

Pensieve header: Testing the expansion extension property for the 3-strand braid group.

```
SetDirectory["C:\\drorbn\\AcademicPensieve\\2015-02"];
<< ..Projects/WKO4/FreeLie.m

FreeLie` implements / extends
{*, +, **, $SeriesShowDegree, <>, , , ad, Ad, adSeries, AllCyclicWords, AllLyndonWords,
AllWords, Arbitrator, ASeries, AW, b, BCH, BooleanSequence, BracketForm, BS, CC, Crop,
CW, CWS, CWSeries, D, Deg, DegreeScale, DerivationSeries, div, DK, DKS, EulerE, Exp,
Inverse, j, J, JA, LieDerivation, LieMorphism, LieSeries, LS, LW, LyndonFactorization,
Morphism, New, RandomCWSeries, Randomizer, RandomLieSeries, RC, SeriesSolve,
Support, t, tb, TopBracketForm, tr, UndeterminedCoefficients, , , , , , }.

n = 3;
Clear[s, cs];
Do[
  Do[cs[i][k, j] = 0, {j, 1, n-1}, {k, j+1, n}];
  cs[i][i+1, i] = 1/2;
  s[i] = DKS[n, cs[i]],
  {i, 1, n-1}
]
s[2]
DKS[ $\frac{\overline{t_{23}}}{2}$ ,  $\overline{t_{13}t_{23}}$  cs[2][3, 1, 2],
 $\overline{t_{13}\overline{t_{13}t_{23}}}$  cs[2][3, 1, 1, 2] +  $\overline{\overline{t_{13}t_{23}}t_{23}}$  cs[2][3, 1, 2, 2], ...]
```



```
SeriesSolve[{s[1], s[2]},
  s[1]**(s[2] //  $\sigma[2, 1, 3]$ )**(s[1] //  $\sigma[2, 3, 1]$ ) =
  s[2]**(s[1] //  $\sigma[1, 3, 2]$ )**(s[2] //  $\sigma[3, 1, 2]$ )
]

{s[1], s[2]}

Arbitrator called on {cs[1][3, 1, 2]}...
Arbitrator called on {cs[1][3, 1, 1, 2], cs[1][3, 1, 2, 2], cs[2][3, 1, 2, 2]}...
{DKS[ $\frac{\overline{t_{12}}}{2}$ , 0, 0, ...], DKS[ $\frac{\overline{t_{23}}}{2}$ ,  $\frac{1}{12}\overline{t_{13}t_{23}}$ , 0, ...]}
```

**First** /@ {}  
{}

**s[1]@{6}**

Arbitrator called on

{cs[1][3, 1, 1, 1, 2], cs[1][3, 1, 1, 2, 2], cs[1][3, 1, 2, 2, 2], cs[2][3, 1, 1, 1, 2]}...

Arbitrator called on {cs[1][3, 1, 1, 1, 2], cs[1][3, 1, 1, 1, 2],  
cs[1][3, 1, 1, 2, 1, 2], cs[1][3, 1, 1, 2, 2, 2], cs[1][3, 1, 2, 1, 2, 2],  
cs[1][3, 1, 2, 2, 2, 2], cs[2][3, 1, 1, 1, 2, 2], cs[2][3, 1, 1, 2, 1, 2]}...

No solutions!

\$Aborted