frac{1}{\omega}, (1-\alpha) p_i x_i - \beta p_j x_i - \theta p_r x_i - \gamma p_i x_j + \right. \\ \left. (1-\delta) p_j x_j - \epsilon p_r x_j - \phi p_i x_r - \psi p_j x_r + (1-\xi) p_r x_r, \in \text{Series}[\mathbf{0}, \mathbf{0}] \right]$$

$$\text{In[*]} := \gamma \mathbf{1} // \mathbf{m}_{i,j \rightarrow k} // \Gamma$$

$$\text{Out[*]} = \Gamma \left[-\omega + \beta \omega, \right. \\ \left. \frac{(-\gamma + \beta \gamma - \alpha \delta) p_k x_k}{-1 + \beta} + \frac{(-\epsilon + \beta \epsilon - \delta \theta) p_r x_k}{-1 + \beta} + \frac{(-\phi + \beta \phi - \alpha \psi) p_k x_r}{-1 + \beta} + \frac{(-\xi + \beta \xi - \theta \psi) p_r x_r}{-1 + \beta} \right]$$

$$\text{In[*]:= Simplify}\left[\left(\mathbb{E}@\Gamma\left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta & \epsilon & \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\}\right] \mathbb{E}_{\{\} \rightarrow \{i, j\}}[1, \theta, \text{eSeries}[\theta, p_i x_i]] // m_{1, i \rightarrow 1} // m_{1, 2 \rightarrow 1} // m_{1, j \rightarrow 1} // m_{1, 3 \rightarrow 1}\right) [[3, 2]] /. (x | p) _ \rightarrow \theta\right]$$

$$\text{Out[*]} = \frac{\beta + \gamma \epsilon - \beta \eta}{-1 + \beta + \gamma \epsilon + \eta - \beta \eta}$$

$$\text{In[*]:= Simplify}\left[\left(\mathbb{E}@\Gamma\left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta & \epsilon & \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\}\right] \mathbb{E}_{\{\} \rightarrow \{i, j\}}[1, \theta, \text{eSeries}[\theta, p_i x_j]] // m_{1, i \rightarrow 1} // m_{1, 2 \rightarrow 1} // m_{1, j \rightarrow 1} // m_{1, 3 \rightarrow 1}\right) [[3, 2]] /. (x | p) _ \rightarrow \theta\right]$$

$$\text{Out[*]} = \frac{\gamma}{-1 + \beta + \gamma \epsilon + \eta - \beta \eta}$$

$$\text{In[*]:= Simplify}\left[\left(\mathbb{E}@\Gamma\left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta & \epsilon & \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\}\right] \mathbb{E}_{\{\} \rightarrow \{i, j\}}[1, \theta, \text{eSeries}[\theta, p_j x_i]] // m_{1, i \rightarrow 1} // m_{1, 2 \rightarrow 1} // m_{1, j \rightarrow 1} // m_{1, 3 \rightarrow 1}\right) [[3, 2]] /. (x | p) _ \rightarrow \theta\right]$$

$$\text{Out[*]} = \frac{\epsilon}{-1 + \beta + \gamma \epsilon + \eta - \beta \eta}$$

$$\text{In[*]:= Simplify}\left[\left(\mathbb{E}@\Gamma\left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta & \epsilon & \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\}\right] \mathbb{E}_{\{\} \rightarrow \{i, j\}}[1, \theta, \text{eSeries}[\theta, p_j x_j]] // m_{1, i \rightarrow 1} // m_{1, 2 \rightarrow 1} // m_{1, j \rightarrow 1} // m_{1, 3 \rightarrow 1}\right) [[3, 2]] /. (x | p) _ \rightarrow \theta\right]$$

$$\text{Out[*]} = \frac{\gamma \epsilon + \eta - \beta \eta}{-1 + \beta + \gamma \epsilon + \eta - \beta \eta}$$

$$\text{In[*]} = C_i$$

$$\text{Out[*]} = \mathbb{E}_{\{\} \rightarrow \{i\}}\left[\sqrt{T}, \theta, \text{eSeries}\left[\theta, \frac{p_i x_i}{2}\right]\right]$$

$$\text{In[*]} := \text{CF}[\overline{\text{Rp}}_{i,j} /. \text{T} \rightarrow \text{T}^{-1}]$$

$$\text{Out[*]} := \mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\mathbf{1}, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_i^2 x_i x_j + \frac{1}{2} p_i p_j x_i x_j + \frac{(1-T) p_i^2 x_j^2}{4 T} + \frac{(-1+T) p_i p_j x_j^2}{4 T} \right] \right]$$

$$\text{In[*]} := \text{CF}[\text{Rp}_{i,j}]$$

$$\text{Out[*]} := \mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\mathbf{1}, \theta, \in \text{Series} \left[\theta, \frac{1}{2} p_i^2 x_i x_j - \frac{1}{2} p_i p_j x_i x_j + \frac{(-1+T) p_i^2 x_j^2}{4 T} + \frac{(1-T) p_i p_j x_j^2}{4 T} \right] \right]$$

$$\text{In[*]} := \text{Simplify} \left[\frac{1}{2} p_i^2 x_i x_j - \frac{1}{2} p_i p_j x_i x_j + \frac{(-1+T) p_i^2 x_j^2}{4 T} + \frac{(1-T) p_i p_j x_j^2}{4 T} \right]$$

$$\text{Out[*]} := \frac{p_i (p_i - p_j) x_j (2 T x_i + (-1+T) x_j)}{4 T}$$

$$\text{In[*]} := \text{Simplify} \left[\right.$$

$$\left(\mathbb{E} @ \Gamma \left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta \in \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\} \right] \mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\mathbf{1}, \theta, \in \text{Series} \left[\theta, p_i^2 x_i x_j \right] \right] // m_{1,i \rightarrow 1} // \right.$$

$$\left. m_{1,2 \rightarrow 1} // m_{1,j \rightarrow 1} // m_{1,3 \rightarrow 1} \right] \left[[3, 2] /. (x | p) _ \rightarrow \theta \right]$$

$$\text{Out[*]} := \frac{2 \gamma (\beta + \gamma \epsilon - \beta \eta)}{(-1 + \beta + \gamma \epsilon + \eta - \beta \eta)^2}$$

$$\text{In[*]} := \text{Simplify} \left[\right.$$

$$\left(\mathbb{E} @ \Gamma \left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta \in \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\} \right] \mathbb{E}_{\{\} \rightarrow \{i,j\}} \left[\mathbf{1}, \theta, \in \text{Series} \left[\theta, p_j x_j \right] \right] // m_{1,i \rightarrow 1} // \right.$$

$$\left. m_{1,2 \rightarrow 1} // m_{1,j \rightarrow 1} // m_{1,3 \rightarrow 1} \right] \left[[3, 2] /. (x | p) _ \rightarrow \theta \right]$$

$$\text{Out[*]} := \frac{\gamma \epsilon + \eta - \beta \eta}{-1 + \beta + \gamma \epsilon + \eta - \beta \eta}$$

$$\text{In[*]} := \mathbb{E} @ \Gamma \left[\omega, \{x_1, x_2, x_3\} \cdot \begin{pmatrix} \alpha & \beta & \gamma \\ \delta \in \eta \\ \lambda & \mu & \nu \end{pmatrix} \cdot \{p_1, p_2, p_3\} \right] \text{Rp}_{i,j} // m_{1,i \rightarrow 1} // m_{1,2 \rightarrow 1} // m_{1,j \rightarrow 1} // m_{1,3 \rightarrow 1}$$

$$\text{Out[*]} := \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{1}{\omega - \beta \omega - \gamma \epsilon \omega - \eta \omega + \beta \eta \omega}, \right.$$

$$\left. \frac{(1 - \beta - \gamma \epsilon - \eta + \beta \eta - \lambda + \beta \lambda + \gamma \epsilon \lambda + \eta \lambda - \beta \eta \lambda - \alpha \mu - \gamma \delta \mu + \alpha \eta \mu - \delta \nu + \beta \delta \nu - \alpha \epsilon \nu) p_1 x_1}{1 - \beta - \gamma \epsilon - \eta + \beta \eta}, \right.$$

$$\in \text{Series} \left[\theta, (2 T \beta \gamma - \gamma^2 + T \gamma^2 - T \gamma \epsilon - T \beta \gamma \epsilon + \gamma^2 \epsilon + T \gamma^2 \epsilon^2 - T \gamma^2 \epsilon^2 - T \beta \eta + T \beta^2 \eta + \gamma \eta - T \gamma \eta - \beta \gamma \eta - T \beta \gamma \eta - T \gamma \epsilon \eta + 2 T \beta \gamma \epsilon \eta + T \beta \eta^2 - T \beta^2 \eta^2) / (2 T - 4 T \beta + 2 T \beta^2 - 4 T \gamma \epsilon + 4 T \beta \gamma \epsilon + 2 T \gamma^2 \epsilon^2 - 4 T \eta + 8 T \beta \eta - 4 T \beta^2 \eta + 4 T \gamma \epsilon \eta - 4 T \beta \gamma \epsilon \eta + 2 T \eta^2 - 4 T \beta \eta^2 + 2 T \beta^2 \eta^2) + \right.$$

$$\begin{aligned}
 & \left((-2T\alpha\gamma\mu - 2T\alpha\beta\gamma\mu + 2\alpha\gamma^2\mu - 2T\alpha\gamma^2\mu + T\gamma\delta\mu - T\beta^2\gamma\delta\mu - \gamma^2\delta\mu - T\gamma^2\delta\mu + \right. \\
 & \quad \beta\gamma^2\delta\mu - 3T\beta\gamma^2\delta\mu + 2\gamma^3\delta\mu - 2T\gamma^3\delta\mu + 3T\alpha\gamma\epsilon\mu + T\alpha\beta\gamma\epsilon\mu - 2\alpha\gamma^2\epsilon\mu + \\
 & \quad 3T\gamma^2\delta\epsilon\mu - T\beta\gamma^2\delta\epsilon\mu - \gamma^3\delta\epsilon\mu - T\gamma^3\delta\epsilon\mu + T\alpha\gamma^2\epsilon^2\mu + T\alpha\eta\mu - T\alpha\beta\eta\mu - \alpha\gamma\eta\mu + \\
 & \quad 5T\alpha\gamma\eta\mu + \alpha\beta\gamma\eta\mu + 3T\alpha\beta\gamma\eta\mu - 2\alpha\gamma^2\eta\mu + 2T\alpha\gamma^2\eta\mu - T\beta\gamma\delta\eta\mu + T\beta^2\gamma\delta\eta\mu - \\
 & \quad \gamma^2\delta\eta\mu + 3T\gamma^2\delta\eta\mu + \beta\gamma^2\delta\eta\mu + T\beta\gamma^2\delta\eta\mu - 4T\alpha\gamma\epsilon\eta\mu - T\alpha\beta\gamma\epsilon\eta\mu + \alpha\gamma^2\epsilon\eta\mu + \\
 & \quad T\alpha\gamma^2\epsilon\eta\mu - T\gamma^2\delta\epsilon\eta\mu - 2T\alpha\eta^2\mu + 2T\alpha\beta\eta^2\mu + \alpha\gamma\eta^2\mu - 3T\alpha\gamma\eta^2\mu - \alpha\beta\gamma\eta^2\mu - \\
 & \quad T\alpha\beta\gamma\eta^2\mu - T\gamma\delta\eta^2\mu + T\beta\gamma\delta\eta^2\mu + T\alpha\gamma\epsilon\eta^2\mu + T\alpha\eta^3\mu - T\alpha\beta\eta^3\mu - 2T\alpha\beta\nu + \\
 & \quad 2T\alpha\beta^2\nu + 2\alpha\gamma\nu - 2T\alpha\gamma\nu - 2\alpha\beta\gamma\nu + 2T\alpha\beta\gamma\nu + T\beta\delta\nu - 2T\beta^2\delta\nu + T\beta^3\delta\nu - \gamma\delta\nu + \\
 & \quad T\gamma\delta\nu + 2T\beta\gamma\delta\nu - 4T\beta\gamma\delta\nu - \beta^2\gamma\delta\nu + 3T\beta^2\gamma\delta\nu + 2\gamma^2\delta\nu - 2T\gamma^2\delta\nu - 2\beta\gamma^2\delta\nu + \\
 & \quad 2T\beta\gamma^2\delta\nu + T\alpha\epsilon\nu - T\alpha\beta^2\epsilon\nu - 2\alpha\gamma\epsilon\nu - 2T\alpha\gamma\epsilon\nu + 2\alpha\beta\gamma\epsilon\nu + 3T\gamma\delta\epsilon\nu - \\
 & \quad 4T\beta\gamma\delta\epsilon\nu + T\beta^2\gamma\delta\epsilon\nu - \gamma^2\delta\epsilon\nu - 3T\gamma^2\delta\epsilon\nu + \beta\gamma^2\delta\epsilon\nu + T\beta\gamma^2\delta\epsilon\nu + 3T\alpha\gamma\epsilon^2\nu - \\
 & \quad T\alpha\beta\gamma\epsilon^2\nu + T\gamma^2\delta\epsilon^2\nu - \alpha\eta\nu + T\alpha\eta\nu + 2\alpha\beta\eta\nu + 2T\alpha\beta\eta\nu - \alpha\beta^2\eta\nu - 3T\alpha\beta^2\eta\nu - \\
 & \quad 2\alpha\gamma\eta\nu + 2T\alpha\gamma\eta\nu + 2\alpha\beta\gamma\eta\nu - 2T\alpha\beta\gamma\eta\nu - T\beta\delta\eta\nu + 2T\beta^2\delta\eta\nu - T\beta^3\delta\eta\nu - \\
 & \quad \gamma\delta\eta\nu + T\gamma\delta\eta\nu + 2T\beta\gamma\delta\eta\nu - \beta^2\gamma\delta\eta\nu - T\beta^2\gamma\delta\eta\nu - T\alpha\beta\epsilon\eta\nu + T\alpha\beta^2\epsilon\eta\nu + \\
 & \quad \alpha\gamma\epsilon\eta\nu + 3T\alpha\gamma\epsilon\eta\nu - \alpha\beta\gamma\epsilon\eta\nu - T\alpha\beta\gamma\epsilon\eta\nu + T\gamma\delta\epsilon\eta\nu - T\beta\gamma\delta\epsilon\eta\nu - T\alpha\gamma\epsilon^2\eta\nu + \\
 & \quad \alpha\eta^2\nu - T\alpha\eta^2\nu - 2\alpha\beta\eta^2\nu + \alpha\beta^2\eta^2\nu + T\alpha\beta^2\eta^2\nu - T\alpha\epsilon\eta^2\nu + T\alpha\beta\epsilon\eta^2\nu) \mathbf{p}_1 \mathbf{x}_1) / \\
 & (2T - 6T\beta + 6T\beta^2 - 2T\beta^3 - 6T\gamma\epsilon + 12T\beta\gamma\epsilon - 6T\beta^2\gamma\epsilon + 6T\gamma^2\epsilon^2 - 6T\beta\gamma^2\epsilon^2 - \\
 & \quad 2T\gamma^3\epsilon^3 - 6T\eta + 18T\beta\eta - 18T\beta^2\eta + 6T\beta^3\eta + 12T\gamma\epsilon\eta - 24T\beta\gamma\epsilon\eta + \\
 & \quad 12T\beta^2\gamma\epsilon\eta - 6T\gamma^2\epsilon^2\eta + 6T\beta\gamma^2\epsilon^2\eta + 6T\eta^2 - 18T\beta\eta^2 + 18T\beta^2\eta^2 - 6T\beta^3\eta^2 - \\
 & \quad 6T\gamma\epsilon\eta^2 + 12T\beta\gamma\epsilon\eta^2 - 6T\beta^2\gamma\epsilon\eta^2 - 2T\eta^3 + 6T\beta\eta^3 - 6T\beta^2\eta^3 + 2T\beta^3\eta^3) + \\
 & \left((2T\alpha^2\gamma\mu^2 - \alpha^2\gamma^2\mu^2 + T\alpha^2\gamma^2\mu^2 - 2T\alpha\gamma\delta\mu^2 + 2T\alpha\beta\gamma\delta\mu^2 + \alpha\gamma^2\delta\mu^2 + 3T\alpha\gamma^2\delta\mu^2 - \alpha\beta\gamma^2\delta\mu^2 + \right. \\
 & \quad T\alpha\beta\gamma^2\delta\mu^2 - 2\alpha\gamma^3\delta\mu^2 + 2T\alpha\gamma^3\delta\mu^2 - 2T\gamma^2\delta^2\mu^2 + 2T\beta\gamma^2\delta^2\mu^2 + \gamma^3\delta^2\mu^2 + T\gamma^3\delta^2\mu^2 - \\
 & \quad \beta\gamma^3\delta^2\mu^2 + T\beta\gamma^3\delta^2\mu^2 - \gamma^4\delta^2\mu^2 + T\gamma^4\delta^2\mu^2 - 2T\alpha^2\gamma\epsilon\mu^2 + \alpha^2\gamma^2\epsilon\mu^2 - T\alpha^2\gamma^2\epsilon\mu^2 - \\
 & \quad 2T\alpha\gamma^2\delta\epsilon\mu^2 + \alpha\gamma^3\delta\epsilon\mu^2 - T\alpha\gamma^3\delta\epsilon\mu^2 - 6T\alpha^2\gamma\eta\mu^2 + 2\alpha^2\gamma^2\eta\mu^2 - 2T\alpha^2\gamma^2\eta\mu^2 + \\
 & \quad 4T\alpha\gamma\delta\eta\mu^2 - 4T\alpha\beta\gamma\delta\eta\mu^2 - \alpha\gamma^2\delta\eta\mu^2 - 7T\alpha\gamma^2\delta\eta\mu^2 + \alpha\beta\gamma^2\delta\eta\mu^2 - T\alpha\beta\gamma^2\delta\eta\mu^2 + \\
 & \quad 2\alpha\gamma^3\delta\eta\mu^2 - 2T\alpha\gamma^3\delta\eta\mu^2 + 2T\gamma^2\delta^2\eta\mu^2 - 2T\beta\gamma^2\delta^2\eta\mu^2 - 2T\gamma^3\delta^2\eta\mu^2 + 4T\alpha^2\gamma\epsilon\eta\mu^2 - \\
 & \quad \alpha^2\gamma^2\epsilon\eta\mu^2 + T\alpha^2\gamma^2\epsilon\eta\mu^2 + 2T\alpha\gamma^2\delta\epsilon\eta\mu^2 + 6T\alpha^2\gamma\eta^2\mu^2 - \alpha^2\gamma^2\eta^2\mu^2 + T\alpha^2\gamma^2\eta^2\mu^2 - \\
 & \quad 2T\alpha\gamma\delta\eta^2\mu^2 + 2T\alpha\beta\gamma\delta\eta^2\mu^2 + 4T\alpha\gamma^2\delta\eta^2\mu^2 - 2T\alpha^2\gamma\epsilon\eta^2\mu^2 - 2T\alpha^2\gamma\eta^3\mu^2 + 2T\alpha^2\mu\nu - \\
 & \quad 2T\alpha^2\beta\mu\nu - 2\alpha^2\gamma\mu\nu + 2T\alpha^2\gamma\mu\nu + 2\alpha^2\beta\gamma\mu\nu - 2T\alpha^2\beta\gamma\mu\nu - 2T\alpha\delta\mu\nu + 4T\alpha\beta\delta\mu\nu - \\
 & \quad 2T\alpha\beta^2\delta\mu\nu + 2\alpha\gamma\delta\mu\nu + 2T\alpha\gamma\delta\mu\nu - 4\alpha\beta\gamma\delta\mu\nu + 2\alpha\beta^2\gamma\delta\mu\nu - 2T\alpha\beta^2\gamma\delta\mu\nu - \\
 & \quad 4\alpha\gamma^2\delta\mu\nu + 4T\alpha\gamma^2\delta\mu\nu + 4\alpha\beta\gamma^2\delta\mu\nu - 4T\alpha\beta\gamma^2\delta\mu\nu - 2T\gamma\delta^2\mu\nu + 4T\beta\gamma\delta^2\mu\nu - \\
 & \quad 2T\beta^2\gamma\delta^2\mu\nu + 2\gamma^2\delta^2\mu\nu - 4\beta\gamma^2\delta^2\mu\nu + 2T\beta\gamma^2\delta^2\mu\nu + 2\beta^2\gamma^2\delta^2\mu\nu - 2T\beta^2\gamma^2\delta^2\mu\nu - \\
 & \quad 2\gamma^3\delta^2\mu\nu + 2T\gamma^3\delta^2\mu\nu + 2\beta\gamma^3\delta^2\mu\nu - 2T\beta\gamma^3\delta^2\mu\nu - 2T\alpha^2\epsilon\mu\nu + 2T\alpha^2\beta\epsilon\mu\nu + \\
 & \quad 2\alpha^2\gamma\epsilon\mu\nu - 2\alpha^2\beta\gamma\epsilon\mu\nu + 2T\alpha^2\beta\gamma\epsilon\mu\nu - 4T\alpha\gamma\delta\epsilon\mu\nu + 4T\alpha\beta\gamma\delta\epsilon\mu\nu + 2\alpha\gamma^2\delta\epsilon\mu\nu + \\
 & \quad 2T\alpha\gamma^2\delta\epsilon\mu\nu - 2\alpha\beta\gamma^2\delta\epsilon\mu\nu + 2T\alpha\beta\gamma^2\delta\epsilon\mu\nu - 2T\gamma^2\delta^2\epsilon\mu\nu + 2T\beta\gamma^2\delta^2\epsilon\mu\nu + \\
 & \quad 2T\gamma^3\delta^2\epsilon\mu\nu - 2T\alpha^2\gamma\epsilon^2\mu\nu - 2T\alpha\gamma^2\delta\epsilon^2\mu\nu - 6T\alpha^2\eta\mu\nu + 6T\alpha^2\beta\eta\mu\nu + 4\alpha^2\gamma\eta\mu\nu - \\
 & \quad 4T\alpha^2\gamma\eta\mu\nu - 4\alpha^2\beta\gamma\eta\mu\nu + 4T\alpha^2\beta\gamma\eta\mu\nu + 4T\alpha\delta\eta\mu\nu - 8T\alpha\beta\delta\eta\mu\nu + 4T\alpha\beta^2\delta\eta\mu\nu - \\
 & \quad 2\alpha\gamma\delta\eta\mu\nu - 6T\alpha\gamma\delta\eta\mu\nu + 4\alpha\beta\gamma\delta\eta\mu\nu + 4T\alpha\beta\gamma\delta\eta\mu\nu - 2\alpha\beta^2\gamma\delta\eta\mu\nu + \\
 & \quad 2T\alpha\beta^2\gamma\delta\eta\mu\nu + 4\alpha\gamma^2\delta\eta\mu\nu - 4T\alpha\gamma^2\delta\eta\mu\nu - 4\alpha\beta\gamma^2\delta\eta\mu\nu + 4T\alpha\beta\gamma^2\delta\eta\mu\nu + \\
 & \quad 2T\gamma\delta^2\eta\mu\nu - 4T\beta\gamma\delta^2\eta\mu\nu + 2T\beta^2\gamma\delta^2\eta\mu\nu - 2T\gamma^2\delta^2\eta\mu\nu + 2T\beta\gamma^2\delta^2\eta\mu\nu + \\
 & \quad 4T\alpha^2\epsilon\eta\mu\nu - 4T\alpha^2\beta\epsilon\eta\mu\nu - 2\alpha^2\gamma\epsilon\eta\mu\nu - 2T\alpha^2\gamma\epsilon\eta\mu\nu + 2\alpha^2\beta\gamma\epsilon\eta\mu\nu - \\
 & \quad 2T\alpha^2\beta\gamma\epsilon\eta\mu\nu + 4T\alpha\gamma\delta\epsilon\eta\mu\nu - 4T\alpha\beta\gamma\delta\epsilon\eta\mu\nu - 4T\alpha\gamma^2\delta\epsilon\eta\mu\nu + 2T\alpha^2\gamma\epsilon^2\eta\mu\nu + \\
 & \quad 6T\alpha^2\eta^2\mu\nu - 6T\alpha^2\beta\eta^2\mu\nu - 2\alpha^2\gamma\eta^2\mu\nu + 2T\alpha^2\gamma\eta^2\mu\nu + 2\alpha^2\beta\gamma\eta^2\mu\nu - 2T\alpha^2\beta\gamma\eta^2\mu\nu - \\
 & \quad 2T\alpha\delta\eta^2\mu\nu + 4T\alpha\beta\delta\eta^2\mu\nu - 2T\alpha\beta^2\delta\eta^2\mu\nu + 4T\alpha\gamma\delta\eta^2\mu\nu - 4T\alpha\beta\gamma\delta\eta^2\mu\nu -
 \end{aligned}$$

