

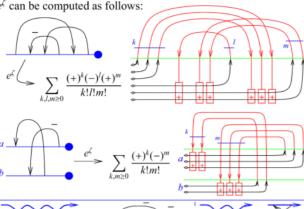


Dror Bar-Natan: Academic Pensieve: http://drorbn.net/AcademicPens

A Partial Reduction of BF Theory to Combinatorics,

combinatorics is obvious...

Theorem 1 (with Cattaneo (credit, no blame)). In the ribbon case, e can be computed as follows:



Theorem 2. Using Gauss diagrams to represent knots and Tcomponent pure tangles, the above formulas define an invariant (the "true" triple linkin $CW(FL(T)) \to CW(T)$, "cyclic words in T"

 Agrees with BN-Dancso [BND] and with [BN2].
In-practice computable! • Vanishes on braids. • Extends to w. • Contains Gnots. In 3D, a generic immersion of S^1 is an Alexander. • The "missing factor" in Levine's factorization [Le] embedding, a knot. In 4D, a generic immersion (the rest of [Le] also fits, hence contains the MVA). • Related to of a surface has finitely-many double points (a extends Farber's [Fa]? • Should be summed and categorified.

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[BND] D. Bar-Natan and Z. Dancso, Finite Type Invariants of W-From Alexander to Kashiwara and Vergne, Knotted Objects: http://www.math.toronto.edu/~drorbn/papers/WKO/.

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[Dal E. Dalvit http://science.unitn.it/~dalvit/.

[CR] A. S. Cattaneo and C. A. Rossi, Wilson Surfaces and Higher Dimensional Knot Invariants, Commun. in Math. Phys. 256-3 (2005) 513-537, arXiv:math-ph/0210037.

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Continuing Joost Slingerland.

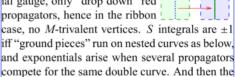






Sketch of Proof. In 4D ax-

ial gauge, only "drop down" red propagators, hence in the ribbon

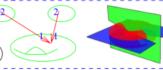




Musings

Chern-Simons. When the domain of BF is restricted to ribbon knots, and the target of CS is restricted to trees and wheels, they agree. Why?

Is this all? What about the ∨-invariant? ing number)

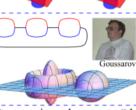


gnot?). Perhaps we should be studying these?

Finite type. What are finite-type would be "chord diagrams"?



There's an alternative definition of finite type in 3D, due obvious parallel in 4D involves "bubble wraps". Is it any good?



Shielded tangles. In 3D, one can't zoom in and compute "the [CKS] J. S. Carter, S. Kamada, and M. Saito, Diagrammatic Computations for Chern-Simons invariant of a tangle". Yet there are well-defined Quandles and Cocycle Knot Invariants, Contemp. Math. 318 (2003) 51-74. invariants of "shielded tangles", and rules for their compositions.







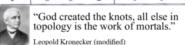


Will the relationship with the Kashiwara-Vergne problem [BND] necessarily arise here?

type invariants of plane curves, in the style of Arnold's J^+ , J^- , and St [Ar], a bit better?



	$a(\frac{1}{K})$	a(≍ ()	$a(\bowtie)$	∞	\circ	0	(III)	(eee)
St	1	0	0	0	0	1	2	3	
J^+	0	2	0	0	0	-2	-4	-6	
J-	0	0	-2	-1	0	-3	-6	-9	
Mary 04000								Yu.	JANK SI







virtual 2- Knots? Group only?