

Pensieve header: J(BCH).

```
SetDirectory["C:\\drorbn\\AcademicPensieve\\2012-09"];
```

```
<< FreeLie.m
```

```
{u = LW["u"], v = LW["v"]}
```

```
{⟨u⟩, ⟨v⟩}
```

```
bch = BCH[u, v]
```

```
LS[⟨u⟩ + ⟨v⟩,  $\frac{\langle uv \rangle}{2}$ ,  $\frac{\langle uuv \rangle}{12} + \frac{\langle uvv \rangle}{12}$ ]
```

```
J[u, bch][{8}]
```

```
CWS[CW[u], 0, 0, 0, 0, 0, 0, 0, 0]
```

**J[v, bch] [{8}]**

$$\begin{aligned}
 & \text{CWS} \left[ \text{CW}[v], \text{CW}[uv], \frac{\text{CW}[uuv]}{2} - \frac{\text{CW}[uvv]}{2}, \frac{\text{CW}[uuuv]}{6} + \frac{7 \text{CW}[uuvv]}{4} - \frac{5 \text{CW}[uvuv]}{2} + \frac{\text{CW}[uvvv]}{6}, \right. \\
 & \frac{\text{CW}[uuuuu]}{24} + \frac{11 \text{CW}[uuuuuv]}{12} - \frac{3 \text{CW}[uuuuuv]}{2} - \frac{11 \text{CW}[uuuvvv]}{12} + \frac{3 \text{CW}[uvuvvv]}{2} - \frac{\text{CW}[uvvvvv]}{24}, \\
 & \frac{\text{CW}[uuuuuu]}{120} + \frac{31 \text{CW}[uuuuuv]}{48} - \frac{11 \text{CW}[uuuuuv]}{6} + \frac{109 \text{CW}[uuuvvv]}{36} + \\
 & \frac{7 \text{CW}[uuvuu]}{8} - \frac{23 \text{CW}[uuvuv]}{4} - \frac{23 \text{CW}[uuvvu]}{4} + \frac{31 \text{CW}[uuvvv]}{48} + \\
 & \frac{28 \text{CW}[uvuvuv]}{3} - \frac{11 \text{CW}[uvuvvv]}{6} + \frac{7 \text{CW}[uvvuv]}{8} + \frac{\text{CW}[uvvvvv]}{120}, \\
 & \frac{\text{CW}[uuuuuuu]}{720} + \frac{59 \text{CW}[uuuuuuv]}{240} - \frac{5 \text{CW}[uuuuuvu]}{8} + \frac{205 \text{CW}[uuuuvvv]}{144} + \frac{\text{CW}[uuuvuuu]}{4} - \\
 & \frac{5 \text{CW}[uuuvuuu]}{4} - \frac{9 \text{CW}[uuuvuvu]}{4} - \frac{205 \text{CW}[uuuvvvv]}{144} - \frac{25 \text{CW}[uuvuuuv]}{8} + \\
 & 6 \text{CW}[uuvuvuv] + \frac{9 \text{CW}[uuvuvvv]}{4} + \frac{25 \text{CW}[uuvvuuv]}{8} + \frac{5 \text{CW}[uuvvvuv]}{4} - \\
 & \frac{59 \text{CW}[uuvvvvv]}{240} - 6 \text{CW}[uvuvuvu] + \frac{5 \text{CW}[uvuvvvv]}{8} - \frac{\text{CW}[uvvuvvv]}{4} - \frac{\text{CW}[uvvvvvv]}{720}, \\
 & \frac{\text{CW}[uuuuuuuu]}{5040} + \frac{127 \text{CW}[uuuuuuuv]}{1440} - \frac{7 \text{CW}[uuuuuuvu]}{24} + \frac{1261 \text{CW}[uuuuuvvv]}{720} + \\
 & \frac{19 \text{CW}[uuuuuuu]}{48} - \frac{203 \text{CW}[uuuuuvuv]}{48} - \frac{179 \text{CW}[uuuuuvvu]}{48} + \\
 & \frac{3079 \text{CW}[uuuuvvvv]}{576} - \frac{17 \text{CW}[uuuvuuu]}{72} + \frac{43 \text{CW}[uuuvuuuv]}{24} + \\
 & \frac{41 \text{CW}[uuuvuuu]}{3} - \frac{377 \text{CW}[uuuvuvuv]}{36} - \frac{17 \text{CW}[uuuvvuuv]}{24} - \frac{107 \text{CW}[uuuvvvuv]}{24} - \\
 & \frac{377 \text{CW}[uuuvvvuv]}{36} + \frac{1261 \text{CW}[uuuvvvvv]}{720} - 8 \text{CW}[uuvuuuv] - \frac{107 \text{CW}[uuvuuuv]}{24} + \\
 & 26 \text{CW}[uuvuvuv] + 20 \text{CW}[uuvuvuv] - \frac{179 \text{CW}[uuvuvvvv]}{48} - \frac{237 \text{CW}[uuvvuuv]}{32} + \\
 & 26 \text{CW}[uuvvuuv] - \frac{17 \text{CW}[uuvvvvvv]}{24} + \frac{43 \text{CW}[uuvvvuvv]}{24} - \frac{203 \text{CW}[uuvvvvu]}{48} + \\
 & \frac{127 \text{CW}[uuvvvvvv]}{1440} - \frac{165 \text{CW}[uvuvuvuv]}{4} + \frac{41 \text{CW}[uvuvuvvv]}{3} - 8 \text{CW}[uvuvuvuv] - \\
 & \left. \frac{7 \text{CW}[uvuvvvvv]}{24} + \frac{19 \text{CW}[uvvuvvvv]}{48} - \frac{17 \text{CW}[uvvvuvvv]}{72} + \frac{\text{CW}[uvvvvvvv]}{5040} \right]
 \end{aligned}$$