$$\begin{aligned}
 & 2T\alpha^2\epsilon\eta^2\mu\nu + 2T\alpha^2\beta\epsilon\eta^2\mu\nu + 2T\alpha^2\gamma\epsilon\eta^2\mu\nu - 2T\alpha^2\eta^3\mu\nu + 2T\alpha^2\beta\eta^3\mu\nu - \alpha^2\nu^2 + \\
 & T\alpha^2\nu^2 + 2\alpha^2\beta\nu^2 - 2T\alpha^2\beta\nu^2 - \alpha^2\beta^2\nu^2 + T\alpha^2\beta^2\nu^2 + \alpha\delta\nu^2 - T\alpha\delta\nu^2 - 3\alpha\beta\delta\nu^2 + \\
 & 3T\alpha\beta\delta\nu^2 + 3\alpha\beta^2\delta\nu^2 - 3T\alpha\beta^2\delta\nu^2 - \alpha\beta^3\delta\nu^2 + T\alpha\beta^3\delta\nu^2 - 2\alpha\gamma\delta\nu^2 + 2T\alpha\gamma\delta\nu^2 + \\
 & 4\alpha\beta\gamma\delta\nu^2 - 4T\alpha\beta\gamma\delta\nu^2 - 2\alpha\beta^2\gamma\delta\nu^2 + 2T\alpha\beta^2\gamma\delta\nu^2 + \gamma\delta^2\nu^2 - T\gamma\delta^2\nu^2 - 3\beta\gamma\delta^2\nu^2 + \\
 & 3T\beta\gamma\delta^2\nu^2 + 3\beta^2\gamma\delta^2\nu^2 - 3T\beta^2\gamma\delta^2\nu^2 - \beta^3\gamma\delta^2\nu^2 + T\beta^3\gamma\delta^2\nu^2 - \gamma^2\delta^2\nu^2 + T\gamma^2\delta^2\nu^2 + \\
 & 2\beta\gamma^2\delta^2\nu^2 - 2T\beta\gamma^2\delta^2\nu^2 - \beta^2\gamma^2\delta^2\nu^2 + T\beta^2\gamma^2\delta^2\nu^2 + \alpha^2\epsilon\nu^2 + T\alpha^2\epsilon\nu^2 - 2\alpha^2\beta\epsilon\nu^2 + \\
 & \alpha^2\beta^2\epsilon\nu^2 - T\alpha^2\beta^2\epsilon\nu^2 - 2T\alpha\delta\epsilon\nu^2 + 4T\alpha\beta\delta\epsilon\nu^2 - 2T\alpha\beta^2\delta\epsilon\nu^2 + \alpha\gamma\delta\epsilon\nu^2 + \\
 & 3T\alpha\gamma\delta\epsilon\nu^2 - 2\alpha\beta\gamma\delta\epsilon\nu^2 - 2T\alpha\beta\gamma\delta\epsilon\nu^2 + \alpha\beta^2\gamma\delta\epsilon\nu^2 - T\alpha\beta^2\gamma\delta\epsilon\nu^2 - 2T\gamma\delta^2\epsilon\nu^2 + \\
 & 4T\beta\gamma\delta^2\epsilon\nu^2 - 2T\beta^2\gamma\delta^2\epsilon\nu^2 + 2T\gamma^2\delta^2\epsilon\nu^2 - 2T\beta\gamma^2\delta^2\epsilon\nu^2 - 2T\alpha^2\epsilon^2\nu^2 + 2T\alpha^2\beta\epsilon^2\nu^2 - \\
 & 2T\alpha\gamma\delta\epsilon^2\nu^2 + 2T\alpha\beta\gamma\delta\epsilon^2\nu^2 + 2\alpha^2\eta\nu^2 - 2T\alpha^2\eta\nu^2 - 4\alpha^2\beta\eta\nu^2 + 4T\alpha^2\beta\eta\nu^2 + \\
 & 2\alpha^2\beta^2\eta\nu^2 - 2T\alpha^2\beta^2\eta\nu^2 - \alpha\delta\eta\nu^2 + T\alpha\delta\eta\nu^2 + 3\alpha\beta\delta\eta\nu^2 - 3T\alpha\beta\delta\eta\nu^2 - 3\alpha\beta^2\delta\eta\nu^2 + \\
 & 3T\alpha\beta^2\delta\eta\nu^2 + \alpha\beta^3\delta\eta\nu^2 - T\alpha\beta^3\delta\eta\nu^2 + 2\alpha\gamma\delta\eta\nu^2 - 2T\alpha\gamma\delta\eta\nu^2 - 4\alpha\beta\gamma\delta\eta\nu^2 + \\
 & 4T\alpha\beta\gamma\delta\eta\nu^2 + 2\alpha\beta^2\gamma\delta\eta\nu^2 - 2T\alpha\beta^2\gamma\delta\eta\nu^2 - \alpha^2\epsilon\eta\nu^2 - 3T\alpha^2\epsilon\eta\nu^2 + 2\alpha^2\beta\epsilon\eta\nu^2 + \\
 & 2T\alpha^2\beta\epsilon\eta\nu^2 - \alpha^2\beta^2\epsilon\eta\nu^2 + T\alpha^2\beta^2\epsilon\eta\nu^2 + 2T\alpha\delta\epsilon\eta\nu^2 - 4T\alpha\beta\delta\epsilon\eta\nu^2 + 2T\alpha\beta^2\delta\epsilon\eta\nu^2 - \\
 & 4T\alpha\gamma\delta\epsilon\eta\nu^2 + 4T\alpha\beta\gamma\delta\epsilon\eta\nu^2 + 2T\alpha^2\epsilon^2\eta\nu^2 - 2T\alpha^2\beta\epsilon^2\eta\nu^2 - \alpha^2\eta^2\nu^2 + T\alpha^2\eta^2\nu^2 + \\
 & 2\alpha^2\beta\eta^2\nu^2 - 2T\alpha^2\beta\eta^2\nu^2 - \alpha^2\beta^2\eta^2\nu^2 + T\alpha^2\beta^2\eta^2\nu^2 + 2T\alpha^2\epsilon\eta^2\nu^2 - 2T\alpha^2\beta\epsilon\eta^2\nu^2) p_1^2 x_1^2) / \\
 & (4T - 16T\beta + 24T\beta^2 - 16T\beta^3 + 4T\beta^4 - 16T\gamma\epsilon + 48T\beta\gamma\epsilon - 48T\beta^2\gamma\epsilon + 16T\beta^3\gamma\epsilon + \\
 & 24T\gamma^2\epsilon^2 - 48T\beta\gamma^2\epsilon^2 + 24T\beta^2\gamma^2\epsilon^2 - 16T\gamma^3\epsilon^3 + 16T\beta\gamma^3\epsilon^3 + 4T\gamma^4\epsilon^4 - \\
 & 16T\eta + 64T\beta\eta - 96T\beta^2\eta + 64T\beta^3\eta - 16T\beta^4\eta + 48T\gamma\epsilon\eta - 144T\beta\gamma\epsilon\eta + \\
 & 144T\beta^2\gamma\epsilon\eta - 48T\beta^3\gamma\epsilon\eta - 48T\gamma^2\epsilon^2\eta + 96T\beta\gamma^2\epsilon^2\eta - 48T\beta^2\gamma^2\epsilon^2\eta + \\
 & 16T\gamma^3\epsilon^3\eta - 16T\beta\gamma^3\epsilon^3\eta + 24T\eta^2 - 96T\beta\eta^2 + 144T\beta^2\eta^2 - 96T\beta^3\eta^2 + \\
 & 24T\beta^4\eta^2 - 48T\gamma\epsilon\eta^2 + 144T\beta\gamma\epsilon\eta^2 - 144T\beta^2\gamma\epsilon\eta^2 + 48T\beta^3\gamma\epsilon\eta^2 + \\
 & 24T\gamma^2\epsilon^2\eta^2 - 48T\beta\gamma^2\epsilon^2\eta^2 + 24T\beta^2\gamma^2\epsilon^2\eta^2 - 16T\eta^3 + 64T\beta\eta^3 - \\
 & 96T\beta^2\eta^3 + 64T\beta^3\eta^3 - 16T\beta^4\eta^3 + 16T\gamma\epsilon\eta^3 - 48T\beta\gamma\epsilon\eta^3 + 48T\beta^2\gamma\epsilon\eta^3 - \\
 & 16T\beta^3\gamma\epsilon\eta^3 + 4T\eta^4 - 16T\beta\eta^4 + 24T\beta^2\eta^4 - 16T\beta^3\eta^4 + 4T\beta^4\eta^4)]]
 \end{aligned}$$

$$\begin{aligned}
 \text{In[]:= Simplify} & [(\beta\gamma - T\beta\gamma - T\gamma^2 + T^2\gamma^2 - \gamma\epsilon - \beta\gamma\epsilon + \gamma^2\epsilon + T\gamma^2\epsilon - \\
 & \gamma^2\epsilon^2 - \beta\eta + \beta^2\eta + 2T\gamma\eta - \beta\gamma\eta - T\beta\gamma\eta - \gamma\epsilon\eta + 2\beta\gamma\epsilon\eta + \beta\eta^2 - \beta^2\eta^2) / \\
 & (2 - 4\beta + 2\beta^2 - 4\gamma\epsilon + 4\beta\gamma\epsilon + 2\gamma^2\epsilon^2 - 4\eta + 8\beta\eta - 4\beta^2\eta + 4\gamma\epsilon\eta - 4\beta\gamma\epsilon\eta + 2\eta^2 - 4\beta\eta^2 + 2\beta^2\eta^2)]
 \end{aligned}$$

$$\begin{aligned}
 \text{Out[]:=} & \frac{1}{2(-1 + \beta + \gamma\epsilon + \eta - \beta\eta)^2} (\beta(-1 + \eta)\eta - \beta^2(-1 + \eta)\eta - \\
 & \beta\gamma(-1 + T + \epsilon + \eta + T\eta - 2\epsilon\eta) + \gamma(T^2\gamma - \epsilon(1 + \gamma(-1 + \epsilon) + \eta) + T(\gamma(-1 + \epsilon) + 2\eta))
 \end{aligned}$$

$$\text{In[]:= IdentityMatrix[3] - } \begin{pmatrix} \alpha & \beta & \gamma \\ \delta & \epsilon & \eta \\ \lambda & \mu & \nu \end{pmatrix} // \text{Det} // \text{Simplify}$$

$$\text{Out[]:= } 1 - \epsilon - \gamma\lambda + \gamma\epsilon\lambda - \gamma\delta\mu - \eta\mu - \nu + \epsilon\nu - \beta(\delta + \eta\lambda - \delta\nu) + \alpha(-1 + \epsilon + \eta\mu + \nu - \epsilon\nu)$$

Solving for R, C, \$k = 2

In[*]:= \$k = 2;

{R1,2, C1}

Short [RMoves, 20]

$$\begin{aligned}
 \text{Out[*]} = & \left\{ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[\sqrt{T}, (-1 + T) p_1 x_2 + (1 - T) p_2 x_2, \right. \right. \\
 & \in \text{Series} \left[\theta, \frac{1}{2} T p_1^2 x_1 x_2 - \frac{1}{2} T p_1 p_2 x_1 x_2 + \frac{1}{4} (T - T^2) p_1^2 x_2^2 + \frac{1}{4} (-T + T^2) p_1 p_2 x_2^2, \right. \\
 & c_{2,1} + p_1 x_1 c_{2,2} + p_1 x_2 (c_{2,2} - T c_{2,2} + T c_{2,3}) + p_2 x_1 c_{2,4} + p_2 x_2 (c_{2,4} - T c_{2,4} + T c_{2,5}) + p_1^2 x_1^2 c_{2,6} + \\
 & p_1^2 x_1 x_2 (2 c_{2,6} - 2 T c_{2,6} + T c_{2,7}) + p_1^2 x_2^2 (c_{2,6} - 2 T c_{2,6} + T^2 c_{2,6} + T c_{2,7} - T^2 c_{2,7} + T^2 c_{2,8}) + \\
 & p_1 p_2 x_1^2 c_{2,9} + p_1 p_2 x_1 x_2 (2 c_{2,9} - 2 T c_{2,9} + T c_{2,10}) + \\
 & p_1 p_2 x_2^2 (c_{2,9} - 2 T c_{2,9} + T^2 c_{2,9} + T c_{2,10} - T^2 c_{2,10} + T^2 c_{2,11}) + p_2^2 x_1^2 c_{2,12} + \\
 & p_2^2 x_1 x_2 (2 c_{2,12} - 2 T c_{2,12} + T c_{2,13}) + p_2^2 x_2^2 (c_{2,12} - 2 T c_{2,12} + T^2 c_{2,12} + T c_{2,13} - T^2 c_{2,13} + T^2 c_{2,14}) + \\
 & p_1^3 x_1^3 c_{2,15} + p_1^3 x_1^2 x_2 (3 c_{2,15} - 3 T c_{2,15} + T c_{2,16}) + \\
 & p_1^3 x_1 x_2^2 (3 c_{2,15} - 6 T c_{2,15} + 3 T^2 c_{2,15} + 2 T c_{2,16} - 2 T^2 c_{2,16} + T^2 c_{2,17}) + p_1^3 x_2^3 \\
 & (c_{2,15} - 3 T c_{2,15} + 3 T^2 c_{2,15} - T^3 c_{2,15} + T c_{2,16} - 2 T^2 c_{2,16} + T^3 c_{2,16} + T^2 c_{2,17} - T^3 c_{2,17} + T^3 c_{2,18}) + \\
 & p_1^2 p_2 x_1^3 c_{2,19} + p_1^2 p_2 x_1^2 x_2 (3 c_{2,19} - 3 T c_{2,19} + T c_{2,20}) + \\
 & p_1^2 p_2 x_1 x_2^2 (3 c_{2,19} - 6 T c_{2,19} + 3 T^2 c_{2,19} + 2 T c_{2,20} - 2 T^2 c_{2,20} + T^2 c_{2,21}) + p_1^2 p_2 x_2^3 \\
 & (c_{2,19} - 3 T c_{2,19} + 3 T^2 c_{2,19} - T^3 c_{2,19} + T c_{2,20} - 2 T^2 c_{2,20} + T^3 c_{2,20} + T^2 c_{2,21} - T^3 c_{2,21} + T^3 c_{2,22}) + \\
 & p_1 p_2^2 x_1^3 c_{2,23} + p_1 p_2^2 x_1^2 x_2 (3 c_{2,23} - 3 T c_{2,23} + T c_{2,24}) + \\
 & p_1 p_2^2 x_1 x_2^2 (3 c_{2,23} - 6 T c_{2,23} + 3 T^2 c_{2,23} + 2 T c_{2,24} - 2 T^2 c_{2,24} + T^2 c_{2,25}) + p_1 p_2^2 x_2^3 \\
 & (c_{2,23} - 3 T c_{2,23} + 3 T^2 c_{2,23} - T^3 c_{2,23} + T c_{2,24} - 2 T^2 c_{2,24} + T^3 c_{2,24} + T^2 c_{2,25} - T^3 c_{2,25} + T^3 c_{2,26}) + \\
 & p_2^3 x_1^3 c_{2,27} + p_2^3 x_1^2 x_2 (3 c_{2,27} - 3 T c_{2,27} + T c_{2,28}) + \\
 & p_2^3 x_1 x_2^2 (3 c_{2,27} - 6 T c_{2,27} + 3 T^2 c_{2,27} + 2 T c_{2,28} - 2 T^2 c_{2,28} + T^2 c_{2,29}) + p_2^3 x_2^3 \\
 & (c_{2,27} - 3 T c_{2,27} + 3 T^2 c_{2,27} - T^3 c_{2,27} + T c_{2,28} - 2 T^2 c_{2,28} + T^3 c_{2,28} + T^2 c_{2,29} - T^3 c_{2,29} + T^3 c_{2,30}) \left. \right] \left. \right\}, \\
 & \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2}, e_{2,1} + p_1 x_1 e_{2,2} + p_1^2 x_1^2 e_{2,3} + p_1^3 x_1^3 e_{2,4} \right] \right] \left. \right\}
 \end{aligned}$$

Out[*]//Short=

{ <<1>> }

In[*]:= unknowns = Cases [{R1,2, R1,2, C1, C1}, (c | d | e | f) \$k,_, ∞] // Union

Out[*]= {c2,1, c2,2, c2,3, c2,4, c2,5, c2,6, c2,7, c2,8, c2,9, c2,10, c2,11, c2,12, c2,13, c2,14, c2,15, c2,16, c2,17, c2,18, c2,19, c2,20, c2,21, c2,22, c2,23, c2,24, c2,25, c2,26, c2,27, c2,28, c2,29, c2,30, d2,1, d2,2, d2,3, d2,4, d2,5, d2,6, d2,7, d2,8, d2,9, d2,10, d2,11, d2,12, d2,13, d2,14, d2,15, d2,16, d2,17, d2,18, d2,19, d2,20, d2,21, d2,22, d2,23, d2,24, d2,25, d2,26, d2,27, d2,28, d2,29, d2,30, e2,1, e2,2, e2,3, e2,4, f2,1, f2,2, f2,3, f2,4}

In[*]:= Short[errors = CCF /@ Cases[RMoves, a_ == b_ => a - b], 25]

Out[*]//Short=

$$\left\{ \frac{1}{8} \left(4 T^2 p_1^3 x_1 x_2 x_3 - 4 T^3 p_1^3 x_1 x_2 x_3 - 4 T^2 p_1^2 p_2 x_1 x_2 x_3 + 4 T^3 p_1^2 p_2 x_1 x_2 x_3 + 2 T^2 p_1 p_2^2 x_1 x_2 x_3 - 2 T^3 p_1 p_2^2 x_1 x_2 x_3 - 2 T^2 p_1^2 p_3 x_1 x_2 x_3 + 2 T^3 p_1^2 p_3 x_1 x_2 x_3 + 2 T^2 p_1^3 x_2^2 x_3 - 2 T^3 p_1^3 x_2^2 x_3 - 3 T^2 p_1^2 p_2 x_2^2 x_3 + 3 T^3 p_1^2 p_2 x_2^2 x_3 + T^2 p_1 p_2^2 x_2^2 x_3 - 3 T^3 p_1 p_2^2 x_2^2 x_3 + 2 T^4 p_1 p_2^2 x_2^2 x_3 + 2 T^3 p_1 p_2 p_3 x_2^2 x_3 - 2 T^4 p_1 p_2 p_3 x_2^2 x_3 - 4 T^3 p_1^3 x_1 x_3^2 + 4 T^4 p_1^3 x_1 x_3^2 + T^2 p_1^2 p_2 x_1 x_3^2 + T^3 p_1^2 p_2 x_1 x_3^2 - 2 T^4 p_1^2 p_2 x_1 x_3^2 - T^2 p_1^2 p_3 x_1 x_3^2 + 5 T^3 p_1^2 p_3 x_1 x_3^2 - 4 T^4 p_1^2 p_3 x_1 x_3^2 - 2 T^3 p_1 p_2 p_3 x_1 x_3^2 + 2 T^4 p_1 p_2 p_3 x_1 x_3^2 - 2 T^4 p_1^3 x_2 x_3^2 + 2 T^5 p_1^3 x_2 x_3^2 - T^3 p_1^2 p_2 x_2 x_3^2 + 2 T^4 p_1^2 p_2 x_2 x_3^2 - T^5 p_1^2 p_2 x_2 x_3^2 + 3 T^4 p_1 p_2^2 x_2 x_3^2 - 3 T^5 p_1 p_2^2 x_2 x_3^2 + T^3 p_1^2 p_3 x_2 x_3^2 + T^4 p_1^2 p_3 x_2 x_3^2 - 2 T^5 p_1^2 p_3 x_2 x_3^2 - 4 T^4 p_1 p_2 p_3 x_2 x_3^2 + 4 T^5 p_1 p_2 p_3 x_2 x_3^2 - 2 T^4 p_1^3 x_3^3 + 4 T^5 p_1^3 x_3^3 - 2 T^6 p_1^3 x_3^3 + \ll 1952 \gg + 8 T^2 p_1^3 x_3^3 c_{2,29} - 32 T^3 p_1^3 x_3^3 c_{2,29} + 48 T^4 p_1^3 x_3^3 c_{2,29} - 32 T^5 p_1^3 x_3^3 c_{2,29} + 8 T^6 p_1^3 x_3^3 c_{2,29} + 8 T^3 p_2^3 x_3^3 c_{2,29} - 24 T^4 p_2^3 x_3^3 c_{2,29} + 24 T^5 p_2^3 x_3^3 c_{2,29} - 8 T^6 p_2^3 x_3^3 c_{2,29} + 24 T^3 p_1^2 p_3 x_3^3 c_{2,29} - 72 T^4 p_1^2 p_3 x_3^3 c_{2,29} + 72 T^5 p_1^2 p_3 x_3^3 c_{2,29} - 24 T^6 p_1^2 p_3 x_3^3 c_{2,29} - 24 T^3 p_2^2 p_3 x_3^3 c_{2,29} + 72 T^4 p_2^2 p_3 x_3^3 c_{2,29} - 72 T^5 p_2^2 p_3 x_3^3 c_{2,29} + 24 T^6 p_2^2 p_3 x_3^3 c_{2,29} + 24 T^4 p_1 p_2^3 x_3^3 c_{2,29} - 48 T^5 p_1 p_2^3 x_3^3 c_{2,29} + 24 T^6 p_1 p_2^3 x_3^3 c_{2,29} - 24 T^4 p_2 p_2^3 x_3^3 c_{2,29} + 48 T^5 p_2 p_2^3 x_3^3 c_{2,29} - 24 T^6 p_2 p_2^3 x_3^3 c_{2,29} + 24 T^3 p_2^3 x_2^2 x_3 c_{2,30} - 24 T^4 p_2^3 x_2^2 x_3 c_{2,30} + 24 T^3 p_2^2 x_2 x_3^2 c_{2,30} - 48 T^4 p_2^2 x_2 x_3^2 c_{2,30} + 24 T^5 p_2^2 x_2 x_3^2 c_{2,30} + 8 T^3 p_1^3 x_3^3 c_{2,30} - 24 T^4 p_1^3 x_3^3 c_{2,30} + 24 T^5 p_1^3 x_3^3 c_{2,30} - 8 T^6 p_1^3 x_3^3 c_{2,30} + 24 T^4 p_1^2 p_3 x_3^3 c_{2,30} - 48 T^5 p_1^2 p_3 x_3^3 c_{2,30} + 24 T^6 p_1^2 p_3 x_3^3 c_{2,30} - 24 T^4 p_2^2 p_3 x_3^3 c_{2,30} + 48 T^5 p_2^2 p_3 x_3^3 c_{2,30} - 24 T^6 p_2^2 p_3 x_3^3 c_{2,30} + 24 T^5 p_1 p_2^3 x_3^3 c_{2,30} - 24 T^6 p_1 p_2^3 x_3^3 c_{2,30} - 24 T^5 p_2 p_2^3 x_3^3 c_{2,30} + 24 T^6 p_2 p_2^3 x_3^3 c_{2,30} \right), \ll 7 \gg, \frac{\ll 1 \gg}{8 \ll 1 \gg} \right\}$$

