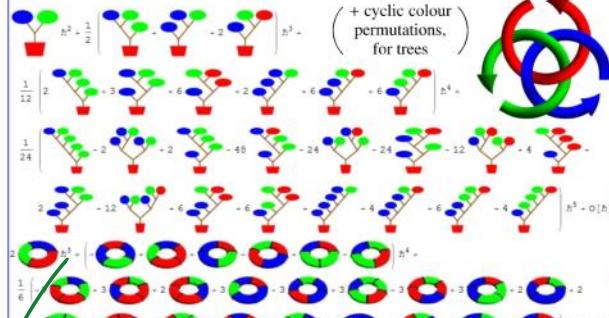


Dror Bar-Natan: Talks: Qinhuangdao-1507:
 $\omega\beta:=\text{http://www.math.toronto.edu/~drorbn/Talks/Qinhuangdao-1507/}$

Theorem 2 [BND]. $\exists!$ a homomorphic expansion, aka a homomorphic universal finite type invariant Z^w of pure w-tangles. $z^w := \log Z^w$ takes values in $FL(S)^S \times CW(S)$.

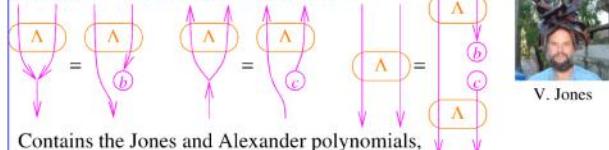
z is computable. z of the Borromean tangle, to degree 5 [BN]:



(I have a fancy free Lie calculated) Nice, but too hard!

Proposition [BN]. Modulo all relations that universally hold for the 2D non-Abelian Lie algebra and after some changes-of-variable, z^w reduces to z_0 .

Back to v – the 2D “Jones Quotient”.



Contains the Jones and Alexander polynomials, still too hard!

The OneCo Quotient.

$= 0$, only one co-bracket is allowed.
 Everything should work, and everything is being worked!

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Let's talk about China, America, Taiwan, economy, ecology, religion, democracy, censorship, and all else.

Polynomial Time Knot Polynomials, B

Definition. (Compare [BNS, BN]) A **The Abstract Context** meta-monoid is a functor M : (finite sets, injections) \rightarrow (sets) (think “ $M(S)$ is quantum G^S ”, for G a group) along with natural operations $*: M(S_1) \times M(S_2) \rightarrow M(S_1 \sqcup S_2)$ whenever $S_1 \cap S_2 = \emptyset$ and $m_c^{ab}: M(S \sqcup \{a, b\}) \rightarrow M(S \sqcup \{c\})$ whenever $a \neq b \notin S$ and $c \notin S$, such that

$$\text{meta-associativity: } m_a^{ab} // m_a^{ac} = m_b^{bc} // m_a^{ab}$$

$$\text{meta-locality: } m_c^{ab} // m_f^{de} = m_f^{de} // m_c^{ab}$$

and, with $\epsilon_b = M(S \hookrightarrow S \sqcup \{b\})$,

$$\text{meta-unit: } \epsilon_b // m_a^{ab} = \text{Id} = \epsilon_b // m_a^{ba}.$$

Claim. Pure virtual tangles $P\Gamma$ form a meta-monoid.

Theorem. $S \mapsto \Gamma_0(S)$ is a meta-monoid and $z_0: P\Gamma \rightarrow \Gamma_0$ is a morphism of meta-monoids.

Strong Conviction. There exists an extension of Γ_0 to a bigger meta-monoid $\Gamma_{01}(S) = \Gamma_0(S) \times \Gamma_1(S)$, along with an extension of z_0 to $z_{01}: P\Gamma \rightarrow \Gamma_{01}$, with (more or less)

$$\Gamma_1(S) =$$

Furthermore, upon reducing to a single variable everything is polynomial size and polynomial time.

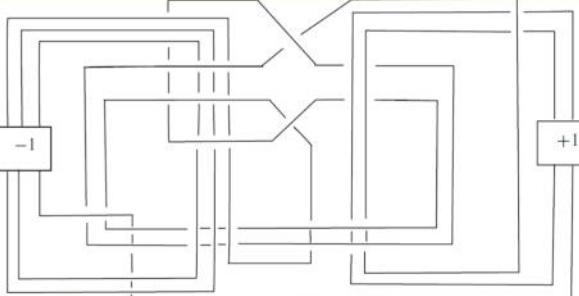
Furthermore, Γ_{01} is given using a “meta-2-cocycle over Γ_0 ”: In addition to $m_c^{ab} \rightarrow m_{0c}^{ab}$, there are R_S -linear $m_{1c}^{ab}: \Gamma_1(S \sqcup \{a, b\}) \rightarrow \Gamma_1(S \sqcup \{c\})$ a meta-right-action $\alpha^{ab}: \Gamma_1(S) \times \Gamma_0(S) \rightarrow \Gamma_1(S)$ R_S -linear in the first variable, and an order 1 differential operator (over R_S) $\rho_c^{ab}: \Gamma_0(S \sqcup \{a, b\}) \rightarrow \Gamma_1(S \sqcup \{c\})$ such that

$$(\zeta_0, \zeta_1) // m_c^{ab} = (\zeta_0 // m_{0c}^{ab}, (\zeta_1, \zeta_0) // \alpha^{ab} // m_{1c}^{ab} + \zeta_0 // \rho_c^{ab})$$

What's missing: Some commutation relations and exponentiated commutation relations, a lot of detail-sensitive work.

A Lit about ribbon knots

1. def.
2. ribbon = slice
3. Fox-Milnor Thm.



[GST]: a slice knot that might not be ribbon (48 crossings).



“God created the knots, all else in topology is the work of mortals.”

Leopold Kronecker (modified)



www.katlas.org The Knot Atlas

✓: $\Gamma_1(S) < V_S^{\otimes 3} \oplus V_S^{\otimes 4}$

$V_S = \langle S \rangle$