\[ g \bar{h} = w(g, h) \bar{g} \bar{h} \] “twisted group algebras”

Added March 24:

To thus twist a semi-direct product, it should be enough to twist the inverse map.