In[*]:= Short[# , 10] & [eqns =

Thread[theta == Union@@ (CoefficientRules[# , {x1, x2, x3, p1, p2, p3}][[; , 2] & /@ errors)]]

Out[*]//Short=

$$\left\{ \theta == c_{2,4} - T c_{2,4}, \theta == -c_{2,4} + T c_{2,4}, \theta == T c_{2,4} - T^2 c_{2,4}, \ll 213 \gg, \right. \\ \theta == -\frac{1}{4} + \frac{T}{4} + T^3 c_{2,18} - T^2 c_{2,22} + T^3 c_{2,22} + T c_{2,26} - 2 T^2 c_{2,26} + T^3 c_{2,26} - \\ c_{2,30} + 3 T c_{2,30} - 3 T^2 c_{2,30} + T^3 c_{2,30} - d_{2,15} + 3 T d_{2,15} - 3 T^2 d_{2,15} + T^3 d_{2,15} + d_{2,16} - \\ 2 T d_{2,16} + T^2 d_{2,16} - d_{2,17} + T d_{2,17} + d_{2,18} - f_{2,4} + 3 T f_{2,4} - 3 T^2 f_{2,4} + T^3 f_{2,4}, \\ \theta == \frac{5 T}{4} - \frac{T^2}{2} + T d_{2,2} + d_{2,3} + T d_{2,4} + d_{2,5} + 4 T d_{2,6} - 4 T^2 d_{2,6} + 2 d_{2,7} - 4 T d_{2,7} - 4 d_{2,8} + 2 T d_{2,9} - \\ 2 T^2 d_{2,9} + d_{2,10} - 2 T d_{2,10} - 2 d_{2,11} + 18 T d_{2,15} - 36 T^2 d_{2,15} + 18 T^3 d_{2,15} + 6 d_{2,16} - 24 T d_{2,16} + \\ 18 T^2 d_{2,16} - 12 d_{2,17} + 18 T d_{2,17} + 18 d_{2,18} + 6 T d_{2,19} - 12 T^2 d_{2,19} + 6 T^3 d_{2,19} + 2 d_{2,20} - 8 T d_{2,20} + \\ 6 T^2 d_{2,20} - 4 d_{2,21} + 6 T d_{2,21} + 6 d_{2,22} + T f_{2,2} + 4 T f_{2,3} - 4 T^2 f_{2,3} + 18 T f_{2,4} - 36 T^2 f_{2,4} + 18 T^3 f_{2,4} \left. \right\}$$

In[]:= **{sol} = Solve[eqns, unknowns]**

Solve: Equations may not give solutions for all "solve" variables.

$$\text{Out[]} = \left\{ \left\{ \begin{aligned} c_{2,1} &\rightarrow -\frac{c_{2,2}}{2} - \frac{c_{2,5}}{2}, c_{2,3} \rightarrow -\frac{c_{2,2}}{T} - c_{2,5}, c_{2,4} \rightarrow 0, c_{2,6} \rightarrow 0, c_{2,8} \rightarrow -\frac{(1-T)c_{2,7}}{T} - \frac{(1-T)c_{2,10}}{2T}, \\ c_{2,9} &\rightarrow 0, c_{2,11} \rightarrow -c_{2,7} - \frac{(1+T)c_{2,10}}{2T}, c_{2,12} \rightarrow 0, c_{2,13} \rightarrow 0, c_{2,14} \rightarrow 0, c_{2,15} \rightarrow 0, \\ c_{2,17} &\rightarrow -\frac{1}{4} - \frac{(1-T)c_{2,16}}{T}, c_{2,18} \rightarrow -\frac{-1-2T+3T^2}{24T^2}, c_{2,19} \rightarrow 0, c_{2,20} \rightarrow -\frac{1}{8}, c_{2,21} \rightarrow -\frac{-1-2T}{8T}, \\ c_{2,22} &\rightarrow -\frac{1+T-2T^2}{24T^2} - \frac{(1-T)c_{2,16}}{T}, c_{2,23} \rightarrow 0, c_{2,24} \rightarrow 0, c_{2,25} \rightarrow -\frac{1}{8}, c_{2,26} \rightarrow -\frac{-2-T}{24T} - c_{2,16}, \\ c_{2,27} &\rightarrow 0, c_{2,28} \rightarrow 0, c_{2,29} \rightarrow 0, c_{2,30} \rightarrow 0, d_{2,1} \rightarrow \frac{c_{2,2}}{2} + \frac{c_{2,5}}{2}, d_{2,2} \rightarrow -c_{2,2}, \\ d_{2,3} &\rightarrow Tc_{2,2} + c_{2,5}, d_{2,4} \rightarrow 0, d_{2,5} \rightarrow -c_{2,5}, d_{2,6} \rightarrow 0, d_{2,7} \rightarrow -\frac{1}{4} - Tc_{2,7} - (-1+T)c_{2,10}, \\ d_{2,8} &\rightarrow \frac{1}{8}(-1+T) - (T-T^2)c_{2,7} - \frac{1}{2}(-1+3T-2T^2)c_{2,10}, d_{2,9} \rightarrow 0, d_{2,10} \rightarrow \frac{1}{4} - c_{2,10}, \\ d_{2,11} &\rightarrow \frac{1-T}{8} + Tc_{2,7} - \frac{1}{2}(1-3T)c_{2,10}, d_{2,12} \rightarrow 0, d_{2,13} \rightarrow 0, d_{2,14} \rightarrow 0, d_{2,15} \rightarrow 0, \\ d_{2,16} &\rightarrow \frac{1+T}{8} - Tc_{2,16}, d_{2,17} \rightarrow \frac{1}{8}(-1-T^2) - (T-T^2)c_{2,16}, d_{2,18} \rightarrow \frac{1}{24}(-3+2T+T^2), d_{2,19} \rightarrow 0, \\ d_{2,20} &\rightarrow -\frac{1}{8}, d_{2,21} \rightarrow \frac{2+T}{8}, d_{2,22} \rightarrow \frac{1}{24}(5-T-4T^2) - (T-T^2)c_{2,16}, d_{2,23} \rightarrow 0, d_{2,24} \rightarrow 0, d_{2,25} \rightarrow -\frac{1}{8}, \\ d_{2,26} &\rightarrow \frac{1}{24}(-2-T) + Tc_{2,16}, d_{2,27} \rightarrow 0, d_{2,28} \rightarrow 0, d_{2,29} \rightarrow 0, d_{2,30} \rightarrow 0, e_{2,1} \rightarrow -\frac{c_{2,2}}{2} - \frac{c_{2,5}}{2}, \\ e_{2,2} &\rightarrow -c_{2,10}, e_{2,3} \rightarrow 0, e_{2,4} \rightarrow 0, f_{2,1} \rightarrow \frac{c_{2,2}}{2} + \frac{c_{2,5}}{2}, f_{2,2} \rightarrow -\frac{1}{4} + c_{2,10}, f_{2,3} \rightarrow 0, f_{2,4} \rightarrow 0 \end{aligned} \right\} \right\}$$

In[]:= **sol /. (a_ -> b_) :-> (a = b)**

$$\text{Out[]} = \left\{ \left\{ \begin{aligned} &-\frac{c_{2,2}}{2} - \frac{c_{2,5}}{2}, -\frac{c_{2,2}}{T} - c_{2,5}, 0, 0, -\frac{(1-T)c_{2,7}}{T} - \frac{(1-T)c_{2,10}}{2T}, 0, -c_{2,7} - \frac{(1+T)c_{2,10}}{2T}, 0, 0, \\ &0, 0, -\frac{1}{4} - \frac{(1-T)c_{2,16}}{T}, -\frac{-1-2T+3T^2}{24T^2}, 0, -\frac{1}{8}, -\frac{-1-2T}{8T}, -\frac{1+T-2T^2}{24T^2} - \frac{(1-T)c_{2,16}}{T}, \\ &0, 0, -\frac{1}{8}, -\frac{-2-T}{24T} - c_{2,16}, 0, 0, 0, 0, \frac{c_{2,2}}{2} + \frac{c_{2,5}}{2}, -c_{2,2}, Tc_{2,2} + c_{2,5}, 0, -c_{2,5}, 0, \\ &-\frac{1}{4} - Tc_{2,7} - (-1+T)c_{2,10}, \frac{1}{8}(-1+T) - (T-T^2)c_{2,7} - \frac{1}{2}(-1+3T-2T^2)c_{2,10}, 0, \frac{1}{4} - c_{2,10}, \\ &\frac{1-T}{8} + Tc_{2,7} - \frac{1}{2}(1-3T)c_{2,10}, 0, 0, 0, 0, \frac{1+T}{8} - Tc_{2,16}, \frac{1}{8}(-1-T^2) - (T-T^2)c_{2,16}, \\ &\frac{1}{24}(-3+2T+T^2), 0, -\frac{1}{8}, \frac{2+T}{8}, \frac{1}{24}(5-T-4T^2) - (T-T^2)c_{2,16}, 0, 0, -\frac{1}{8}, \\ &\frac{1}{24}(-2-T) + Tc_{2,16}, 0, 0, 0, 0, -\frac{c_{2,2}}{2} - \frac{c_{2,5}}{2}, -c_{2,10}, 0, 0, \frac{c_{2,2}}{2} + \frac{c_{2,5}}{2}, -\frac{1}{4} + c_{2,10}, 0, 0 \end{aligned} \right\} \right\}$$

In[*]:= Cases [{R_{1,2}, R̄_{1,2}, C₁, C̄₁}, (c | d | e | f)_{sk,-}, ∞] // Union

Out[*]:= {C_{2,2}, C_{2,5}, C_{2,7}, C_{2,10}, C_{2,16}}

In[*]:= {Z1, Z2} = ZF /@ {Knot [10, 106], Knot [12, NonAlternating, 369]}

KnotTheory: Loading precomputed data in KnotTheory/12N.dts.

KnotTheory: The GaussCode to PD conversion was written by Siddarth Sankaran at the University of Toronto in the summer of 2005.

$$\text{Out[*]} = \left\{ \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{T^4}{1 - 4T + 9T^2 - 15T^3 + 17T^4 - 15T^5 + 9T^6 - 4T^7 + T^8}, \right. \right. \\
 \left. \left. \begin{aligned}
 & \theta, \in \text{Series} \left[\theta, (3 - 20T + 69T^2 - 161T^3 + 272T^4 - 328T^5 + 225T^6 + 92T^7 - \right. \right. \\
 & \quad 548T^8 + 952T^9 - 1113T^{10} + 980T^{11} - 668T^{12} + 349T^{13} - 135T^{14} + 36T^{15} - 5T^{16}) / \\
 & \quad (2 - 16T + 68T^2 - 204T^3 + 470T^4 - 872T^5 + 1338T^6 - 1720T^7 + 1870T^8 - 1720T^9 + \\
 & \quad \quad \left. 1338T^{10} - 872T^{11} + 470T^{12} - 204T^{13} + 68T^{14} - 16T^{15} + 2T^{16}), \right. \\
 & \quad (3 - 40T + 264T^2 - 1128T^3 + 3437T^4 - 7552T^5 + 10297T^6 + 2304T^7 - 67324T^8 + 259472T^9 - \\
 & \quad \quad 699066T^{10} + 1539252T^{11} - 2919131T^{12} + 4882760T^{13} - 7290870T^{14} + 9779044T^{15} - \\
 & \quad \quad 11816854T^{16} + 12877354T^{17} - 12651386T^{18} + 11191592T^{19} - 8896165T^{20} + 6336738T^{21} - \\
 & \quad \quad 4030390T^{22} + 2278962T^{23} - 1139320T^{24} + 500046T^{25} - 190857T^{26} + 62504T^{27} - 17215T^{28} + \\
 & \quad \quad 3862T^{29} - 668T^{30} + 80T^{31} - 5T^{32} - 32C_{2,2} + 480TC_{2,2} - 3696T^2C_{2,2} + 19448T^3C_{2,2} - \\
 & \quad \quad 78192T^4C_{2,2} + 254496T^5C_{2,2} - 693960T^6C_{2,2} + 1620216T^7C_{2,2} - 3284656T^8C_{2,2} + \\
 & \quad \quad 5831784T^9C_{2,2} - 9103728T^{10}C_{2,2} + 12483640T^{11}C_{2,2} - 14922472T^{12}C_{2,2} + 15241728T^{13}C_{2,2} - \\
 & \quad \quad 12646416T^{14}C_{2,2} + 7205208T^{15}C_{2,2} - 7205208T^{17}C_{2,2} + 12646416T^{18}C_{2,2} - 15241728T^{19}C_{2,2} + \\
 & \quad \quad 14922472T^{20}C_{2,2} - 12483640T^{21}C_{2,2} + 9103728T^{22}C_{2,2} - 5831784T^{23}C_{2,2} + 3284656T^{24}C_{2,2} - \\
 & \quad \quad 1620216T^{25}C_{2,2} + 693960T^{26}C_{2,2} - 254496T^{27}C_{2,2} + 78192T^{28}C_{2,2} - 19448T^{29}C_{2,2} + \\
 & \quad \quad 3696T^{30}C_{2,2} - 480T^{31}C_{2,2} + 32T^{32}C_{2,2} - 32C_{2,5} + 480TC_{2,5} - 3696T^2C_{2,5} + 19448T^3C_{2,5} - \\
 & \quad \quad 78192T^4C_{2,5} + 254496T^5C_{2,5} - 693960T^6C_{2,5} + 1620216T^7C_{2,5} - 3284656T^8C_{2,5} + \\
 & \quad \quad 5831784T^9C_{2,5} - 9103728T^{10}C_{2,5} + 12483640T^{11}C_{2,5} - 14922472T^{12}C_{2,5} + 15241728T^{13}C_{2,5} - \\
 & \quad \quad 12646416T^{14}C_{2,5} + 7205208T^{15}C_{2,5} - 7205208T^{17}C_{2,5} + 12646416T^{18}C_{2,5} - 15241728T^{19}C_{2,5} + \\
 & \quad \quad 14922472T^{20}C_{2,5} - 12483640T^{21}C_{2,5} + 9103728T^{22}C_{2,5} - 5831784T^{23}C_{2,5} + 3284656T^{24}C_{2,5} - \\
 & \quad \quad 1620216T^{25}C_{2,5} + 693960T^{26}C_{2,5} - 254496T^{27}C_{2,5} + 78192T^{28}C_{2,5} - 19448T^{29}C_{2,5} + \\
 & \quad \quad 3696T^{30}C_{2,5} - 480T^{31}C_{2,5} + 32T^{32}C_{2,5} - 24C_{2,10} + 352TC_{2,10} - 2648T^2C_{2,10} + 13592T^3C_{2,10} - \\
 & \quad \quad 53208T^4C_{2,10} + 168192T^5C_{2,10} - 443688T^6C_{2,10} + 995864T^7C_{2,10} - 1920832T^8C_{2,10} + \\
 & \quad \quad 3187896T^9C_{2,10} - 4506304T^{10}C_{2,10} + 5249976T^{11}C_{2,10} - 4549000T^{12}C_{2,10} + 1601312T^{13}C_{2,10} + \\
 & \quad \quad 3879856T^{14}C_{2,10} - 11310184T^{15}C_{2,10} + 19225392T^{16}C_{2,10} - 25720600T^{17}C_{2,10} + \\
 & \quad \quad 29172688T^{18}C_{2,10} - 28882144T^{19}C_{2,10} + 25295944T^{20}C_{2,10} - 19717304T^{21}C_{2,10} + \\
 & \quad \quad 13701152T^{22}C_{2,10} - 8475672T^{23}C_{2,10} + 4648480T^{24}C_{2,10} - 2244568T^{25}C_{2,10} + 944232T^{26}C_{2,10} - \\
 & \quad \quad 340800T^{27}C_{2,10} + 103176T^{28}C_{2,10} - 25304T^{29}C_{2,10} + 4744T^{30}C_{2,10} - 608T^{31}C_{2,10} + 40T^{32}C_{2,10}) / \\
 & \quad (8 - 128T + 1056T^2 - 5984T^3 + 26064T^4 - 92544T^5 + 277584T^6 - 720096T^7 + 1642328T^8 - \\
 & \quad \quad 3332448T^9 + 6069152T^{10} - 9986912T^{11} + 14922472T^{12} - 20322304T^{13} + 25292832T^{14} - \\
 & \quad \quad 28820832T^{15} + 30099512T^{16} - 28820832T^{17} + 25292832T^{18} - 20322304T^{19} + \\
 & \quad \quad 14922472T^{20} - 9986912T^{21} + 6069152T^{22} - 3332448T^{23} + 1642328T^{24} - 720096T^{25} + \\
 & \quad \quad 277584T^{26} - 92544T^{27} + 26064T^{28} - 5984T^{29} + 1056T^{30} - 128T^{31} + 8T^{32}) \left. \right] \right\},
 \end{aligned}$$

$$E_{\{\} \rightarrow \{1\}} \left[\frac{T^4}{1 - 4T + 9T^2 - 15T^3 + 17T^4 - 15T^5 + 9T^6 - 4T^7 + T^8}, \right.$$

0,

$$\in \text{Series} \left[0, \right.$$

$$\left. \left(3 - 20T + 69T^2 - 161T^3 + 272T^4 - 328T^5 + 225T^6 + 92T^7 - 548T^8 + \right. \right.$$

$$\left. \left. 952T^9 - 1113T^{10} + 980T^{11} - 668T^{12} + 349T^{13} - 135T^{14} + 36T^{15} - 5T^{16} \right) / \right.$$

$$\left. \left(2 - 16T + 68T^2 - 204T^3 + 470T^4 - 872T^5 + 1338T^6 - 1720T^7 + 1870T^8 - 1720T^9 + \right. \right.$$

$$\left. \left. 1338T^{10} - 872T^{11} + 470T^{12} - 204T^{13} + 68T^{14} - 16T^{15} + 2T^{16} \right), \right.$$

$$\left. \left(3 - 40T + 264T^2 - 1120T^3 + 3333T^4 - 6896T^5 + 7641T^6 + 9944T^7 - 83404T^8 + 283088T^9 - \right. \right.$$

$$\left. \left. 716082T^{10} + 1514140T^{11} - 2796883T^{12} + 4607952T^{13} - 6839214T^{14} + 9183044T^{15} - \right. \right.$$

$$\left. \left. 11164950T^{16} + 12281354T^{17} - 12199730T^{18} + 10916784T^{19} - 8773917T^{20} + 6311626T^{21} - \right. \right.$$

$$\left. \left. 4047406T^{22} + 2302578T^{23} - 1155400T^{24} + 507686T^{25} - 193513T^{26} + 63160T^{27} - 17319T^{28} + \right. \right.$$

$$\left. \left. 3870T^{29} - 668T^{30} + 80T^{31} - 5T^{32} - 32c_{2,2} + 480Tc_{2,2} - 3696T^2c_{2,2} + 19448T^3c_{2,2} - \right. \right.$$

$$\left. \left. 78192T^4c_{2,2} + 254496T^5c_{2,2} - 693960T^6c_{2,2} + 1620216T^7c_{2,2} - 3284656T^8c_{2,2} + \right. \right.$$

$$\left. \left. 5831784T^9c_{2,2} - 9103728T^{10}c_{2,2} + 12483640T^{11}c_{2,2} - 14922472T^{12}c_{2,2} + 15241728T^{13}c_{2,2} - \right. \right.$$

$$\left. \left. 12646416T^{14}c_{2,2} + 7205208T^{15}c_{2,2} - 7205208T^{17}c_{2,2} + 12646416T^{18}c_{2,2} - 15241728T^{19}c_{2,2} + \right. \right.$$

$$\left. \left. 14922472T^{20}c_{2,2} - 12483640T^{21}c_{2,2} + 9103728T^{22}c_{2,2} - 5831784T^{23}c_{2,2} + 3284656T^{24}c_{2,2} - \right. \right.$$

$$\left. \left. 1620216T^{25}c_{2,2} + 693960T^{26}c_{2,2} - 254496T^{27}c_{2,2} + 78192T^{28}c_{2,2} - 19448T^{29}c_{2,2} + \right. \right.$$

$$\left. \left. 3696T^{30}c_{2,2} - 480T^{31}c_{2,2} + 32T^{32}c_{2,2} - 32c_{2,5} + 480Tc_{2,5} - 3696T^2c_{2,5} + 19448T^3c_{2,5} - \right. \right.$$

$$\left. \left. 78192T^4c_{2,5} + 254496T^5c_{2,5} - 693960T^6c_{2,5} + 1620216T^7c_{2,5} - 3284656T^8c_{2,5} + \right. \right.$$

$$\left. \left. 5831784T^9c_{2,5} - 9103728T^{10}c_{2,5} + 12483640T^{11}c_{2,5} - 14922472T^{12}c_{2,5} + 15241728T^{13}c_{2,5} - \right. \right.$$

$$\left. \left. 12646416T^{14}c_{2,5} + 7205208T^{15}c_{2,5} - 7205208T^{17}c_{2,5} + 12646416T^{18}c_{2,5} - 15241728T^{19}c_{2,5} + \right. \right.$$

$$\left. \left. 14922472T^{20}c_{2,5} - 12483640T^{21}c_{2,5} + 9103728T^{22}c_{2,5} - 5831784T^{23}c_{2,5} + 3284656T^{24}c_{2,5} - \right. \right.$$

$$\left. \left. 1620216T^{25}c_{2,5} + 693960T^{26}c_{2,5} - 254496T^{27}c_{2,5} + 78192T^{28}c_{2,5} - 19448T^{29}c_{2,5} + \right. \right.$$

$$\left. \left. 3696T^{30}c_{2,5} - 480T^{31}c_{2,5} + 32T^{32}c_{2,5} - 24c_{2,10} + 352Tc_{2,10} - 2648T^2c_{2,10} + 13592T^3c_{2,10} - \right. \right.$$

$$\left. \left. 53208T^4c_{2,10} + 168192T^5c_{2,10} - 443688T^6c_{2,10} + 995864T^7c_{2,10} - 1920832T^8c_{2,10} + \right. \right.$$

$$\left. \left. 3187896T^9c_{2,10} - 4506304T^{10}c_{2,10} + 5249976T^{11}c_{2,10} - 4549000T^{12}c_{2,10} + 1601312T^{13}c_{2,10} + \right. \right.$$

$$\left. \left. 3879856T^{14}c_{2,10} - 11310184T^{15}c_{2,10} + 19225392T^{16}c_{2,10} - 25720600T^{17}c_{2,10} + \right. \right.$$

$$\left. \left. 29172688T^{18}c_{2,10} - 28882144T^{19}c_{2,10} + 25295944T^{20}c_{2,10} - 19717304T^{21}c_{2,10} + \right. \right.$$

$$\left. \left. 13701152T^{22}c_{2,10} - 8475672T^{23}c_{2,10} + 4648480T^{24}c_{2,10} - 2244568T^{25}c_{2,10} + 944232T^{26}c_{2,10} - \right. \right.$$

$$\left. \left. 340800T^{27}c_{2,10} + 103176T^{28}c_{2,10} - 25304T^{29}c_{2,10} + 4744T^{30}c_{2,10} - 608T^{31}c_{2,10} + 40T^{32}c_{2,10} \right) / \right.$$

$$\left. \left(8 - 128T + 1056T^2 - 5984T^3 + 26064T^4 - 92544T^5 + 277584T^6 - 720096T^7 + 1642328T^8 - \right. \right.$$

$$\left. \left. 3332448T^9 + 6069152T^{10} - 9986912T^{11} + 14922472T^{12} - 20322304T^{13} + 25292832T^{14} - \right. \right.$$

$$\left. \left. 28820832T^{15} + 30099512T^{16} - 28820832T^{17} + 25292832T^{18} - 20322304T^{19} + \right. \right.$$

$$\left. \left. 14922472T^{20} - 9986912T^{21} + 6069152T^{22} - 3332448T^{23} + 1642328T^{24} - 720096T^{25} + \right. \right.$$

$$\left. \left. 277584T^{26} - 92544T^{27} + 26064T^{28} - 5984T^{29} + 1056T^{30} - 128T^{31} + 8T^{32} \right) \right] \left. \right\}$$

In[*]:= {Z1[[3, 2]] == Z2[[3, 2]], Z1[[3, 3]] - Z2[[3, 3]]} // Simplify

$$\text{Out[*]} = \left\{ \text{True}, - \frac{(-1 + T)^4 T^3 (1 - 3T + 2T^2 + 5T^3 - 12T^4 + 18T^5 - 12T^6 + 5T^7 + 2T^8 - 3T^9 + T^{10})}{(1 - T + T^2) (1 - 3T + 5T^2 - 7T^3 + 5T^4 - 3T^5 + T^6)^3} \right\}$$

$$\text{In[*]:= } \{C_1, \bar{C}_1, \text{CF}[\text{CF}[\text{Rp}_{1,2} /. T \rightarrow T^{-1}][[3, 3]] - \text{CF}[\bar{\text{Rp}}_{1,2}][[3, 3]]\} / . \\ \{C_{2,2} \rightarrow 0, C_{2,5} \rightarrow 0, C_{2,10} \rightarrow 1/8, C_{2,7} \rightarrow -1/8, C_{2,16} \rightarrow 1/8\}$$

$$\text{Out[*]:= } \{E_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, 0, \in \text{Series} \left[0, \frac{p_1 x_1}{2}, -\frac{1}{8} p_1 x_1 \right] \right], \\ E_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, 0, \in \text{Series} \left[0, -\frac{1}{2} p_1 x_1, -\frac{1}{8} p_1 x_1 \right] \right], 0\}$$

$$\text{In[*]:= } \{C_{2,2} = 0, C_{2,5} = 0, C_{2,10} = 1/8, C_{2,7} = -1/8, C_{2,16} = 1/8\}; \\ \{R_{1,2}, \bar{R}_{1,2}, R_{1,2} /. T \rightarrow T^{-1}, C_1, \bar{C}_1\} // \text{CF} // \text{Column}$$

$$E_{\{\} \rightarrow \{1,2\}} \left[\sqrt{T}, (-1+T) p_1 x_2 + (1-T) p_2 x_2, \right. \\ \in \text{Series} \left[0, \frac{1}{2} T p_1^2 x_1 x_2 - \frac{1}{2} T p_1 p_2 x_1 x_2 + \frac{1}{4} (T-T^2) p_1^2 x_2^2 + \frac{1}{4} (-T+T^2) p_1 p_2 x_2^2, \right. \\ \left. -\frac{1}{8} T p_1^2 x_1 x_2 + \frac{1}{8} T p_1 p_2 x_1 x_2 + \frac{1}{8} T p_1^3 x_1^2 x_2 - \frac{1}{8} T p_1^2 p_2 x_1^2 x_2 + \frac{1}{16} (-T+T^2) p_1^2 x_2^2 + \right. \\ \left. \frac{1}{16} (T-T^2) p_1 p_2 x_2^2 + \frac{1}{8} (T-3T^2) p_1^3 x_1 x_2^2 + \frac{1}{8} (-T+4T^2) p_1^2 p_2 x_1 x_2^2 - \frac{1}{8} T^2 p_1 p_2^2 x_1 x_2^2 + \right. \\ \left. \frac{1}{24} (T-4T^2+3T^3) p_1^3 x_2^3 + \frac{1}{24} (-T+5T^2-4T^3) p_1^2 p_2 x_2^3 + \frac{1}{24} (-T^2+T^3) p_1 p_2^2 x_2^3 \right] \\ E_{\{\} \rightarrow \{1,2\}} \left[\frac{1}{\sqrt{T}}, \frac{(1-T) p_1 x_2}{T} + \frac{(-1+T) p_2 x_2}{T}, \in \text{Series} \left[0, -\frac{p_1^2 x_1 x_2}{2T} + \frac{p_1 p_2 x_1 x_2}{2T} + \frac{(1-T) p_1^2 x_2^2}{4T^2} + \frac{(-1+T) p_1 p_2 x_2^2}{4T^2}, \right. \right. \\ \left. \left. -\frac{p_1^2 x_1 x_2}{8T} + \frac{p_1 p_2 x_1 x_2}{8T} + \frac{p_1^3 x_1^2 x_2}{8T} - \frac{p_1^2 p_2 x_1^2 x_2}{8T} + \frac{(1-T) p_1^2 x_2^2}{16T^2} + \frac{(-1+T) p_1 p_2 x_2^2}{16T^2} + \frac{(-3+T) p_1^3 x_1 x_2^2}{8T^2} + \right. \right. \\ \left. \left. \frac{(4-T) p_1^2 p_2 x_1 x_2^2}{8T^2} - \frac{p_1 p_2^2 x_1 x_2^2}{8T^2} + \frac{(3-4T+T^2) p_1^3 x_2^3}{24T^3} + \frac{(-4+5T-T^2) p_1^2 p_2 x_2^3}{24T^3} + \frac{(1-T) p_1 p_2^2 x_2^3}{24T^3} \right] \right] \\ E_{\{\} \rightarrow \{1,2\}} \left[\sqrt{\frac{1}{T}}, \frac{(1-T) p_1 x_2}{T} + \frac{(-1+T) p_2 x_2}{T}, \right. \\ \in \text{Series} \left[0, \frac{p_1^2 x_1 x_2}{2T} - \frac{p_1 p_2 x_1 x_2}{2T} + \frac{(-1+T) p_1^2 x_2^2}{4T^2} + \frac{(1-T) p_1 p_2 x_2^2}{4T^2}, -\frac{p_1^2 x_1 x_2}{8T} + \frac{p_1 p_2 x_1 x_2}{8T} + \frac{p_1^3 x_1^2 x_2}{8T} - \frac{p_1^2 p_2 x_1^2 x_2}{8T} + \frac{(1-T) p_1^2 x_2^2}{16T^2} + \right. \\ \left. \frac{(-1+T) p_1 p_2 x_2^2}{16T^2} + \frac{(-3+T) p_1^3 x_1 x_2^2}{8T^2} + \frac{(4-T) p_1^2 p_2 x_1 x_2^2}{8T^2} - \frac{p_1 p_2^2 x_1 x_2^2}{8T^2} + \frac{(3-4T+T^2) p_1^3 x_2^3}{24T^3} + \frac{(-4+5T-T^2) p_1^2 p_2 x_2^3}{24T^3} + \frac{(1-T) p_1 p_2^2 x_2^3}{24T^3} \right] \\ E_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, 0, \in \text{Series} \left[0, \frac{p_1 x_1}{2}, -\frac{1}{8} p_1 x_1 \right] \right] \\ E_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, 0, \in \text{Series} \left[0, -\frac{1}{2} p_1 x_1, -\frac{1}{8} p_1 x_1 \right] \right]$$

$$\text{In[*]:= } \text{CF}[\text{R}_{1,2} /. T \rightarrow T^{-1}][[3, 3]] - \text{CF}[\bar{\text{R}}_{1,2}][[3, 3]]$$

$$\text{Out[*]:= } 0$$

$$\text{In[*]:= } \text{Factor} / @ \text{Rp}_{1,2}[[3]]$$

$$\text{Out[*]:= } \in \text{Series} \left[0, \frac{p_1 (p_1 - p_2) x_2 (2 T x_1 - x_2 + T x_2)}{4 T}, \right. \\ \frac{1}{48 T^2} p_1 (p_1 - p_2) x_2 (-6 T^2 x_1 + 6 T^2 p_1 x_1^2 + 3 T x_2 - 3 T^2 x_2 - 6 T p_1 x_1 x_2 - \\ \left. 6 T^2 p_1 x_1 x_2 + 6 T^2 p_2 x_1 x_2 + 2 p_1 x_2^2 + 4 T p_1 x_2^2 - 6 T^2 p_1 x_2^2 - 4 T p_2 x_2^2 + 4 T^2 p_2 x_2^2) \right]$$

$$\text{In[*]:= } \text{Simplify} / @ \text{Rp}_{1,2}[[3]]$$

$$\text{Out[*]:= } \in \text{Series} \left[0, \frac{p_1 (p_1 - p_2) x_2 (2 T x_1 + (-1+T) x_2)}{4 T}, -\frac{1}{48 T^2} p_1 (p_1 - p_2) x_2 \right. \\ \left. (-6 T^2 p_1 x_1^2 + 6 T x_1 (T + (1+T) p_1 x_2 - T p_2 x_2) + (-1+T) x_2 (2 (1+3 T) p_1 x_2 + T (3-4 p_2 x_2))) \right]$$

In[]:= **RMoves**

Out[]:= {True, True, True, True, True, True, True, True, True}

Solving for R, C, \$k = 3

In[]:= **\$k = 3;**

{R_{1,2}, C₁}

Out[]:= $\{E_{\{1,2\}} \left[\sqrt{T}, (-1 + T) p_1 x_2 + (1 - T) p_2 x_2, \right.$

$\in \text{Series} \left[0, \frac{1}{2} T p_1^2 x_1 x_2 - \frac{1}{2} T p_1 p_2 x_1 x_2 + \frac{1}{4} (T - T^2) p_1^2 x_2^2 + \frac{1}{4} (-T + T^2) p_1 p_2 x_2^2, \right.$

$-\frac{1}{8} T p_1^2 x_1 x_2 + \frac{1}{8} T p_1 p_2 x_1 x_2 + \frac{1}{8} T p_1^3 x_1^2 x_2 - \frac{1}{8} T p_1^2 p_2 x_1^2 x_2 + \frac{1}{16} (-T + T^2) p_1^2 x_2^2 +$

$\frac{1}{16} (T - T^2) p_1 p_2 x_2^2 + \frac{1}{8} (T - 3 T^2) p_1^3 x_1 x_2^2 + \frac{1}{8} (-T + 4 T^2) p_1^2 p_2 x_1 x_2^2 - \frac{1}{8} T^2 p_1 p_2^2 x_1 x_2^2 +$

$\frac{1}{24} (T - 4 T^2 + 3 T^3) p_1^3 x_2^3 + \frac{1}{24} (-T + 5 T^2 - 4 T^3) p_1^2 p_2 x_2^3 + \frac{1}{24} (-T^2 + T^3) p_1 p_2^2 x_2^3,$

$C_{3,1} + p_1 x_1 C_{3,2} + p_1 x_2 (C_{3,2} - T C_{3,2} + T C_{3,3}) + p_2 x_1 C_{3,4} + p_2 x_2 (C_{3,4} - T C_{3,4} + T C_{3,5}) + p_1^2 x_1^2 C_{3,6} +$

$p_1^2 x_1 x_2 (2 C_{3,6} - 2 T C_{3,6} + T C_{3,7}) + p_1^2 x_2^2 (C_{3,6} - 2 T C_{3,6} + T^2 C_{3,6} + T C_{3,7} - T^2 C_{3,7} + T^2 C_{3,8}) +$

$p_1 p_2 x_1^2 C_{3,9} + p_1 p_2 x_1 x_2 (2 C_{3,9} - 2 T C_{3,9} + T C_{3,10}) +$

$p_1 p_2 x_2^2 (C_{3,9} - 2 T C_{3,9} + T^2 C_{3,9} + T C_{3,10} - T^2 C_{3,10} + T^2 C_{3,11}) + p_2^2 x_1^2 C_{3,12} +$

$p_2^2 x_1 x_2 (2 C_{3,12} - 2 T C_{3,12} + T C_{3,13}) + p_2^2 x_2^2 (C_{3,12} - 2 T C_{3,12} + T^2 C_{3,12} + T C_{3,13} - T^2 C_{3,13} + T^2 C_{3,14}) +$

$p_1^3 x_1^3 C_{3,15} + p_1^3 x_1^2 x_2 (3 C_{3,15} - 3 T C_{3,15} + T C_{3,16}) +$

$p_1^3 x_1 x_2^2 (3 C_{3,15} - 6 T C_{3,15} + 3 T^2 C_{3,15} + 2 T C_{3,16} - 2 T^2 C_{3,16} + T^2 C_{3,17}) + p_1^3 x_2^3$

$(C_{3,15} - 3 T C_{3,15} + 3 T^2 C_{3,15} - T^3 C_{3,15} + T C_{3,16} - 2 T^2 C_{3,16} + T^3 C_{3,16} + T^2 C_{3,17} - T^3 C_{3,17} + T^3 C_{3,18}) +$

$p_1^2 p_2 x_1^3 C_{3,19} + p_1^2 p_2 x_1^2 x_2 (3 C_{3,19} - 3 T C_{3,19} + T C_{3,20}) +$

$p_1^2 p_2 x_1 x_2^2 (3 C_{3,19} - 6 T C_{3,19} + 3 T^2 C_{3,19} + 2 T C_{3,20} - 2 T^2 C_{3,20} + T^2 C_{3,21}) + p_1^2 p_2 x_2^3$

$(C_{3,19} - 3 T C_{3,19} + 3 T^2 C_{3,19} - T^3 C_{3,19} + T C_{3,20} - 2 T^2 C_{3,20} + T^3 C_{3,20} + T^2 C_{3,21} - T^3 C_{3,21} + T^3 C_{3,22}) +$

$p_1 p_2^2 x_1^3 C_{3,23} + p_1 p_2^2 x_1^2 x_2 (3 C_{3,23} - 3 T C_{3,23} + T C_{3,24}) +$

$p_1 p_2^2 x_1 x_2^2 (3 C_{3,23} - 6 T C_{3,23} + 3 T^2 C_{3,23} + 2 T C_{3,24} - 2 T^2 C_{3,24} + T^2 C_{3,25}) + p_1 p_2^2 x_2^3$

$(C_{3,23} - 3 T C_{3,23} + 3 T^2 C_{3,23} - T^3 C_{3,23} + T C_{3,24} - 2 T^2 C_{3,24} + T^3 C_{3,24} + T^2 C_{3,25} - T^3 C_{3,25} + T^3 C_{3,26}) +$

$p_2^3 x_1^3 C_{3,27} + p_2^3 x_1^2 x_2 (3 C_{3,27} - 3 T C_{3,27} + T C_{3,28}) +$

$p_2^3 x_1 x_2^2 (3 C_{3,27} - 6 T C_{3,27} + 3 T^2 C_{3,27} + 2 T C_{3,28} - 2 T^2 C_{3,28} + T^2 C_{3,29}) + p_2^3 x_2^3$

$(C_{3,27} - 3 T C_{3,27} + 3 T^2 C_{3,27} - T^3 C_{3,27} + T C_{3,28} - 2 T^2 C_{3,28} + T^3 C_{3,28} + T^2 C_{3,29} - T^3 C_{3,29} + T^3 C_{3,30}) +$

$p_1^4 x_1^4 C_{3,31} + p_1^4 x_1^3 x_2 (4 C_{3,31} - 4 T C_{3,31} + T C_{3,32}) +$

$p_1^4 x_1^2 x_2^2 (6 C_{3,31} - 12 T C_{3,31} + 6 T^2 C_{3,31} + 3 T C_{3,32} - 3 T^2 C_{3,32} + T^2 C_{3,33}) +$

$p_1^4 x_1 x_2^3 (4 C_{3,31} - 12 T C_{3,31} + 12 T^2 C_{3,31} - 4 T^3 C_{3,31} + 3 T C_{3,32} - 6 T^2 C_{3,32} + 3 T^3 C_{3,32} + 2 T^2 C_{3,33} -$

$2 T^3 C_{3,33} + T^3 C_{3,34}) + p_1^4 x_2^4 (C_{3,31} - 4 T C_{3,31} + 6 T^2 C_{3,31} - 4 T^3 C_{3,31} + T^4 C_{3,31} + T C_{3,32} -$

$3 T^2 C_{3,32} + 3 T^3 C_{3,32} - T^4 C_{3,32} + T^2 C_{3,33} - 2 T^3 C_{3,33} + T^4 C_{3,33} + T^3 C_{3,34} - T^4 C_{3,34} + T^4 C_{3,35}) +$

$p_1^3 p_2 x_1^4 C_{3,36} + p_1^3 p_2 x_1^3 x_2 (4 C_{3,36} - 4 T C_{3,36} + T C_{3,37}) +$

$p_1^3 p_2 x_1^2 x_2^2 (6 C_{3,36} - 12 T C_{3,36} + 6 T^2 C_{3,36} + 3 T C_{3,37} - 3 T^2 C_{3,37} + T^2 C_{3,38}) +$

$p_1^3 p_2 x_1 x_2^3 (4 C_{3,36} - 12 T C_{3,36} + 12 T^2 C_{3,36} - 4 T^3 C_{3,36} + 3 T C_{3,37} - 6 T^2 C_{3,37} + 3 T^3 C_{3,37} + 2 T^2 C_{3,38} -$

$$\begin{aligned}
 & 2 T^3 C_{3,38} + T^3 C_{3,39} + p_1^3 p_2 x_2^4 (C_{3,36} - 4 T C_{3,36} + 6 T^2 C_{3,36} - 4 T^3 C_{3,36} + T^4 C_{3,36} + T C_{3,37} - \\
 & 3 T^2 C_{3,37} + 3 T^3 C_{3,37} - T^4 C_{3,37} + T^2 C_{3,38} - 2 T^3 C_{3,38} + T^4 C_{3,38} + T^3 C_{3,39} - T^4 C_{3,39} + T^4 C_{3,40}) + \\
 & p_1^2 p_2^2 x_1^4 C_{3,41} + p_1^2 p_2^2 x_1^3 x_2 (4 C_{3,41} - 4 T C_{3,41} + T C_{3,42}) + \\
 & p_1^2 p_2^2 x_1^2 x_2^2 (6 C_{3,41} - 12 T C_{3,41} + 6 T^2 C_{3,41} + 3 T C_{3,42} - 3 T^2 C_{3,42} + T^2 C_{3,43}) + \\
 & p_1^2 p_2^2 x_1 x_2^3 (4 C_{3,41} - 12 T C_{3,41} + 12 T^2 C_{3,41} - 4 T^3 C_{3,41} + 3 T C_{3,42} - 6 T^2 C_{3,42} + 3 T^3 C_{3,42} + 2 T^2 C_{3,43} - \\
 & 2 T^3 C_{3,43} + T^3 C_{3,44}) + p_1^2 p_2^2 x_2^4 (C_{3,41} - 4 T C_{3,41} + 6 T^2 C_{3,41} - 4 T^3 C_{3,41} + T^4 C_{3,41} + T C_{3,42} - \\
 & 3 T^2 C_{3,42} + 3 T^3 C_{3,42} - T^4 C_{3,42} + T^2 C_{3,43} - 2 T^3 C_{3,43} + T^4 C_{3,43} + T^3 C_{3,44} - T^4 C_{3,44} + T^4 C_{3,45}) + \\
 & p_1 p_2^3 x_1^4 C_{3,46} + p_1 p_2^3 x_1^3 x_2 (4 C_{3,46} - 4 T C_{3,46} + T C_{3,47}) + \\
 & p_1 p_2^3 x_1^2 x_2^2 (6 C_{3,46} - 12 T C_{3,46} + 6 T^2 C_{3,46} + 3 T C_{3,47} - 3 T^2 C_{3,47} + T^2 C_{3,48}) + \\
 & p_1 p_2^3 x_1 x_2^3 (4 C_{3,46} - 12 T C_{3,46} + 12 T^2 C_{3,46} - 4 T^3 C_{3,46} + \\
 & 3 T C_{3,47} - 6 T^2 C_{3,47} + 3 T^3 C_{3,47} + 2 T^2 C_{3,48} - 2 T^3 C_{3,48} + T^3 C_{3,49}) + \\
 & p_1 p_2^3 x_2^4 (C_{3,46} - 4 T C_{3,46} + 6 T^2 C_{3,46} - 4 T^3 C_{3,46} + T^4 C_{3,46} + T C_{3,47} - 3 T^2 C_{3,47} + \\
 & 3 T^3 C_{3,47} - T^4 C_{3,47} + T^2 C_{3,48} - 2 T^3 C_{3,48} + T^4 C_{3,48} + T^3 C_{3,49} - T^4 C_{3,49} + T^4 C_{3,50}) + \\
 & p_2^4 x_1^4 C_{3,51} + p_2^4 x_1^3 x_2 (4 C_{3,51} - 4 T C_{3,51} + T C_{3,52}) + \\
 & p_2^4 x_1^2 x_2^2 (6 C_{3,51} - 12 T C_{3,51} + 6 T^2 C_{3,51} + 3 T C_{3,52} - 3 T^2 C_{3,52} + T^2 C_{3,53}) + \\
 & p_2^4 x_1 x_2^3 (4 C_{3,51} - 12 T C_{3,51} + 12 T^2 C_{3,51} - 4 T^3 C_{3,51} + \\
 & 3 T C_{3,52} - 6 T^2 C_{3,52} + 3 T^3 C_{3,52} + 2 T^2 C_{3,53} - 2 T^3 C_{3,53} + T^3 C_{3,54}) + \\
 & p_2^4 x_2^4 (C_{3,51} - 4 T C_{3,51} + 6 T^2 C_{3,51} - 4 T^3 C_{3,51} + T^4 C_{3,51} + T C_{3,52} - 3 T^2 C_{3,52} + 3 T^3 C_{3,52} - \\
 & T^4 C_{3,52} + T^2 C_{3,53} - 2 T^3 C_{3,53} + T^4 C_{3,53} + T^3 C_{3,54} - T^4 C_{3,54} + T^4 C_{3,55}) \Big], \\
 & E_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2}, -\frac{1}{8} p_1 x_1, e_{3,1} + p_1 x_1 e_{3,2} + p_1^2 x_1^2 e_{3,3} + p_1^3 x_1^3 e_{3,4} + p_1^4 x_1^4 e_{3,5} \right] \right] \Big\}
 \end{aligned}$$

In[*]:= unknowns = Cases [{R_{1,2}, R̄_{1,2}, C₁, C̄₁}, (c | d | e | f)_{k,_, ∞}] // Union

Out[*]:= {C_{3,1}, C_{3,2}, C_{3,3}, C_{3,4}, C_{3,5}, C_{3,6}, C_{3,7}, C_{3,8}, C_{3,9}, C_{3,10}, C_{3,11}, C_{3,12}, C_{3,13}, C_{3,14}, C_{3,15}, C_{3,16}, C_{3,17}, C_{3,18}, C_{3,19}, C_{3,20}, C_{3,21}, C_{3,22}, C_{3,23}, C_{3,24}, C_{3,25}, C_{3,26}, C_{3,27}, C_{3,28}, C_{3,29}, C_{3,30}, C_{3,31}, C_{3,32}, C_{3,33}, C_{3,34}, C_{3,35}, C_{3,36}, C_{3,37}, C_{3,38}, C_{3,39}, C_{3,40}, C_{3,41}, C_{3,42}, C_{3,43}, C_{3,44}, C_{3,45}, C_{3,46}, C_{3,47}, C_{3,48}, C_{3,49}, C_{3,50}, C_{3,51}, C_{3,52}, C_{3,53}, C_{3,54}, C_{3,55}, d_{3,1}, d_{3,2}, d_{3,3}, d_{3,4}, d_{3,5}, d_{3,6}, d_{3,7}, d_{3,8}, d_{3,9}, d_{3,10}, d_{3,11}, d_{3,12}, d_{3,13}, d_{3,14}, d_{3,15}, d_{3,16}, d_{3,17}, d_{3,18}, d_{3,19}, d_{3,20}, d_{3,21}, d_{3,22}, d_{3,23}, d_{3,24}, d_{3,25}, d_{3,26}, d_{3,27}, d_{3,28}, d_{3,29}, d_{3,30}, d_{3,31}, d_{3,32}, d_{3,33}, d_{3,34}, d_{3,35}, d_{3,36}, d_{3,37}, d_{3,38}, d_{3,39}, d_{3,40}, d_{3,41}, d_{3,42}, d_{3,43}, d_{3,44}, d_{3,45}, d_{3,46}, d_{3,47}, d_{3,48}, d_{3,49}, d_{3,50}, d_{3,51}, d_{3,52}, d_{3,53}, d_{3,54}, d_{3,55}, e_{3,1}, e_{3,2}, e_{3,3}, e_{3,4}, e_{3,5}, f_{3,1}, f_{3,2}, f_{3,3}, f_{3,4}, f_{3,5}}

In[]:= Short[errors = CCF /@ Cases[RMoves, a_ == b_ => a - b], 25]

Out[]//Short=

$$\left\{ \frac{1}{192} \left(-72 T^2 p_1^3 x_1 x_2 x_3 + 72 T^3 p_1^3 x_1 x_2 x_3 + 72 T^2 p_1^2 p_2 x_1 x_2 x_3 - 72 T^3 p_1^2 p_2 x_1 x_2 x_3 - 24 T^2 p_1 p_2^2 x_1 x_2 x_3 + \right. \right.$$

$$24 T^3 p_1 p_2^2 x_1 x_2 x_3 + 24 T^2 p_1^2 p_3 x_1 x_2 x_3 - 24 T^3 p_1^2 p_3 x_1 x_2 x_3 + 84 T^2 p_1^4 x_1^2 x_2 x_3 - 84 T^3 p_1^4 x_1^2 x_2 x_3 -$$

$$120 T^2 p_1^3 p_2 x_1^2 x_2 x_3 + 120 T^3 p_1^3 p_2 x_1^2 x_2 x_3 + 48 T^2 p_1^2 p_2^2 x_1^2 x_2 x_3 - 48 T^3 p_1^2 p_2^2 x_1^2 x_2 x_3 -$$

$$12 T^2 p_1^3 p_3 x_1^2 x_2 x_3 + 12 T^3 p_1^3 p_3 x_1^2 x_2 x_3 - 36 T^2 p_1^3 x_2^2 x_3 + 36 T^3 p_1^3 x_2^2 x_3 + 48 T^2 p_1^2 p_2 x_2^2 x_3 -$$

$$48 T^3 p_1^2 p_2 x_2^2 x_3 - 12 T^2 p_1 p_2^2 x_2^2 x_3 + 36 T^3 p_1 p_2^2 x_2^2 x_3 - 24 T^4 p_1 p_2^2 x_2^2 x_3 - 24 T^3 p_1 p_2 p_3 x_2^2 x_3 +$$

$$24 T^4 p_1 p_2 p_3 x_2^2 x_3 + 108 T^2 p_1^4 x_1 x_2^2 x_3 - 204 T^3 p_1^4 x_1 x_2^2 x_3 + 96 T^4 p_1^4 x_1 x_2^2 x_3 - 156 T^2 p_1^3 p_2 x_1 x_2^2 x_3 +$$

$$324 T^3 p_1^3 p_2 x_1 x_2^2 x_3 - 168 T^4 p_1^3 p_2 x_1 x_2^2 x_3 + 60 T^2 p_1^2 p_2^2 x_1 x_2^2 x_3 - 156 T^3 p_1^2 p_2^2 x_1 x_2^2 x_3 +$$

$$96 T^4 p_1^2 p_2^2 x_1 x_2^2 x_3 + 12 T^3 p_1 p_2^3 x_1 x_2^2 x_3 - 12 T^4 p_1 p_2^3 x_1 x_2^2 x_3 - 12 T^2 p_1^3 p_3 x_1 x_2^2 x_3 + \ll 8105 \gg +$$

$$768 T^8 p_1 p_3^3 x_3^4 c_{3,54} - 768 T^6 p_2 p_3^3 x_3^4 c_{3,54} + 1536 T^7 p_2 p_3^3 x_3^4 c_{3,54} - 768 T^8 p_2 p_3^3 x_3^4 c_{3,54} +$$

$$768 T^4 p_2^4 x_2^3 c_{3,55} - 768 T^5 p_2^4 x_2^3 c_{3,55} + 1152 T^4 p_2^4 x_2^3 c_{3,55} - 2304 T^5 p_2^4 x_2^3 c_{3,55} +$$

$$1152 T^6 p_2^4 x_2^3 c_{3,55} + 768 T^4 p_2^4 x_2^3 c_{3,55} - 2304 T^5 p_2^4 x_2^3 c_{3,55} + 2304 T^6 p_2^4 x_2^3 c_{3,55} -$$

$$768 T^7 p_2^4 x_2^3 c_{3,55} + 192 T^4 p_1^4 x_3^4 c_{3,55} - 768 T^5 p_1^4 x_3^4 c_{3,55} + 1152 T^6 p_1^4 x_3^4 c_{3,55} - 768 T^7 p_1^4 x_3^4 c_{3,55} +$$

$$192 T^8 p_1^4 x_3^4 c_{3,55} + 768 T^5 p_1^3 p_3 x_3^4 c_{3,55} - 2304 T^6 p_1^3 p_3 x_3^4 c_{3,55} + 2304 T^7 p_1^3 p_3 x_3^4 c_{3,55} -$$

$$768 T^8 p_1^3 p_3 x_3^4 c_{3,55} - 768 T^5 p_2^3 p_3 x_3^4 c_{3,55} + 2304 T^6 p_2^3 p_3 x_3^4 c_{3,55} - 2304 T^7 p_2^3 p_3 x_3^4 c_{3,55} +$$

$$768 T^8 p_2^3 p_3 x_3^4 c_{3,55} + 1152 T^6 p_1^2 p_3^2 x_3^4 c_{3,55} - 2304 T^7 p_1^2 p_3^2 x_3^4 c_{3,55} + 1152 T^8 p_1^2 p_3^2 x_3^4 c_{3,55} -$$

$$1152 T^6 p_2^2 p_3^2 x_3^4 c_{3,55} + 2304 T^7 p_2^2 p_3^2 x_3^4 c_{3,55} - 1152 T^8 p_2^2 p_3^2 x_3^4 c_{3,55} + 768 T^7 p_1 p_3^3 x_3^4 c_{3,55} -$$

$$768 T^8 p_1 p_3^3 x_3^4 c_{3,55} - 768 T^7 p_2 p_3^3 x_3^4 c_{3,55} + 768 T^8 p_2 p_3^3 x_3^4 c_{3,55} \Big), \frac{\ll 1 \gg}{\ll 1 \gg}, \ll 6 \gg, \frac{\ll 1 \gg}{48 \ll 1 \gg} \Big\}$$

In[]:= Short[# , 10] &[eqns =

Thread[0 == Union@@(CoefficientRules[# , {x1, x2, x3, p1, p2, p3}][[; ; , 2] & /@ errors)]]]

Out[]//Short=

$$\left\{ \theta == c_{3,4} - T c_{3,4}, \theta == -c_{3,4} + T c_{\ll 1 \gg}, \ll 490 \gg, \theta == \ll 1 \gg, \right.$$

$$\theta == \frac{9}{16} + \frac{5 T}{16} - \frac{19 T^2}{16} + \frac{3 T^3}{16} + T^2 d_{3,6} + T d_{3,7} + d_{3,8} + T^2 d_{3,9} + T d_{3,10} + d_{3,11} + T^2 d_{3,12} + T d_{3,13} + d_{3,14} +$$

$$9 T^2 d_{3,15} - 9 T^3 d_{3,15} + 6 T d_{3,16} - 9 T^2 d_{3,16} + 3 d_{3,17} - 9 T d_{3,17} - 9 d_{3,18} + 6 T^2 d_{3,19} - 6 T^3 d_{3,19} +$$

$$4 T d_{3,20} - 6 T^2 d_{3,20} + 2 d_{3,21} - 6 T d_{3,21} - 6 d_{3,22} + 3 T^2 d_{3,23} - 3 T^3 d_{3,23} + 2 T d_{3,24} - 3 T^2 d_{3,24} + d_{3,25} -$$

$$3 T d_{3,25} - 3 d_{3,26} + \ll 14 \gg + 72 T d_{3,34} + 72 d_{3,35} + 36 T^2 d_{3,36} - 72 T^3 d_{3,36} + 36 T^4 d_{3,36} + 18 T d_{3,37} -$$

$$54 T^2 d_{3,37} + 36 T^3 d_{3,37} + 6 d_{3,38} - 36 T d_{3,38} + 36 T^2 d_{3,38} - 18 d_{3,39} + 36 T d_{3,39} + 36 d_{3,40} + 12 T^2 d_{3,41} -$$

$$24 T^3 d_{3,41} + 12 T^4 d_{3,41} + 6 T d_{3,42} - 18 T^2 d_{3,42} + 12 T^3 d_{3,42} + 2 d_{3,43} - 12 T d_{3,43} + 12 T^2 d_{3,43} -$$

$$6 d_{3,44} + 12 T d_{3,44} + 12 d_{3,45} + T^2 f_{3,3} + 9 T^2 f_{3,4} - 9 T^3 f_{3,4} + 72 T^2 f_{3,5} - 144 T^3 f_{3,5} + 72 T^4 f_{3,5} \Big\}$$

In[]:= {sol} = Solve[eqns, unknowns]

Solve: Equations may not give solutions for all "solve" variables.

$$\text{Out[]} = \left\{ \left\{ c_{3,1} \rightarrow -\frac{c_{3,2}}{2} - \frac{c_{3,5}}{2}, c_{3,3} \rightarrow -\frac{c_{3,2}}{T} - c_{3,5}, c_{3,4} \rightarrow \theta, c_{3,6} \rightarrow \theta, c_{3,8} \rightarrow -\frac{(1-T) c_{3,7}}{T} - \frac{(1-T) c_{3,10}}{2 T}, \right. \right.$$

$$c_{3,9} \rightarrow \theta, c_{3,11} \rightarrow -c_{3,7} - \frac{(1+T) c_{3,10}}{2 T}, c_{3,12} \rightarrow \theta, c_{3,13} \rightarrow \theta, c_{3,14} \rightarrow \theta, c_{3,15} \rightarrow \theta,$$

$$c_{3,17} \rightarrow \frac{3}{16} - \frac{(1-T) c_{3,16}}{T}, c_{3,18} \rightarrow -\frac{1+4 T-5 T^2}{48 T^2}, c_{3,19} \rightarrow \theta, c_{3,20} \rightarrow \frac{1}{16}, c_{3,21} \rightarrow -\frac{1+3 T}{16 T}, \left. \right\}$$

$$\begin{aligned}
c_{3,22} &\rightarrow -\frac{-1-3T+4T^2}{48T^2} - \frac{(1-T)c_{3,16}}{T}, c_{3,23} \rightarrow 0, c_{3,24} \rightarrow 0, c_{3,25} \rightarrow \frac{1}{16}, c_{3,26} \rightarrow -\frac{2+T}{48T} - c_{3,16}, \\
c_{3,27} &\rightarrow 0, c_{3,28} \rightarrow 0, c_{3,29} \rightarrow 0, c_{3,30} \rightarrow 0, c_{3,31} \rightarrow 0, c_{3,33} \rightarrow -\frac{7}{32} + \frac{3(-1+T)c_{3,32}}{2T}, \\
c_{3,34} &\rightarrow -\frac{-2+T}{8T} - \frac{(-1+2T-T^2)c_{3,32}}{T^2}, c_{3,35} \rightarrow -\frac{-1+18T-15T^2-2T^3}{192T^3} - \frac{(1-3T+3T^2-T^3)c_{3,32}}{2T^3}, \\
c_{3,36} &\rightarrow 0, c_{3,37} \rightarrow -\frac{1}{48}, c_{3,38} \rightarrow -\frac{-1-10T}{32T}, c_{3,39} \rightarrow -\frac{1+17T-6T^2}{48T^2}, \\
c_{3,40} &\rightarrow -\frac{-1-25T+17T^2+9T^3}{192T^3} - \frac{(1-2T+T^2)c_{3,32}}{T^2}, c_{3,41} \rightarrow 0, c_{3,42} \rightarrow 0, c_{3,43} \rightarrow -\frac{1}{8}, \\
c_{3,44} &\rightarrow \frac{7}{48T}, c_{3,45} \rightarrow -\frac{3-T-2T^2}{64T^2} + \frac{3(-1+T)c_{3,32}}{2T}, c_{3,46} \rightarrow 0, c_{3,47} \rightarrow 0, c_{3,48} \rightarrow 0, \\
c_{3,49} &\rightarrow -\frac{1}{48}, c_{3,50} \rightarrow -\frac{-3-T}{192T} - c_{3,32}, c_{3,51} \rightarrow 0, c_{3,52} \rightarrow 0, c_{3,53} \rightarrow 0, c_{3,54} \rightarrow 0, c_{3,55} \rightarrow 0, \\
d_{3,1} &\rightarrow \frac{c_{3,2}}{2} + \frac{c_{3,5}}{2}, d_{3,2} \rightarrow -c_{3,2}, d_{3,3} \rightarrow Tc_{3,2} + c_{3,5}, d_{3,4} \rightarrow 0, d_{3,5} \rightarrow -c_{3,5}, d_{3,6} \rightarrow 0, \\
d_{3,7} &\rightarrow -Tc_{3,7} - (-1+T)c_{3,10}, d_{3,8} \rightarrow -\left((T-T^2)c_{3,7}\right) - \frac{1}{2}(-1+3T-2T^2)c_{3,10}, d_{3,9} \rightarrow 0, \\
d_{3,10} &\rightarrow -c_{3,10}, d_{3,11} \rightarrow Tc_{3,7} - \frac{1}{2}(1-3T)c_{3,10}, d_{3,12} \rightarrow 0, d_{3,13} \rightarrow 0, d_{3,14} \rightarrow 0, d_{3,15} \rightarrow 0, \\
d_{3,16} &\rightarrow \frac{1-T}{16} - Tc_{3,16}, d_{3,17} \rightarrow \frac{1}{16}(-2-2T+T^2) - (T-T^2)c_{3,16}, d_{3,18} \rightarrow \frac{1}{48}(-5+4T+T^2), \\
d_{3,19} &\rightarrow 0, d_{3,20} \rightarrow -\frac{1}{16}, d_{3,21} \rightarrow \frac{3+T}{16}, d_{3,22} \rightarrow \frac{1}{48}(7-9T+2T^2) - (T-T^2)c_{3,16}, \\
d_{3,23} &\rightarrow 0, d_{3,24} \rightarrow 0, d_{3,25} \rightarrow -\frac{1}{16}, d_{3,26} \rightarrow \frac{1}{48}(-2+5T) + Tc_{3,16}, d_{3,27} \rightarrow 0, \\
d_{3,28} &\rightarrow 0, d_{3,29} \rightarrow 0, d_{3,30} \rightarrow 0, d_{3,31} \rightarrow 0, d_{3,32} \rightarrow \frac{1}{48}(-1+T) - Tc_{3,32}, \\
d_{3,33} &\rightarrow \frac{1}{32}(6+2T-T^2) + \frac{3}{2}(-T+T^2)c_{3,32}, d_{3,34} \rightarrow \frac{1}{48}(5-9T-3T^2+T^3) - (T-2T^2+T^3)c_{3,32}, \\
d_{3,35} &\rightarrow \frac{1}{192}(-4-7T+6T^2+7T^3-2T^4) - \frac{1}{2}(T-3T^2+3T^3-T^4)c_{3,32}, \\
d_{3,36} &\rightarrow 0, d_{3,37} \rightarrow \frac{1}{48}, d_{3,38} \rightarrow \frac{1}{32}(-10-T), d_{3,39} \rightarrow \frac{1}{48}(-6+17T+T^2), \\
d_{3,40} &\rightarrow \frac{1}{192}(13+5T-13T^2-5T^3) - (-T+2T^2-T^3)c_{3,32}, d_{3,41} \rightarrow 0, d_{3,42} \rightarrow 0, \\
d_{3,43} &\rightarrow \frac{1}{8}, d_{3,44} \rightarrow -\frac{7T}{48}, d_{3,45} \rightarrow \frac{1}{64}(-4+3T+T^2) + \frac{3}{2}(-1+T)Tc_{3,32}, d_{3,46} \rightarrow 0, \\
d_{3,47} &\rightarrow 0, d_{3,48} \rightarrow 0, d_{3,49} \rightarrow \frac{1}{48}, d_{3,50} \rightarrow \frac{1}{192}(3-7T) + Tc_{3,32}, d_{3,51} \rightarrow 0, d_{3,52} \rightarrow 0, \\
d_{3,53} &\rightarrow 0, d_{3,54} \rightarrow 0, d_{3,55} \rightarrow 0, e_{3,1} \rightarrow -\frac{c_{3,2}}{2} - \frac{c_{3,5}}{2}, e_{3,2} \rightarrow -c_{3,10}, e_{3,3} \rightarrow 0,
\end{aligned}$$

$$e_{3,4} \rightarrow 0, e_{3,5} \rightarrow 0, f_{3,1} \rightarrow \frac{c_{3,2}}{2} + \frac{c_{3,5}}{2}, f_{3,2} \rightarrow c_{3,10}, f_{3,3} \rightarrow 0, f_{3,4} \rightarrow 0, f_{3,5} \rightarrow 0 \}} \}$$

In[*]:= sol /. (a_ -> b_) :-> (a = b)

$$\text{Out[*]} = \left\{ -\frac{c_{3,2}}{2} - \frac{c_{3,5}}{2}, -\frac{c_{3,2}}{T} - c_{3,5}, 0, 0, -\frac{(1-T)c_{3,7}}{T} - \frac{(1-T)c_{3,10}}{2T}, 0, -c_{3,7} - \frac{(1+T)c_{3,10}}{2T}, 0, 0, 0, \right. \\ 0, \frac{3}{16} - \frac{(1-T)c_{3,16}}{T}, -\frac{1+4T-5T^2}{48T^2}, 0, \frac{1}{16}, -\frac{1+3T}{16T}, -\frac{-1-3T+4T^2}{48T^2} - \frac{(1-T)c_{3,16}}{T}, 0, \\ 0, \frac{1}{16}, -\frac{2+T}{48T} - c_{3,16}, 0, 0, 0, 0, 0, -\frac{7}{32} + \frac{3(-1+T)c_{3,32}}{2T}, -\frac{-2+T}{8T} - \frac{(-1+2T-T^2)c_{3,32}}{T^2}, \\ -\frac{-1+18T-15T^2-2T^3}{192T^3} - \frac{(1-3T+3T^2-T^3)c_{3,32}}{2T^3}, 0, -\frac{1}{48}, -\frac{-1-10T}{32T}, -\frac{1+17T-6T^2}{48T^2}, \\ -\frac{-1-25T+17T^2+9T^3}{192T^3} - \frac{(1-2T+T^2)c_{3,32}}{T^2}, 0, 0, -\frac{1}{8}, \frac{7}{48T}, -\frac{3-T-2T^2}{64T^2} + \frac{3(-1+T)c_{3,32}}{2T}, \\ 0, 0, 0, -\frac{1}{48}, -\frac{-3-T}{192T} - c_{3,32}, 0, 0, 0, 0, 0, \frac{c_{3,2}}{2} + \frac{c_{3,5}}{2}, -c_{3,2}, T c_{3,2} + c_{3,5}, 0, \\ -c_{3,5}, 0, -T c_{3,7} - (-1+T)c_{3,10}, -((T-T^2)c_{3,7}) - \frac{1}{2}(-1+3T-2T^2)c_{3,10}, 0, -c_{3,10}, \\ T c_{3,7} - \frac{1}{2}(1-3T)c_{3,10}, 0, 0, 0, 0, \frac{1-T}{16} - T c_{3,16}, \frac{1}{16}(-2-2T+T^2) - (T-T^2)c_{3,16}, \\ \frac{1}{48}(-5+4T+T^2), 0, -\frac{1}{16}, \frac{3+T}{16}, \frac{1}{48}(7-9T+2T^2) - (T-T^2)c_{3,16}, \\ 0, 0, -\frac{1}{16}, \frac{1}{48}(-2+5T) + T c_{3,16}, 0, 0, 0, 0, 0, \frac{1}{48}(-1+T) - T c_{3,32}, \\ \frac{1}{32}(6+2T-T^2) + \frac{3}{2}(-T+T^2)c_{3,32}, \frac{1}{48}(5-9T-3T^2+T^3) - (T-2T^2+T^3)c_{3,32}, \\ \frac{1}{192}(-4-7T+6T^2+7T^3-2T^4) - \frac{1}{2}(T-3T^2+3T^3-T^4)c_{3,32}, 0, \frac{1}{48}, \frac{1}{32}(-10-T), \\ \frac{1}{48}(-6+17T+T^2), \frac{1}{192}(13+5T-13T^2-5T^3) - (-T+2T^2-T^3)c_{3,32}, 0, 0, \frac{1}{8}, \\ -\frac{7T}{48}, \frac{1}{64}(-4+3T+T^2) + \frac{3}{2}(-1+T)T c_{3,32}, 0, 0, 0, \frac{1}{48}, \frac{1}{192}(3-7T) + T c_{3,32}, \\ 0, 0, 0, 0, 0, -\frac{c_{3,2}}{2} - \frac{c_{3,5}}{2}, -c_{3,10}, 0, 0, 0, \frac{c_{3,2}}{2} + \frac{c_{3,5}}{2}, c_{3,10}, 0, 0, 0 \}$$

In[*]:= Cases[{R1,2, R1,2, C1, C1}, (c | d | e | f)_{sk,-}, inf] // Union

Out[*]:= {C3,2, C3,5, C3,7, C3,10, C3,16, C3,32}

In[*]:= CF[{C1, (C1[[3, 4]] /. T -> T^-1) + C1[[3, 4]], (Rp1,2 /. T -> T^-1)[[3, 4]] + R1,2[[3, 4]]} /. {C3,32 -> 1/48, C3,16 -> -1/16, C3,10 -> -C3,7}]

Out[*]:= {E_{1} -> {1}}[sqrt(T), 0, Series[0, p1 x1 / 2, -1/8 p1 x1, 1/2 (-c3,2 - c3,5) + p1 x1 c3,7], 0, 0]

$$In[*]:= CF [Rp_{1,2} / \cdot \{c_{3,32} \rightarrow 1 / 48, c_{3,16} \rightarrow -1 / 16, c_{3,10} \rightarrow -c_{3,7}\}]$$

$$Out[*]:= E_{\{\} \rightarrow \{1,2\}} \left[1, 0, \in Series \left[0, \frac{1}{2} p_1^2 x_1 x_2 - \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{(-1+T) p_1^2 x_2^2}{4 T} + \frac{(1-T) p_1 p_2 x_2^2}{4 T}, \right. \right. \\ - \frac{1}{8} p_1^2 x_1 x_2 + \frac{1}{8} p_1 p_2 x_1 x_2 + \frac{1}{8} p_1^3 x_1^2 x_2 - \frac{1}{8} p_1^2 p_2 x_1^2 x_2 + \frac{(1-T) p_1^2 x_2^2}{16 T} + \\ \frac{(-1+T) p_1 p_2 x_2^2}{16 T} + \frac{(-1-T) p_1^3 x_1 x_2^2}{8 T} + \frac{(1+2 T) p_1^2 p_2 x_1 x_2^2}{8 T} - \frac{1}{8} p_1 p_2^2 x_1 x_2^2 + \\ \frac{(1+2 T-3 T^2) p_1^3 x_2^3}{24 T^2} + \frac{(-1-4 T+5 T^2) p_1^2 p_2 x_2^3}{24 T^2} + \frac{(1-T) p_1 p_2^2 x_2^3}{12 T}, \\ - \frac{1}{16} p_1^3 x_1^2 x_2 + \frac{1}{16} p_1^2 p_2 x_1^2 x_2 + \frac{1}{48} p_1^4 x_1^3 x_2 - \frac{1}{48} p_1^3 p_2 x_1^3 x_2 + \frac{(1+2 T) p_1^3 x_1 x_2^2}{16 T} + \\ \frac{(-1-3 T) p_1^2 p_2 x_1 x_2^2}{16 T} + \frac{1}{16} p_1 p_2^2 x_1 x_2^2 + \frac{(-1-6 T) p_1^4 x_1^2 x_2^2}{32 T} + \frac{(1+10 T) p_1^3 p_2 x_1^2 x_2^2}{32 T} - \\ \frac{1}{8} p_1^2 p_2^2 x_1^2 x_2^2 + \frac{(-1-4 T+5 T^2) p_1^3 x_2^3}{48 T^2} + \frac{(1+6 T-7 T^2) p_1^2 p_2 x_2^3}{48 T^2} + \frac{(-1+T) p_1 p_2^2 x_2^3}{24 T} + \\ \frac{(1+10 T-5 T^2) p_1^4 x_1 x_2^3}{48 T^2} + \frac{(-1-17 T+6 T^2) p_1^3 p_2 x_1 x_2^3}{48 T^2} + \frac{7 p_1^2 p_2^2 x_1 x_2^3}{48 T} - \frac{1}{48} p_1 p_2^3 x_1 x_2^3 + \\ \frac{(-1-12 T+9 T^2+4 T^3) p_1^4 x_2^4}{192 T^3} + \frac{(1+21 T-9 T^2-13 T^3) p_1^3 p_2 x_2^4}{192 T^3} + \frac{(-3-T+4 T^2) p_1^2 p_2^2 x_2^4}{64 T^2} + \\ \left. \left. \frac{(1-T) p_1 p_2^3 x_2^4}{64 T} + p_1 x_1 c_{3,2} + \frac{1}{2} (-c_{3,2} - c_{3,5}) + p_2 x_2 c_{3,5} + \frac{p_1 x_2 (-c_{3,2} - T c_{3,5})}{T} + \right. \right. \\ \left. \left. p_1^2 x_1 x_2 c_{3,7} - p_1 p_2 x_1 x_2 c_{3,7} + \frac{p_1 p_2 x_2^2 (c_{3,7} - T c_{3,7})}{2 T} + \frac{p_1^2 x_2^2 (-c_{3,7} + T c_{3,7})}{2 T} \right] \right]$$

Fast ρ_1

$R_{ij}^s = T^{s/2} \rho (T^s - 1) (p_i - p_j) x_i x_j$
 $x p = p x - 1 \downarrow$
 $G_{x\beta} = \langle p_x x_\beta \rangle$ & with effort: $G_{x\beta} = \langle x_\beta x_x \rangle = G_{x\beta} - \int dx_\beta$
 $G_{1,\beta} = 0$
 $X_{ij}^s: \begin{cases} \text{row } i & \tilde{G}_{i,j,\beta} - G_{i+1,j,\beta} = 0 \Leftrightarrow G_{i,j,\beta} - G_{i+1,j,\beta} = r_{i,j,\beta} \\ \text{row } j & \tilde{G}_{j,\beta} - G_{j+1,\beta} - (T^s - 1)(G_{i+1,j,\beta} - \tilde{G}_{i,j,\beta}) = 0 \end{cases}$
 $B \in M_{2n \times (2n+1)}$
 $\Leftrightarrow T^s G_{j,\beta} - G_{j+1,\beta} + (1 - T^s) G_{i+1,j,\beta} = T^s r_{j,\beta}$
 $B = (\phi | A) \quad G = \begin{pmatrix} 0 & 0 & 0 \\ D & 0 & 0 \end{pmatrix} \quad BG = \begin{pmatrix} I_{2n \times 2n} & 0 \end{pmatrix}$
 $AD = I$

```

In[ ]:= PAB1[K_] := Module[{Cs, Rs, n, B, A, c, s, i, j, rho, G, rho1},
  {Cs, Rs} = List@@RVK[K]; n = Length[Cs];
  B = Table[0, {2 n, 2 n + 1}];
  Do[s = If[Head[c] === Xp, 1, -1]; {i, j} = List@@c;
    B[[i, {i, i + 1}]] = {1, -1}; B[[j, {j, j + 1, i + 1}]] = {1, -T^-s, T^-s - 1},
    {c, Cs}];
  rho = Det[A = B[[All, 2 ;;]]] // Factor;
  G = Prepend[Table[0, {2 n}][Inverse[A]];
  rho1 = Factor[1/2 Plus[
    Sum[s = If[Head[c] === Xp, 1, -1]; {i, j} = List@@c;
      s (2 G[[i, i]] G[[i, j]] - G[[i, i]] G[[j, j]] -
        G[[i, j]] G[[j, i]] + (1 - T^-s) (G[[i, j]]^2 - G[[i, j]] G[[j, j]])), {c, Cs}],
    Sum[Rs[[k]] G[[k, k]], {k, 2 n}]]];
  {rho, rho1} ]

```

```

In[ ]:= $k = 1; CF /@ {Rp_{1,2}, R\bar{p}_{1,2}, C_1, \bar{C}_1}

```

$$\text{Out[]} = \left\{ \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, \frac{1}{2} p_1^2 x_1 x_2 - \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{(-1+T) p_1^2 x_2^2}{4 T} + \frac{(1-T) p_1 p_2 x_2^2}{4 T} \right] \right], \right. \\
 \mathbb{E}_{\{\} \rightarrow \{1,2\}} \left[1, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1^2 x_1 x_2 + \frac{1}{2} p_1 p_2 x_1 x_2 + \frac{1}{4} (-1+T) p_1^2 x_2^2 + \frac{1}{4} (1-T) p_1 p_2 x_2^2 \right] \right], \\
 \left. \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\sqrt{T}, \theta, \in \text{Series} \left[\theta, \frac{p_1 x_1}{2} \right] \right], \mathbb{E}_{\{\} \rightarrow \{1\}} \left[\frac{1}{\sqrt{T}}, \theta, \in \text{Series} \left[\theta, -\frac{1}{2} p_1 x_1 \right] \right] \right\}$$

In[]:= **K = GST48;**

Alexander[K][T]

$$\text{Out[]}:= 13 - \frac{1}{T^8} + \frac{2}{T^7} - \frac{1}{T^6} - \frac{2}{T^4} + \frac{5}{T^3} - \frac{2}{T^2} - \frac{7}{T} - 7T - 2T^2 + 5T^3 - 2T^4 - T^6 + 2T^7 - T^8$$

In[]:= **Timing@PAB1[K]**

$$\text{Out[]}:= \left\{ 48.0938, \left\{ -\frac{(-1 + 2T - T^2 - T^3 + 2T^4 - T^5 + T^8)(-1 + T^3 - 2T^4 + T^5 + T^6 - 2T^7 + T^8)}{T^7}, \right. \right. \\ \left. - \left((-1 + T) (13 - 45T + 71T^2 - 71T^3 + 58T^4 - 35T^5 - 39T^6 + 101T^7 + 37T^8 - 335T^9 + 372T^{10} + 56T^{11} - \right. \right. \\ \left. \left. 506T^{12} + 478T^{13} - 114T^{14} - 81T^{15} - 31T^{16} + 204T^{17} - 270T^{18} + 210T^{19} + 8T^{20} - 328T^{21} + \right. \right. \\ \left. \left. 481T^{22} - 311T^{23} - 7T^{24} + 169T^{25} - 115T^{26} - 10T^{27} + 59T^{28} - 31T^{29} + T^{30} + 3T^{31}) \right) \right\} / \\ \left. \left(2(-1 + 2T - T^2 - T^3 + 2T^4 - T^5 + T^8)^2 (-1 + T^3 - 2T^4 + T^5 + T^6 - 2T^7 + T^8)^2 \right) \right\}$$

In[]:= **ZF[K][[3, 2]] // Factor**

$$\text{Out[]}:= -\frac{(-1 + T)^2 (-5 + 17T - 19T^2 + 21T^3 - 19T^4 + 12T^5 - 7T^6 + 3T^7 - T^8 - T^9 + T^{10})}{2(1 - 3T + 3T^2 - 3T^3 + 3T^4 - 3T^5 + T^6)^2}$$

The Dunfield Knots

In[]:= **Ks = ReadList["C:\\drorbn\\AcademicPensieve\\People\\Dunfield\\nmd_random_knots"] /.**

i_Integer -> i + 1;

tab = {};

In[]:= **Do[**

AppendTo[tab, Echo@Timing@{Crossings[K], PAB1[K]}],

{K, Ks[[{98, 144, 200, 288, 400, 576, 800, 998}]]}

]

» {2530.13, {100,

$$\left\{ -\frac{1}{T^{29}} (90 - 4191T + 93808T^2 - 1350157T^3 + 14094887T^4 - 114093181T^5 + 747334274T^6 - 4080812510T^7 + \right. \\ 18988434455T^8 - 76571119755T^9 + 271181538682T^{10} - 852587915221T^{11} + 2400574002517T^{12} - \\ 6097234930996T^{13} + 14054039062621T^{14} - 29545412051243T^{15} + 56886358621438T^{16} - \\ 100661418654577T^{17} + 164176135336778T^{18} - 247394236438275T^{19} + 345108115623752T^{20} - \\ 446366907831089T^{21} + 535954571148512T^{22} - 597914563591946T^{23} + 620084807002653T^{24} - \\ 597914563591946T^{25} + 535954571148512T^{26} - 446366907831089T^{27} + 345108115623752T^{28} - \\ 247394236438275T^{29} + 164176135336778T^{30} - 100661418654577T^{31} + 56886358621438T^{32} - \\ 29545412051243T^{33} + 14054039062621T^{34} - 6097234930996T^{35} + 2400574002517T^{36} - \\ 852587915221T^{37} + 271181538682T^{38} - 76571119755T^{39} + 18988434455T^{40} - 4080812510T^{41} + \\ 747334274T^{42} - 114093181T^{43} + 14094887T^{44} - 1350157T^{45} + 93808T^{46} - 4191T^{47} + 90T^{48}), \\ \left. - \left((-1 + T) (161937 - 14489697T + 635470366T^2 - 18224912736T^3 + 384751566717T^4 - \right. \right. \\ \left. \left. 6381329305196T^5 + 86658799856073T^6 - 991584058562206T^7 + 9763623993034797T^8 - \right. \right. \\ \left. \left. 84076719803317845T^9 + 641331937048382570T^{10} - 4378714116477072665T^{11} + \right. \right. \\ \left. \left. 26990183066997846721T^{12} - 151288917889407398042T^{13} + 775948734581632316171T^{14} - \right. \right. \\ \left. \left. 3660958964786586817214T^{15} + 15962504472342421264591T^{16} - \right. \right.$$

$$\begin{aligned}
 & 344\,516\,034\,368\,T^7 + 1\,779\,504\,363\,078\,T^8 - 8\,042\,174\,372\,557\,T^9 + 32\,231\,562\,387\,870\,T^{10} - \\
 & 115\,815\,717\,852\,178\,T^{11} + 376\,496\,389\,523\,755\,T^{12} - 1\,115\,760\,699\,354\,364\,T^{13} + 3\,034\,085\,808\,198\,831\,T^{14} - \\
 & 7\,613\,448\,663\,622\,029\,T^{15} + 17\,716\,466\,439\,842\,235\,T^{16} - 38\,398\,262\,636\,324\,625\,T^{17} + \\
 & 77\,817\,245\,375\,284\,936\,T^{18} - 147\,975\,161\,806\,008\,018\,T^{19} + 264\,864\,463\,654\,413\,778\,T^{20} - \\
 & 447\,537\,155\,866\,622\,680\,T^{21} + 715\,724\,452\,091\,768\,365\,T^{22} - 1\,085\,975\,248\,590\,733\,307\,T^{23} + \\
 & 1\,566\,793\,410\,493\,137\,029\,T^{24} - 2\,153\,782\,249\,322\,555\,994\,T^{25} + 2\,826\,132\,464\,730\,846\,217\,T^{26} - \\
 & 3\,545\,734\,448\,752\,219\,235\,T^{27} + 4\,259\,704\,526\,510\,564\,908\,T^{28} - 4\,906\,306\,554\,934\,041\,288\,T^{29} + \\
 & 5\,423\,374\,081\,718\,704\,899\,T^{30} - 5\,757\,666\,735\,070\,210\,053\,T^{31} + 5\,873\,314\,948\,586\,537\,617\,T^{32} - \\
 & 5\,757\,666\,735\,070\,210\,053\,T^{33} + 5\,423\,374\,081\,718\,704\,899\,T^{34} - 4\,906\,306\,554\,934\,041\,288\,T^{35} + \\
 & 4\,259\,704\,526\,510\,564\,908\,T^{36} - 3\,545\,734\,448\,752\,219\,235\,T^{37} + 2\,826\,132\,464\,730\,846\,217\,T^{38} - \\
 & 2\,153\,782\,249\,322\,555\,994\,T^{39} + 1\,566\,793\,410\,493\,137\,029\,T^{40} - 1\,085\,975\,248\,590\,733\,307\,T^{41} + \\
 & 715\,724\,452\,091\,768\,365\,T^{42} - 447\,537\,155\,866\,622\,680\,T^{43} + 264\,864\,463\,654\,413\,778\,T^{44} - \\
 & 147\,975\,161\,806\,008\,018\,T^{45} + 77\,817\,245\,375\,284\,936\,T^{46} - 38\,398\,262\,636\,324\,625\,T^{47} + \\
 & 17\,716\,466\,439\,842\,235\,T^{48} - 7\,613\,448\,663\,622\,029\,T^{49} + 3\,034\,085\,808\,198\,831\,T^{50} - \\
 & 1\,115\,760\,699\,354\,364\,T^{51} + 376\,496\,389\,523\,755\,T^{52} - 115\,815\,717\,852\,178\,T^{53} + 32\,231\,562\,387\,870\,T^{54} - \\
 & 8\,042\,174\,372\,557\,T^{55} + 1\,779\,504\,363\,078\,T^{56} - 344\,516\,034\,368\,T^{57} + 57\,373\,789\,206\,T^{58} - \\
 & 8\,038\,473\,748\,T^{59} + 919\,380\,688\,T^{60} - 82\,195\,664\,T^{61} + 5\,367\,456\,T^{62} - 226\,560\,T^{63} + 4608\,T^{64} , \\
 & - \left((-1 + T) \left(764\,116\,992 - 73\,158\,623\,232\,T + 3\,439\,280\,900\,096\,T^2 - 105\,991\,199\,410\,176\,T^3 + \right. \right. \\
 & \quad 2\,411\,758\,420\,522\,240\,T^4 - 43\,265\,721\,625\,530\,112\,T^5 + 638\,020\,949\,170\,066\,816\,T^6 - \\
 & \quad 7\,961\,634\,561\,647\,453\,888\,T^7 + 85\,885\,853\,452\,477\,144\,416\,T^8 - 814\,175\,390\,523\,043\,043\,968\,T^9 + \\
 & \quad 6\,871\,322\,681\,183\,645\,652\,800\,T^{10} - 52\,177\,107\,908\,117\,352\,155\,636\,T^{11} + \\
 & \quad 359\,619\,478\,550\,238\,576\,942\,049\,T^{12} - 2\,266\,403\,065\,259\,697\,821\,736\,183\,T^{13} + \\
 & \quad 13\,143\,201\,306\,546\,058\,953\,530\,311\,T^{14} - 70\,518\,330\,807\,768\,102\,869\,671\,279\,T^{15} + \\
 & \quad 351\,726\,387\,216\,396\,014\,463\,630\,626\,T^{16} - 1\,637\,674\,357\,805\,841\,857\,337\,754\,976\,T^{17} + \\
 & \quad 7\,144\,660\,870\,479\,205\,736\,629\,643\,564\,T^{18} - 29\,302\,592\,549\,386\,833\,488\,535\,105\,218\,T^{19} + \\
 & \quad 113\,316\,469\,918\,038\,034\,696\,584\,187\,421\,T^{20} - 414\,294\,640\,780\,190\,366\,123\,183\,273\,704\,T^{21} + \\
 & \quad 1\,435\,533\,832\,704\,614\,312\,670\,331\,372\,551\,T^{22} - 4\,724\,654\,254\,260\,323\,651\,567\,396\,492\,752\,T^{23} + \\
 & \quad 14\,800\,000\,214\,419\,554\,474\,111\,197\,032\,505\,T^{24} - 44\,207\,810\,510\,136\,684\,455\,610\,766\,427\,656\,T^{25} + \\
 & \quad 126\,132\,986\,368\,977\,801\,895\,667\,107\,693\,376\,T^{26} - 344\,303\,096\,798\,453\,368\,787\,237\,567\,797\,767\,T^{27} + \\
 & \quad 900\,482\,772\,131\,236\,131\,952\,212\,976\,513\,452\,T^{28} - 2\,259\,573\,209\,825\,075\,815\,100\,401\,976\,543\,734\,T^{29} + \\
 & \quad 5\,446\,874\,397\,323\,839\,791\,291\,117\,262\,648\,609\,T^{30} - 12\,628\,581\,960\,100\,582\,170\,440\,155\,599\,028\,804\,T^{31} + \\
 & \quad 28\,192\,311\,853\,538\,182\,576\,778\,400\,985\,589\,738\,T^{32} - 60\,663\,485\,819\,361\,596\,786\,806\,702\,208\,311\,878\,T^{33} + \\
 & \quad 125\,941\,203\,343\,849\,771\,021\,221\,802\,806\,059\,823\,T^{34} - 252\,492\,805\,759\,717\,905\,588\,003\,591\,595\,421\,685\, \\
 & \quad T^{35} + 489\,263\,930\,345\,678\,982\,510\,564\,678\,718\,329\,440\,T^{36} - \\
 & \quad 917\,064\,100\,815\,211\,332\,774\,194\,481\,298\,736\,932\,T^{37} + 1\,663\,971\,843\,658\,686\,665\,960\,740\,212\,328\,386\,843\, \\
 & \quad T^{38} - 2\,924\,749\,963\,944\,237\,154\,463\,125\,983\,005\,660\,912\,T^{39} + \\
 & \quad 4\,983\,273\,380\,191\,933\,723\,159\,515\,120\,306\,278\,817\,T^{40} - \\
 & \quad 8\,235\,522\,367\,538\,426\,167\,006\,116\,523\,796\,628\,747\,T^{41} + \\
 & \quad 13\,208\,887\,241\,278\,837\,769\,140\,976\,097\,887\,051\,079\,T^{42} - \\
 & \quad 20\,571\,650\,797\,712\,592\,739\,587\,918\,062\,152\,374\,105\,T^{43} + \\
 & \quad 31\,125\,041\,835\,670\,930\,074\,999\,605\,468\,452\,296\,875\,T^{44} - \\
 & \quad 45\,769\,815\,968\,979\,965\,730\,315\,734\,592\,525\,102\,595\,T^{45} + \\
 & \quad 65\,440\,575\,702\,872\,917\,402\,885\,102\,910\,814\,276\,276\,T^{46} - \\
 & \quad 91\,004\,484\,120\,189\,189\,288\,980\,845\,021\,373\,306\,390\,T^{47} + \\
 & \quad 123\,126\,761\,462\,996\,010\,695\,479\,232\,529\,009\,984\,922\,T^{48} - \\
 & \quad 162\,112\,905\,290\,510\,654\,438\,748\,617\,555\,190\,192\,045\,T^{49} + \\
 & \quad 207\,745\,798\,094\,379\,488\,167\,751\,158\,877\,993\,571\,866\,T^{50} - \\
 & \quad 259\,143\,036\,747\,137\,093\,285\,885\,386\,059\,471\,228\,890\,T^{51} + \\
 & \quad 314\,663\,924\,285\,883\,371\,314\,907\,970\,392\,176\,392\,225\,T^{52} - \\
 & \quad 371\,894\,772\,654\,987\,620\,980\,216\,616\,753\,273\,115\,529\,T^{53} +
 \end{aligned}$$

»

427 734 359 759 097 085 053 853 449 580 209 899 315 T⁵⁴ -
 478 588 637 562 574 620 611 136 723 322 577 116 387 T⁵⁵ +
 520 666 601 483 684 890 928 657 528 553 540 406 471 T⁵⁶ -
 550 350 434 078 828 411 199 860 827 794 771 572 429 T⁵⁷ +
 564 596 307 436 346 759 388 723 201 712 038 047 201 T⁵⁸ -
 561 311 322 469 355 376 165 167 102 169 814 629 937 T⁵⁹ +
 539 649 908 594 740 617 615 141 235 433 960 932 974 T⁶⁰ -
 500 180 920 532 088 669 110 059 618 702 117 086 205 T⁶¹ +
 444 893 900 367 003 198 292 403 501 606 159 356 997 T⁶² -
 377 036 735 214 183 343 538 480 076 815 001 055 931 T⁶³ +
 300 802 940 416 512 693 272 596 995 459 940 460 323 T⁶⁴ -
 220 910 152 748 111 847 353 795 479 550 077 303 061 T⁶⁵ +
 142 127 731 574 903 312 146 278 645 593 374 996 475 T⁶⁶ -
 68 817 691 633 539 816 162 349 546 087 100 092 394 T⁶⁷ +
 4 548 642 190 839 017 810 943 214 488 145 709 721 T⁶⁸ +
 48 171 724 844 587 793 774 225 735 898 414 936 163 T⁶⁹ -
 88 020 682 033 142 847 680 864 175 243 517 373 167 T⁷⁰ +
 114 839 126 415 003 811 665 136 702 030 830 369 361 T⁷¹ -
 129 484 052 475 101 577 765 524 322 626 888 261 061 T⁷² +
 133 589 810 658 825 308 640 635 636 994 576 950 661 T⁷³ -
 129 281 444 944 910 416 874 741 581 584 795 044 485 T⁷⁴ +
 118 883 803 919 548 327 518 270 635 929 249 388 073 T⁷⁵ -
 104 663 649 586 771 562 870 757 664 524 595 336 408 T⁷⁶ +
 88 630 798 639 469 792 470 809 150 215 545 565 796 T⁷⁷ -
 72 411 095 942 389 570 291 326 266 753 936 819 957 T⁷⁸ +
 57 191 335 869 719 288 258 812 368 730 018 580 046 T⁷⁹ -
 43 726 144 616 491 019 916 715 188 957 179 825 010 T⁸⁰ +
 32 390 489 687 856 182 452 346 652 704 369 725 968 T⁸¹ -
 23 259 143 906 644 980 947 901 190 868 039 145 011 T⁸² +
 16 195 567 523 201 952 862 212 505 831 699 692 459 T⁸³ -
 10 936 236 605 561 455 643 511 085 024 329 128 701 T⁸⁴ +
 7 161 200 229 624 581 207 002 594 961 418 140 927 T⁸⁵ -
 4 546 453 740 851 806 975 672 939 805 666 910 767 T⁸⁶ +
 2 797 732 217 103 480 699 101 471 140 873 818 713 T⁸⁷ -
 1 668 107 080 371 760 038 928 705 006 978 365 206 T⁸⁸ + 963 227 993 117 488 149 779 064 086 479 816 889
 T⁸⁹ - 538 384 538 692 953 693 548 553 768 197 039 944 T⁹⁰ +
 291 108 716 268 884 488 943 375 243 978 546 588 T⁹¹ - 152 169 934 971 142 439 217 111 032 527 184 807
 T⁹² + 76 841 686 294 921 286 877 410 382 305 875 553 T⁹³ -
 37 455 367 686 376 302 483 140 775 134 141 596 T⁹⁴ + 17 607 833 584 753 809 866 993 089 267 195 660 T⁹⁵ -
 7 975 679 648 984 980 816 169 123 570 478 054 T⁹⁶ + 3 477 465 262 482 453 436 363 451 042 376 763 T⁹⁷ -
 1 457 876 778 515 847 672 271 262 983 639 924 T⁹⁸ + 586 995 936 620 020 363 271 395 909 951 710 T⁹⁹ -
 226 704 293 650 514 311 551 313 410 494 859 T¹⁰⁰ + 83 869 900 028 588 285 462 278 137 584 868 T¹⁰¹ -
 29 678 273 862 306 632 337 012 128 587 148 T¹⁰² + 10 029 280 641 193 727 701 679 935 863 457 T¹⁰³ -
 3 231 129 106 479 071 774 151 973 676 366 T¹⁰⁴ + 990 563 442 718 037 167 782 112 711 189 T¹⁰⁵ -
 288 383 842 669 892 535 165 869 991 388 T¹⁰⁶ + 79 552 658 529 585 978 038 080 737 053 T¹⁰⁷ -
 20 743 101 070 378 443 272 071 754 916 T¹⁰⁸ + 5 098 698 532 107 329 588 362 804 682 T¹⁰⁹ -
 1 177 923 904 252 627 539 258 740 848 T¹¹⁰ + 254 921 181 085 040 399 293 954 626 T¹¹¹ -
 51 488 544 002 382 700 417 662 573 T¹¹² + 9 665 186 209 658 960 091 438 505 T¹¹³ -
 1 678 168 039 306 037 623 148 601 T¹¹⁴ + 268 049 190 944 682 816 294 623 T¹¹⁵ -
 39 138 290 733 728 552 556 828 T¹¹⁶ + 5 185 401 774 321 877 851 616 T¹¹⁷ -
 617 930 527 374 019 489 856 T¹¹⁸ + 65 534 318 803 258 712 480 T¹¹⁹ - 6 105 239 098 703 721 024 T¹²⁰ +

»

$$\frac{491464515937915008 T^{121} - 33460198809091328 T^{122} + 1871419847408384 T^{123} - 82456268912640 T^{124} + 2679881807872 T^{125} - 57024970752 T^{126} + 594837504 T^{127}}{(2 (4608 - 226560 T + 5367456 T^2 - 82195664 T^3 + 919380688 T^4 - 8038473748 T^5 + 57373789206 T^6 - 344516034368 T^7 + 1779504363078 T^8 - 8042174372557 T^9 + 32231562387870 T^{10} - 115815717852178 T^{11} + 376496389523755 T^{12} - 1115760699354364 T^{13} + 3034085808198831 T^{14} - 7613448663622029 T^{15} + 17716466439842235 T^{16} - 38398262636324625 T^{17} + 77817245375284936 T^{18} - 147975161806008018 T^{19} + 264864463654413778 T^{20} - 447537155866622680 T^{21} + 715724452091768365 T^{22} - 1085975248590733307 T^{23} + 1566793410493137029 T^{24} - 2153782249322555994 T^{25} + 2826132464730846217 T^{26} - 354573444875219235 T^{27} + 4259704526510564908 T^{28} - 4906306554934041288 T^{29} + 5423374081718704899 T^{30} - 5757666735070210053 T^{31} + 5873314948586537617 T^{32} - 5757666735070210053 T^{33} + 5423374081718704899 T^{34} - 4906306554934041288 T^{35} + 4259704526510564908 T^{36} - 354573444875219235 T^{37} + 2826132464730846217 T^{38} - 2153782249322555994 T^{39} + 1566793410493137029 T^{40} - 1085975248590733307 T^{41} + 715724452091768365 T^{42} - 447537155866622680 T^{43} + 264864463654413778 T^{44} - 147975161806008018 T^{45} + 77817245375284936 T^{46} - 38398262636324625 T^{47} + 17716466439842235 T^{48} - 7613448663622029 T^{49} + 3034085808198831 T^{50} - 1115760699354364 T^{51} + 376496389523755 T^{52} - 115815717852178 T^{53} + 32231562387870 T^{54} - 8042174372557 T^{55} + 1779504363078 T^{56} - 344516034368 T^{57} + 57373789206 T^{58} - 8038473748 T^{59} + 919380688 T^{60} - 82195664 T^{61} + 5367456 T^{62} - 226560 T^{63} + 4608 T^{64})^2)}}$$

» {47523.2, {202,

$$\left\{ -\frac{1}{T^{62}} (4800 - 308320 T + 9808032 T^2 - 206446584 T^3 + 3240074008 T^4 - 40497584374 T^5 + 420342156836 T^6 - 3729360372285 T^7 + 28886460771468 T^8 - 198493122075857 T^9 + 1225259574313104 T^{10} - 6862621358717871 T^{11} + 35161777425089269 T^{12} - 165919824943691051 T^{13} + 725151525523471344 T^{14} - 294950904603953312 T^{15} + 11211306256912870636 T^{16} - 39967653669292309438 T^{17} + 134053197568094483321 T^{18} - 424205145842882102739 T^{19} + 1269667339152811019616 T^{20} - 3602437237953283642154 T^{21} + 9709162260153481775468 T^{22} - 24903210081100111755078 T^{23} + 60892070619759266748729 T^{24} - 142162508609466554569870 T^{25} + 317370541942009804323618 T^{26} - 678424052396014040801259 T^{27} + 1390425932872917374248443 T^{28} - 2735476394145142161400403 T^{29} + 5171952055961873577218673 T^{30} - 9407733385388457266951989 T^{31} + 16480655049183131814166657 T^{32} - 27832517078630143339405034 T^{33} + 45355511337845824737431258 T^{34} - 71384032621621999512690626 T^{35} + 108603350274522125432833887 T^{36} - 159852220077767515160259085 T^{37} + 227810788203271578088595570 T^{38} - 314587480356289981678538895 T^{39} + 421245626639574905673378673 T^{40} - 547336490029846034651443955 T^{41} + 690523005477615544197880341 T^{42} - 846381427143857246661703154 T^{43} + 1008452514745427709634112880 T^{44} - 1168580428400909213992280313 T^{45} + 1317531316281517546141592855 T^{46} - 1445833434997087861671838638 T^{47} + 1544736819332921675652646352 T^{48} - 1607162329928754027810599785 T^{49} + 1628503554237935640660012461 T^{50} - 1607162329928754027810599785 T^{51} + 1544736819332921675652646352 T^{52} - 1445833434997087861671838638 T^{53} + 1317531316281517546141592855 T^{54} - 1168580428400909213992280313 T^{55} + 1008452514745427709634112880 T^{56} - 846381427143857246661703154 T^{57} + 690523005477615544197880341 T^{58} - 547336490029846034651443955 T^{59} + 421245626639574905673378673 T^{60} - 314587480356289981678538895 T^{61} + 227810788203271578088595570 T^{62} - 159852220077767515160259085 T^{63} + 108603350274522125432833887 T^{64} -$$

$$\begin{aligned}
 & 71\,384\,032\,621\,621\,999\,512\,690\,626\,T^{65} + 45\,355\,511\,337\,845\,824\,737\,431\,258\,T^{66} - \\
 & 27\,832\,517\,078\,630\,143\,339\,405\,034\,T^{67} + 16\,480\,655\,049\,183\,131\,814\,166\,657\,T^{68} - \\
 & 9\,407\,733\,385\,388\,457\,266\,951\,989\,T^{69} + 5\,171\,952\,055\,961\,873\,577\,218\,673\,T^{70} - \\
 & 2\,735\,476\,394\,145\,142\,161\,400\,403\,T^{71} + 1\,390\,425\,932\,872\,917\,374\,248\,443\,T^{72} - \\
 & 678\,424\,052\,396\,014\,040\,801\,259\,T^{73} + 317\,370\,541\,942\,009\,804\,323\,618\,T^{74} - \\
 & 142\,162\,508\,609\,466\,554\,569\,870\,T^{75} + 60\,892\,070\,619\,759\,266\,748\,729\,T^{76} - \\
 & 24\,903\,210\,081\,100\,111\,755\,078\,T^{77} + 9\,709\,162\,260\,153\,481\,775\,468\,T^{78} - 3\,602\,437\,237\,953\,283\,642\,154\,T^{79} + \\
 & 1\,269\,667\,339\,152\,811\,019\,616\,T^{80} - 424\,205\,145\,842\,882\,102\,739\,T^{81} + 134\,053\,197\,568\,094\,483\,321\,T^{82} - \\
 & 39\,967\,653\,669\,292\,309\,438\,T^{83} + 11\,211\,306\,256\,912\,870\,636\,T^{84} - 2\,949\,509\,046\,039\,533\,312\,T^{85} + \\
 & 725\,151\,525\,523\,471\,344\,T^{86} - 165\,919\,824\,943\,691\,051\,T^{87} + 35\,161\,777\,425\,089\,269\,T^{88} - \\
 & 6\,862\,621\,358\,717\,871\,T^{89} + 1\,225\,259\,574\,313\,104\,T^{90} - 198\,493\,122\,075\,857\,T^{91} + \\
 & 28\,886\,460\,771\,468\,T^{92} - 3\,729\,360\,372\,285\,T^{93} + 420\,342\,156\,836\,T^{94} - 40\,497\,584\,374\,T^{95} + \\
 & 3\,240\,074\,008\,T^{96} - 206\,446\,584\,T^{97} + 9\,808\,032\,T^{98} - 308\,320\,T^{99} + 4800\,T^{100} \Big), \\
 & - \left((-1 + T) \left(987\,099\,136 - 124\,379\,138\,048\,T + 7\,798\,546\,122\,496\,T^2 - 324\,576\,957\,954\,304\,T^3 + \right. \right. \\
 & \quad 10\,092\,819\,466\,715\,392\,T^4 - 250\,212\,078\,578\,000\,768\,T^5 + 5\,153\,437\,321\,659\,901\,360\,T^6 - \\
 & \quad 90\,731\,666\,901\,446\,584\,816\,T^7 + 1\,394\,369\,096\,884\,600\,439\,280\,T^8 - 19\,006\,665\,626\,124\,478\,509\,416\,T^9 + \\
 & \quad 232\,721\,325\,714\,933\,548\,898\,953\,T^{10} - 2\,585\,929\,106\,098\,833\,051\,163\,333\,T^{11} + \\
 & \quad 26\,297\,905\,814\,520\,775\,242\,008\,033\,T^{12} - 246\,509\,413\,122\,988\,105\,101\,999\,725\,T^{13} + \\
 & \quad 2\,142\,775\,257\,798\,340\,491\,544\,339\,145\,T^{14} - 17\,362\,282\,496\,846\,522\,459\,440\,283\,017\,T^{15} + \\
 & \quad 131\,729\,690\,298\,890\,186\,676\,193\,687\,686\,T^{16} - 939\,557\,153\,448\,157\,781\,332\,831\,979\,194\,T^{17} + \\
 & \quad 6\,321\,775\,572\,725\,439\,050\,980\,470\,716\,739\,T^{18} - 40\,250\,845\,588\,079\,899\,395\,955\,459\,740\,056\,T^{19} + \\
 & \quad 243\,181\,598\,940\,839\,296\,885\,938\,258\,944\,898\,T^{20} - 1\,397\,599\,767\,245\,485\,336\,675\,035\,767\,211\,411\,T^{21} + \\
 & \quad 7\,657\,765\,640\,390\,344\,990\,439\,804\,130\,027\,443\,T^{22} - 40\,083\,668\,510\,523\,030\,111\,333\,915\,378\,260\,914\,T^{23} + \\
 & \quad 200\,806\,642\,959\,102\,754\,482\,191\,371\,374\,018\,046\,T^{24} - \\
 & \quad 964\,412\,910\,184\,772\,574\,615\,278\,515\,245\,835\,808\,T^{25} + 4\,447\,232\,266\,784\,147\,678\,346\,723\,842\,571\,130\,414 \\
 & \quad T^{26} - 19\,718\,396\,176\,154\,942\,873\,091\,270\,239\,997\,483\,091\,T^{27} + \\
 & \quad 84\,173\,075\,260\,206\,492\,366\,265\,998\,946\,906\,879\,346\,T^{28} - \\
 & \quad 346\,351\,039\,118\,067\,715\,052\,167\,693\,438\,502\,466\,247\,T^{29} + \\
 & \quad 1\,375\,260\,402\,919\,825\,750\,597\,001\,605\,623\,683\,857\,625\,T^{30} - \\
 & \quad 5\,275\,061\,561\,015\,294\,856\,990\,577\,317\,710\,841\,553\,682\,T^{31} + \\
 & \quad 19\,564\,209\,438\,811\,526\,882\,740\,157\,782\,218\,379\,441\,501\,T^{32} - \\
 & \quad 70\,222\,992\,576\,318\,949\,624\,133\,321\,829\,528\,771\,089\,516\,T^{33} + \\
 & \quad 244\,142\,516\,984\,154\,581\,384\,619\,110\,585\,517\,547\,151\,262\,T^{34} - \\
 & \quad 822\,804\,032\,928\,775\,734\,993\,116\,306\,030\,848\,552\,529\,132\,T^{35} + \\
 & \quad 2\,690\,043\,472\,303\,690\,344\,091\,498\,150\,756\,971\,740\,125\,534\,T^{36} - \\
 & \quad 8\,537\,564\,955\,427\,363\,336\,498\,728\,216\,622\,770\,040\,222\,252\,T^{37} + \\
 & \quad 26\,321\,164\,967\,002\,177\,499\,930\,978\,815\,605\,585\,085\,345\,486\,T^{38} - \\
 & \quad 78\,875\,316\,518\,765\,021\,754\,371\,964\,792\,236\,600\,430\,773\,028\,T^{39} + \\
 & \quad 229\,877\,211\,030\,737\,739\,118\,437\,440\,252\,986\,474\,119\,443\,122\,T^{40} - \\
 & \quad 651\,943\,350\,828\,790\,658\,065\,704\,655\,079\,645\,898\,818\,625\,414\,T^{41} + \\
 & \quad 1\,800\,158\,597\,480\,666\,746\,436\,409\,430\,864\,479\,646\,507\,847\,235\,T^{42} - \\
 & \quad 4\,841\,889\,637\,440\,309\,873\,517\,125\,762\,285\,143\,727\,603\,405\,376\,T^{43} + \\
 & \quad 12\,691\,930\,474\,675\,474\,013\,390\,055\,251\,839\,167\,437\,517\,496\,277\,T^{44} - \\
 & \quad 32\,437\,293\,022\,586\,172\,636\,232\,325\,374\,594\,813\,595\,856\,494\,846\,T^{45} + \\
 & \quad 80\,863\,347\,090\,650\,042\,434\,996\,417\,496\,581\,613\,710\,914\,697\,203\,T^{46} - \\
 & \quad 196\,709\,937\,676\,505\,270\,088\,886\,112\,814\,117\,526\,196\,753\,422\,743\,T^{47} + \\
 & \quad 467\,129\,613\,694\,294\,203\,617\,697\,137\,119\,263\,137\,530\,462\,477\,742\,T^{48} - \\
 & \quad 1\,083\,293\,820\,256\,849\,989\,118\,768\,039\,289\,300\,245\,423\,140\,346\,802\,T^{49} + \\
 & \quad 2\,454\,182\,123\,424\,701\,438\,050\,835\,920\,683\,340\,522\,427\,183\,170\,020\,T^{50} - \\
 & \quad 5\,433\,327\,302\,576\,867\,194\,986\,872\,705\,163\,986\,230\,005\,563\,749\,009\,T^{51} +
 \end{aligned}$$

11 758 819 828 778 507 154 116 542 672 453 251 244 187 668 337 675 T⁵² -
 24 884 804 935 728 874 665 033 426 151 844 219 023 552 375 908 252 T⁵³ +
 51 511 605 254 833 799 439 417 008 528 690 375 063 800 671 496 038 T⁵⁴ -
 104 327 313 132 641 424 050 697 174 242 401 021 031 615 236 744 976 T⁵⁵ +
 206 789 759 448 816 890 332 971 193 763 435 170 328 008 813 465 925 T⁵⁶ -
 401 243 865 059 427 019 776 751 272 119 484 240 100 458 886 320 995 T⁵⁷ +
 762 326 242 477 791 319 768 261 992 601 637 942 863 705 046 614 304 T⁵⁸ -
 1 418 487 733 172 648 020 680 417 455 187 083 651 684 615 144 830 503 T⁵⁹ +
 2 585 569 053 690 001 638 155 352 281 022 952 621 627 227 117 716 895 T⁶⁰ -
 4 617 644 579 864 512 570 701 770 101 773 184 161 046 460 978 122 180 T⁶¹ +
 8 081 665 630 085 471 653 088 653 927 224 191 337 355 649 323 004 703 T⁶² -
 13 863 520 950 635 119 415 181 896 543 955 289 732 219 890 385 335 840 T⁶³ +
 23 313 559 078 092 624 211 890 151 915 995 446 062 701 226 861 828 572 T⁶⁴ -
 38 438 774 139 302 814 176 663 660 628 547 122 805 805 708 057 582 414 T⁶⁵ +
 62 145 968 043 472 649 703 628 882 340 344 804 744 351 081 418 530 406 T⁶⁶ -
 98 534 400 245 575 362 067 349 193 418 447 091 776 921 090 249 269 001 T⁶⁷ +
 153 226 908 006 894 300 820 851 840 729 717 984 404 413 016 732 217 502 T⁶⁸ -
 233 714 696 222 997 090 137 957 997 351 009 384 232 596 311 621 179 544 T⁶⁹ +
 349 673 015 071 829 248 473 661 920 406 052 250 094 651 069 118 155 367 T⁷⁰ -
 513 183 753 576 802 654 378 760 326 864 098 686 326 599 704 532 686 023 T⁷¹ +
 738 778 805 466 783 888 642 912 730 220 597 974 478 020 057 612 342 368 T⁷² -
 1 043 198 562 619 327 376 194 104 244 304 945 337 199 362 672 739 123 621 T⁷³ +
 1 444 748 081 034 523 328 621 298 266 384 436 145 260 349 471 731 742 722 T⁷⁴ -
 1 962 135 329 157 390 708 998 706 793 377 647 568 734 675 314 646 129 361 T⁷⁵ +
 2 612 697 600 110 213 550 698 206 765 115 412 081 339 672 914 974 856 273 T⁷⁶ -
 3 409 968 707 174 929 985 015 538 443 968 787 546 843 729 546 253 577 798 T⁷⁷ +
 4 360 613 468 354 192 993 318 927 857 858 124 896 772 385 065 667 382 650 T⁷⁸ -
 5 460 855 577 227 263 424 995 605 535 558 339 581 605 037 108 922 139 151 T⁷⁹ +
 6 692 643 229 235 292 907 420 058 466 140 270 878 022 547 826 969 630 695 T⁸⁰ -
 8 019 920 856 693 127 127 638 569 878 007 034 236 635 420 669 794 554 277 T⁸¹ +
 9 385 486 602 181 526 686 799 349 767 337 886 346 204 690 885 023 609 172 T⁸² -
 10 708 991 637 314 478 275 004 878 294 351 873 396 534 045 028 518 845 377 T⁸³ +
 11 886 656 421 522 793 463 325 133 987 039 810 480 856 252 958 230 990 109 T⁸⁴ -
 12 793 221 271 544 870 445 095 555 217 162 219 606 697 287 431 114 672 505 T⁸⁵ +
 13 286 502 887 998 012 392 698 257 695 979 033 990 365 659 933 804 826 868 T⁸⁶ -
 13 214 695 425 642 258 746 787 850 407 988 157 318 495 714 120 442 807 100 T⁸⁷ +
 12 426 249 556 467 427 521 997 019 873 525 516 916 063 206 786 080 700 570 T⁸⁸ -
 10 781 816 028 891 983 390 721 792 673 767 792 126 152 645 089 909 405 034 T⁸⁹ +
 8 167 394 423 883 992 112 400 553 325 884 201 159 902 106 064 003 053 596 T⁹⁰ -
 4 507 533 666 577 488 585 267 776 405 494 093 413 869 855 847 408 886 740 T⁹¹ -
 222 760 913 263 417 681 349 211 091 346 652 936 515 676 253 684 299 602 T⁹² +
 5 988 806 173 084 509 338 399 006 973 538 418 676 318 989 799 881 872 818 T⁹³ -
 12 690 973 956 230 022 407 685 088 311 855 101 946 730 816 832 161 899 928 T⁹⁴ +
 20 164 349 293 645 914 128 960 007 367 012 126 491 943 089 162 161 457 721 T⁹⁵ -
 28 183 836 821 886 591 433 727 153 547 852 203 814 272 941 212 201 829 677 T⁹⁶ +
 36 474 686 034 889 082 431 212 777 202 567 629 137 612 863 385 943 066 185 T⁹⁷ -
 44 727 816 162 884 429 760 815 931 511 895 308 758 520 751 163 197 314 753 T⁹⁸ +
 52 618 770 012 386 393 019 119 280 152 928 155 778 564 370 571 743 447 429 T⁹⁹ -
 59 828 687 470 167 614 568 541 545 544 625 577 056 806 411 082 801 237 077 T¹⁰⁰ +
 66 065 424 920 349 432 904 894 385 003 628 559 933 640 529 105 123 432 433 T¹⁰¹ -
 71 082 894 988 379 578 696 004 477 671 115 045 583 161 623 342 460 086 483 T¹⁰² +

74 696 871 099 031 193 900 219 423 541 848 234 564 011 012 904 967 593 851 T¹⁰³ -
 76 795 871 886 024 592 388 899 614 148 206 618 657 459 403 070 449 874 459 T¹⁰⁴ +
 77 346 262 734 015 496 551 430 635 960 905 543 587 878 531 599 944 101 860 T¹⁰⁵ -
 76 391 317 208 349 427 365 589 411 917 390 456 593 856 370 584 978 961 250 T¹⁰⁶ +
 74 044 592 282 932 756 282 073 228 295 689 091 949 468 891 881 662 623 910 T¹⁰⁷ -
 70 478 513 094 555 760 031 390 433 476 987 466 788 741 266 559 757 686 432 T¹⁰⁸ +
 65 909 473 632 280 914 427 690 338 938 667 407 112 188 776 278 062 570 676 T¹⁰⁹ -
 60 580 998 760 008 417 765 186 840 700 611 892 899 451 633 773 075 766 784 T¹¹⁰ +
 54 746 565 202 471 287 082 273 033 630 472 760 130 523 592 604 394 198 512 T¹¹¹ -
 48 653 555 063 599 683 179 514 089 541 490 025 477 379 460 662 323 438 570 T¹¹² +
 42 529 547 284 909 828 294 095 478 880 983 054 558 994 989 675 194 646 026 T¹¹³ -
 36 571 787 439 196 652 778 237 270 350 279 406 868 993 163 906 155 924 193 T¹¹⁴ +
 30 940 268 505 961 919 950 452 550 566 984 922 213 339 425 306 767 979 193 T¹¹⁵ -
 25 754 457 526 145 059 971 616 229 000 668 772 111 767 149 743 142 877 145 T¹¹⁶ +
 21 093 359 640 481 200 005 919 585 658 261 046 900 035 670 230 537 283 664 T¹¹⁷ -
 16 998 353 116 276 124 434 265 605 947 759 738 547 843 717 393 857 213 801 T¹¹⁸ +
 13 478 072 254 786 022 710 400 394 561 619 489 899 120 716 594 351 756 563 T¹¹⁹ -
 10 514 560 130 785 992 627 591 816 163 128 643 722 897 979 181 398 951 971 T¹²⁰ +
 8 069 947 871 552 250 765 362 724 920 352 470 487 226 243 551 678 888 146 T¹²¹ -
 6 093 020 735 434 785 966 276 467 856 765 714 532 779 434 975 202 071 376 T¹²² +
 4 525 178 284 285 087 444 262 624 302 437 358 095 553 701 798 181 170 519 T¹²³ -
 3 305 460 931 798 525 795 844 932 861 527 788 607 898 998 970 602 223 927 T¹²⁴ +
 2 374 475 763 090 535 515 630 122 775 082 340 837 741 296 454 285 544 540 T¹²⁵ -
 1 677 193 889 907 119 924 064 255 337 925 307 574 116 671 673 860 417 291 T¹²⁶ +
 1 164 699 325 912 713 549 031 318 948 162 599 036 761 482 241 943 565 854 T¹²⁷ -
 795 041 368 114 039 337 882 587 522 462 564 063 176 366 433 974 786 991 T¹²⁸ +
 533 380 027 681 216 177 257 895 821 793 697 677 823 727 014 095 865 679 T¹²⁹ -
 351 622 277 893 806 979 884 527 286 645 656 223 970 907 724 475 205 810 T¹³⁰ +
 227 733 058 738 503 032 254 026 261 161 266 825 633 018 513 491 244 432 T¹³¹ -
 144 877 004 659 004 877 536 647 785 562 909 719 136 869 315 799 493 065 T¹³² +
 90 512 066 593 690 014 156 110 555 975 991 263 583 690 050 532 266 342 T¹³³ -
 55 520 528 175 177 652 367 543 684 072 370 297 725 818 162 475 455 562 T¹³⁴ +
 33 430 572 559 537 476 689 513 295 864 132 627 205 615 368 752 606 112 T¹³⁵ -
 19 754 992 074 670 864 150 337 258 736 050 428 104 410 613 159 130 848 T¹³⁶ +
 11 453 788 107 077 521 992 590 861 787 190 109 370 552 956 788 702 763 T¹³⁷ -
 6 514 091 113 959 471 110 593 487 537 834 552 799 977 288 846 489 676 T¹³⁸ +
 3 633 128 889 585 185 271 434 629 755 644 237 957 358 489 306 589 079 T¹³⁹ -
 1 986 628 510 370 580 744 612 785 160 938 069 507 547 353 218 657 403 T¹⁴⁰ +
 1 064 742 600 075 629 995 985 139 005 588 446 085 939 923 232 431 796 T¹⁴¹ -
 559 170 792 190 972 236 024 128 963 882 567 895 958 611 294 120 411 T¹⁴² +
 287 668 568 798 304 104 497 913 217 546 907 998 206 468 738 387 761 T¹⁴³ -
 144 930 879 755 625 968 215 065 757 978 982 345 781 783 363 326 862 T¹⁴⁴ +
 71 485 612 314 609 216 492 822 291 138 330 626 346 892 605 195 244 T¹⁴⁵ -
 34 508 818 603 490 084 881 830 320 444 807 936 956 753 393 913 380 T¹⁴⁶ +
 16 298 795 758 921 999 579 497 410 570 766 212 199 796 621 360 003 T¹⁴⁷ -
 7 529 230 668 780 096 196 510 202 499 368 022 104 466 475 867 841 T¹⁴⁸ +
 3 400 683 298 452 482 879 073 106 434 234 972 887 239 040 258 944 T¹⁴⁹ -
 1 501 232 500 589 812 177 851 961 305 103 461 634 054 954 111 134 T¹⁵⁰ +
 647 494 496 356 607 130 082 742 429 845 223 629 390 788 943 610 T¹⁵¹ -
 272 750 041 612 759 308 793 434 610 228 285 582 474 464 250 133 T¹⁵² +
 112 166 230 052 700 982 936 673 005 801 347 330 624 300 276 973 T¹⁵³ -

$$\begin{aligned}
 & 45\ 014\ 154\ 500\ 323\ 548\ 776\ 841\ 595\ 628\ 762\ 225\ 388\ 388\ 582\ 146\ T^{154} + \\
 & 17\ 621\ 364\ 509\ 969\ 712\ 160\ 030\ 634\ 510\ 288\ 585\ 465\ 706\ 148\ 661\ T^{155} - \\
 & 6\ 725\ 728\ 178\ 646\ 870\ 761\ 893\ 705\ 606\ 924\ 573\ 397\ 869\ 465\ 638\ T^{156} + \\
 & 2\ 501\ 760\ 605\ 927\ 669\ 468\ 250\ 883\ 548\ 091\ 956\ 306\ 717\ 112\ 121\ T^{157} - \\
 & 906\ 456\ 395\ 920\ 315\ 065\ 964\ 066\ 144\ 572\ 352\ 692\ 015\ 662\ 142\ T^{158} + \\
 & 319\ 757\ 579\ 828\ 441\ 073\ 590\ 854\ 436\ 613\ 365\ 345\ 993\ 748\ 658\ T^{159} - \\
 & 109\ 757\ 618\ 722\ 472\ 023\ 082\ 790\ 876\ 863\ 168\ 251\ 395\ 152\ 392\ T^{160} + \\
 & 36\ 639\ 005\ 893\ 229\ 486\ 192\ 490\ 783\ 731\ 851\ 212\ 753\ 541\ 818\ T^{161} - \\
 & 11\ 887\ 491\ 704\ 451\ 921\ 274\ 845\ 074\ 584\ 273\ 930\ 301\ 086\ 950\ T^{162} + \\
 & 3\ 746\ 300\ 162\ 324\ 069\ 281\ 343\ 269\ 767\ 638\ 827\ 006\ 605\ 904\ T^{163} - \\
 & 1\ 146\ 023\ 569\ 314\ 117\ 207\ 137\ 838\ 572\ 127\ 018\ 193\ 230\ 118\ T^{164} + \\
 & 340\ 062\ 774\ 895\ 916\ 277\ 424\ 693\ 120\ 851\ 329\ 943\ 284\ 788\ T^{165} - \\
 & 97\ 808\ 495\ 210\ 864\ 797\ 674\ 958\ 210\ 072\ 279\ 094\ 904\ 150\ T^{166} + \\
 & 27\ 246\ 012\ 146\ 704\ 872\ 330\ 194\ 049\ 104\ 844\ 674\ 397\ 707\ T^{167} - \\
 & 7\ 344\ 675\ 664\ 292\ 370\ 021\ 911\ 435\ 407\ 512\ 453\ 357\ 966\ T^{168} + \\
 & 1\ 914\ 234\ 456\ 321\ 132\ 511\ 935\ 180\ 065\ 129\ 172\ 542\ 717\ T^{169} - \\
 & 481\ 894\ 973\ 661\ 473\ 811\ 499\ 225\ 274\ 424\ 793\ 586\ 931\ T^{170} + \\
 & 117\ 056\ 544\ 252\ 694\ 089\ 459\ 920\ 486\ 282\ 409\ 118\ 558\ T^{171} - \\
 & 27\ 405\ 779\ 544\ 368\ 786\ 071\ 516\ 758\ 972\ 335\ 693\ 645\ T^{172} + \\
 & 6\ 176\ 902\ 534\ 744\ 792\ 472\ 221\ 696\ 207\ 836\ 338\ 900\ T^{173} - \\
 & 1\ 338\ 497\ 835\ 031\ 886\ 569\ 768\ 313\ 007\ 194\ 721\ 628\ T^{174} + \\
 & 278\ 465\ 284\ 668\ 764\ 669\ 325\ 690\ 809\ 634\ 297\ 518\ T^{175} - 55\ 534\ 745\ 493\ 645\ 998\ 745\ 723\ 557\ 438\ 444\ 710 \\
 & \quad T^{176} + 10\ 599\ 155\ 562\ 857\ 066\ 274\ 948\ 635\ 162\ 699\ 495\ T^{177} - \\
 & 1\ 932\ 382\ 137\ 045\ 462\ 443\ 996\ 676\ 466\ 931\ 333\ T^{178} + 335\ 855\ 649\ 658\ 299\ 054\ 354\ 994\ 089\ 870\ 164\ T^{179} - \\
 & 55\ 524\ 042\ 514\ 471\ 397\ 353\ 319\ 173\ 682\ 642\ T^{180} + 8\ 709\ 699\ 705\ 240\ 762\ 603\ 156\ 340\ 718\ 741\ T^{181} - \\
 & 1\ 292\ 768\ 329\ 392\ 160\ 818\ 818\ 614\ 004\ 612\ T^{182} + 181\ 005\ 260\ 499\ 681\ 637\ 355\ 252\ 698\ 384\ T^{183} - \\
 & 23\ 823\ 308\ 173\ 801\ 591\ 476\ 066\ 865\ 465\ T^{184} + 2\ 935\ 878\ 686\ 172\ 126\ 247\ 605\ 080\ 053\ T^{185} - \\
 & 337\ 240\ 899\ 232\ 109\ 473\ 309\ 085\ 507\ T^{186} + 35\ 921\ 323\ 165\ 780\ 741\ 356\ 147\ 399\ T^{187} - \\
 & 3\ 526\ 559\ 175\ 823\ 790\ 962\ 692\ 403\ T^{188} + 316\ 849\ 121\ 091\ 410\ 995\ 714\ 591\ T^{189} - \\
 & 25\ 833\ 387\ 148\ 435\ 632\ 983\ 800\ T^{190} + 1\ 891\ 856\ 210\ 054\ 199\ 852\ 176\ T^{191} - 122\ 879\ 144\ 603\ 897\ 926\ 928 \\
 & \quad T^{192} + 6\ 966\ 213\ 823\ 199\ 880\ 656\ T^{193} - 337\ 564\ 967\ 346\ 814\ 848\ T^{194} + 13\ 588\ 652\ 416\ 314\ 112\ T^{195} - \\
 & 436\ 071\ 838\ 784\ 256\ T^{196} + 10\ 454\ 126\ 850\ 304\ T^{197} - 166\ 344\ 189\ 952\ T^{198} + 1\ 316\ 900\ 864\ T^{199}) / \\
 & (2 (4800 - 308\ 320\ T + 9\ 808\ 032\ T^2 - 206\ 446\ 584\ T^3 + 3\ 240\ 074\ 008\ T^4 - 40\ 497\ 584\ 374\ T^5 + \\
 & \quad 420\ 342\ 156\ 836\ T^6 - 3\ 729\ 360\ 372\ 285\ T^7 + 28\ 886\ 460\ 771\ 468\ T^8 - 198\ 493\ 122\ 075\ 857\ T^9 + \\
 & \quad 1\ 225\ 259\ 574\ 313\ 104\ T^{10} - 6\ 862\ 621\ 358\ 717\ 871\ T^{11} + 35\ 161\ 777\ 425\ 089\ 269\ T^{12} - \\
 & \quad 165\ 919\ 824\ 943\ 691\ 051\ T^{13} + 725\ 151\ 525\ 523\ 471\ 344\ T^{14} - 2\ 949\ 509\ 046\ 039\ 533\ 312\ T^{15} + \\
 & \quad 11\ 211\ 306\ 256\ 912\ 870\ 636\ T^{16} - 39\ 967\ 653\ 669\ 292\ 309\ 438\ T^{17} + 134\ 053\ 197\ 568\ 094\ 483\ 321\ T^{18} - \\
 & \quad 424\ 205\ 145\ 842\ 882\ 102\ 739\ T^{19} + 1\ 269\ 667\ 339\ 152\ 811\ 019\ 616\ T^{20} - 3\ 602\ 437\ 237\ 953\ 283\ 642\ 154 \\
 & \quad T^{21} + 9\ 709\ 162\ 260\ 153\ 481\ 775\ 468\ T^{22} - 24\ 903\ 210\ 081\ 100\ 111\ 755\ 078\ T^{23} + \\
 & \quad 60\ 892\ 070\ 619\ 759\ 266\ 748\ 729\ T^{24} - 142\ 162\ 508\ 609\ 466\ 554\ 569\ 870\ T^{25} + \\
 & \quad 317\ 370\ 541\ 942\ 009\ 804\ 323\ 618\ T^{26} - 678\ 424\ 052\ 396\ 014\ 040\ 801\ 259\ T^{27} + \\
 & \quad 1\ 390\ 425\ 932\ 872\ 917\ 374\ 248\ 443\ T^{28} - 2\ 735\ 476\ 394\ 145\ 142\ 161\ 400\ 403\ T^{29} + \\
 & \quad 5\ 171\ 952\ 055\ 961\ 873\ 577\ 218\ 673\ T^{30} - 9\ 407\ 733\ 385\ 388\ 457\ 266\ 951\ 989\ T^{31} + \\
 & \quad 16\ 480\ 655\ 049\ 183\ 131\ 814\ 166\ 657\ T^{32} - 27\ 832\ 517\ 078\ 630\ 143\ 339\ 405\ 034\ T^{33} + \\
 & \quad 45\ 355\ 511\ 337\ 845\ 824\ 737\ 431\ 258\ T^{34} - 71\ 384\ 032\ 621\ 621\ 999\ 512\ 690\ 626\ T^{35} + \\
 & \quad 108\ 603\ 350\ 274\ 522\ 125\ 432\ 833\ 887\ T^{36} - 159\ 852\ 220\ 077\ 767\ 515\ 160\ 259\ 085\ T^{37} + \\
 & \quad 227\ 810\ 788\ 203\ 271\ 578\ 088\ 595\ 570\ T^{38} - 314\ 587\ 480\ 356\ 289\ 981\ 678\ 538\ 895\ T^{39} + \\
 & \quad 421\ 245\ 626\ 639\ 574\ 905\ 673\ 378\ 673\ T^{40} - 547\ 336\ 490\ 029\ 846\ 034\ 651\ 443\ 955\ T^{41} + \\
 & \quad 690\ 523\ 005\ 477\ 615\ 544\ 197\ 880\ 341\ T^{42} - 846\ 381\ 427\ 143\ 857\ 246\ 661\ 703\ 154\ T^{43} + \\
 & \quad 1\ 008\ 452\ 514\ 745\ 427\ 709\ 634\ 112\ 880\ T^{44} - 1\ 168\ 580\ 428\ 400\ 909\ 213\ 992\ 280\ 313\ T^{45} +
 \end{aligned}$$

$$\begin{aligned}
 & 1\ 317\ 531\ 316\ 281\ 517\ 546\ 141\ 592\ 855\ T^{46} - 1\ 445\ 833\ 434\ 997\ 087\ 861\ 671\ 838\ 638\ T^{47} + \\
 & 1\ 544\ 736\ 819\ 332\ 921\ 675\ 652\ 646\ 352\ T^{48} - 1\ 607\ 162\ 329\ 928\ 754\ 027\ 810\ 599\ 785\ T^{49} + \\
 & 1\ 628\ 503\ 554\ 237\ 935\ 640\ 660\ 012\ 461\ T^{50} - 1\ 607\ 162\ 329\ 928\ 754\ 027\ 810\ 599\ 785\ T^{51} + \\
 & 1\ 544\ 736\ 819\ 332\ 921\ 675\ 652\ 646\ 352\ T^{52} - 1\ 445\ 833\ 434\ 997\ 087\ 861\ 671\ 838\ 638\ T^{53} + \\
 & 1\ 317\ 531\ 316\ 281\ 517\ 546\ 141\ 592\ 855\ T^{54} - 1\ 168\ 580\ 428\ 400\ 909\ 213\ 992\ 280\ 313\ T^{55} + \\
 & 1\ 008\ 452\ 514\ 745\ 427\ 709\ 634\ 112\ 880\ T^{56} - 846\ 381\ 427\ 143\ 857\ 246\ 661\ 703\ 154\ T^{57} + \\
 & 690\ 523\ 005\ 477\ 615\ 544\ 197\ 880\ 341\ T^{58} - 547\ 336\ 490\ 029\ 846\ 034\ 651\ 443\ 955\ T^{59} + \\
 & 421\ 245\ 626\ 639\ 574\ 905\ 673\ 378\ 673\ T^{60} - 314\ 587\ 480\ 356\ 289\ 981\ 678\ 538\ 895\ T^{61} + \\
 & 227\ 810\ 788\ 203\ 271\ 578\ 088\ 595\ 570\ T^{62} - 159\ 852\ 220\ 077\ 767\ 515\ 160\ 259\ 085\ T^{63} + \\
 & 108\ 603\ 350\ 274\ 522\ 125\ 432\ 833\ 887\ T^{64} - 71\ 384\ 032\ 621\ 621\ 999\ 512\ 690\ 626\ T^{65} + \\
 & 45\ 355\ 511\ 337\ 845\ 824\ 737\ 431\ 258\ T^{66} - 27\ 832\ 517\ 078\ 630\ 143\ 339\ 405\ 034\ T^{67} + \\
 & 16\ 480\ 655\ 049\ 183\ 131\ 814\ 166\ 657\ T^{68} - 9\ 407\ 733\ 385\ 388\ 457\ 266\ 951\ 989\ T^{69} + \\
 & 5\ 171\ 952\ 055\ 961\ 873\ 577\ 218\ 673\ T^{70} - 2\ 735\ 476\ 394\ 145\ 142\ 161\ 400\ 403\ T^{71} + \\
 & 1\ 390\ 425\ 932\ 872\ 917\ 374\ 248\ 443\ T^{72} - 678\ 424\ 052\ 396\ 014\ 040\ 801\ 259\ T^{73} + \\
 & 317\ 370\ 541\ 942\ 009\ 804\ 323\ 618\ T^{74} - 142\ 162\ 508\ 609\ 466\ 554\ 569\ 870\ T^{75} + \\
 & 60\ 892\ 070\ 619\ 759\ 266\ 748\ 729\ T^{76} - 24\ 903\ 210\ 081\ 100\ 111\ 755\ 078\ T^{77} + \\
 & 9\ 709\ 162\ 260\ 153\ 481\ 775\ 468\ T^{78} - 3\ 602\ 437\ 237\ 953\ 283\ 642\ 154\ T^{79} + \\
 & 1\ 269\ 667\ 339\ 152\ 811\ 019\ 616\ T^{80} - 424\ 205\ 145\ 842\ 882\ 102\ 739\ T^{81} + 134\ 053\ 197\ 568\ 094\ 483\ 321\ T^{82} - \\
 & 39\ 967\ 653\ 669\ 292\ 309\ 438\ T^{83} + 11\ 211\ 306\ 256\ 912\ 870\ 636\ T^{84} - 2\ 949\ 509\ 046\ 039\ 533\ 312\ T^{85} + \\
 & 725\ 151\ 525\ 523\ 471\ 344\ T^{86} - 165\ 919\ 824\ 943\ 691\ 051\ T^{87} + 35\ 161\ 777\ 425\ 089\ 269\ T^{88} - \\
 & 6\ 862\ 621\ 358\ 717\ 871\ T^{89} + 1\ 225\ 259\ 574\ 313\ 104\ T^{90} - 198\ 493\ 122\ 075\ 857\ T^{91} + \\
 & 28\ 886\ 460\ 771\ 468\ T^{92} - 3\ 729\ 360\ 372\ 285\ T^{93} + 420\ 342\ 156\ 836\ T^{94} - 40\ 497\ 584\ 374\ T^{95} + \\
 & 3\ 240\ 074\ 008\ T^{96} - 206\ 446\ 584\ T^{97} + 9\ 808\ 032\ T^{98} - 308\ 320\ T^{99} + 4800\ T^{100}
 \end{aligned}$$

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Out[]= \$Aborted