

Pensieve header: A  $\mu$ -calculus demo for my Hamburg talk.

```
SetDirectory["/drorbn/AcademicPensieve/2012-08"];
<< muCalculus.m

Format[CW[w_], StandardForm] := "[" <> w <> "]";
```

ExampleZeta

```
T0 = Rm[3, a] Rp[b, 2] Rp[1, 4];
\xi = T0 // dm[2, 1, 1] // dm[4, b, b] // dm[1, a, a] // dm[3, a, a];
\xi[{5}] /. {w_LW \rightarrow (Deg[w] + 1) ! w, w_CW \rightarrow Deg[w] ! w}
```

ExampleZeta

```
\mu[CWS[-[a], -2[ab], -3[aab] - 3[abb], -4[aaab] + 42[aabb] - 60[abab] - 4[abbb],
-5[aaaab] + 110[aaabb] - 180[aabab] + 110[aabbb] - 180[ababb] - 5[abbbb]],
h[b] LS[2⟨a⟩, 0, -24⟨aab⟩, -60⟨aaab⟩ + 60⟨aabb⟩,
-120⟨aaaab⟩ + 900⟨aaabb⟩ + 360⟨aabab⟩ - 120⟨aabbb⟩] +
h[a] LS[-2⟨a⟩ + 2⟨b⟩, 9⟨ab⟩, 26⟨aab⟩ - 26⟨abb⟩, 60⟨aaab⟩ - 255⟨aabb⟩ + 60⟨abbb⟩,
119⟨aaaab⟩ - 1504⟨aaabb⟩ + 118⟨aabab⟩ + 1504⟨aabbb⟩ + 1386⟨ababb⟩ - 119⟨abbbb⟩]]
```

```
\xi[{10}] /. {w_LW \rightarrow (Deg[w] + 1) ! * w, w_CW \rightarrow Deg[w] ! * w}
```

$$\begin{aligned} & \mu \left[ CWS[-[a], -2[ab], -3[aab] - 3[abb], -4[aaab] + 42[aabb] - 60[abab] - 4[abbb], \right. \\ & \quad \left. -5[aaaab] + 110[aaabb] - 180[aabab] + 110[aabbb] - 180[ababb] - 5[abbbb], \right. \\ & \quad \left. -6[aaaaab] + 465[aaaabb] - 1320[aaabab] - 2180[aaabbb] + 630[aabaab] + 4140[aababb] + \right. \\ & \quad \left. 4140[aabbab] + 465[aabbbb] - 6720[ababab] - 1320[ababbb] + 630[ababb] - 6[abbbb], \right. \\ & \quad \left. -7[aaaaaaab] + 1239[aaaaabb] - 3150[aaaabab] - 7175[aaaabbb] + 1260[aaabaab] + \right. \\ & \quad \left. 6300[aaababb] + 11340[aaabbab] - 7175[aaabbbb] + 15750[aabaabb] - \right. \\ & \quad \left. 30240[aababab] + 11340[aababbb] + 15750[aabbabb] + 6300[aabbbab] + \right. \\ & \quad \left. 1239[aabbbbb] - 30240[abababb] - 3150[ababbbb] + 1260[abbabbb] - 7[abbbbb], \right. \\ & \quad \left. -8[aaaaaaaaab] + 3556[aaaaaab] - 11760[aaaaabab] - 70616[aaaaabbb] + 15960[aaaabaab] + \right. \\ & \quad \left. 170520[aaaababb] + 150360[aaaabbab] + 215530[aaaabbbb] - 9520[aaabaaab] - \right. \\ & \quad \left. 72240[aaabaabb] - 551040[aaababab] - 422240[aaababbb] + 28560[aaabbaab] - \right. \\ & \quad \left. 179760[aaabbabb] - 422240[aaabbbab] - 70616[aaabbbb] + 322560[aabaabab] - \right. \\ & \quad \left. 179760[aabaabbb] + 1048320[aabababb] + 806400[aababab] + 150360[aababbbb] - \right. \\ & \quad \left. 298620[aabbaabb] + 1048320[aabbabab] + 28560[aabbabbb] - 72240[aabbabbb] + \right. \\ & \quad \left. 170520[aabbabbab] + 3556[aabbabbb] - 1663200[abababab] - 551040[abababbb] + \right. \\ & \quad \left. 322560[ababbabb] - 11760[ababbbb] + 15960[ababbbb] - 9520[abbbabbb] - 8[abbbbbb], \right. \\ & \quad \left. -9[aaaaaaaaab] + 9036[aaaaaaab] - 31752[aaaaaabab] - 271236[aaaaaabbb] + \right. \\ & \quad \left. 40824[aaaaabaab] + 494424[aaaaababb] + 585144[aaaaabab] + 778554[aaaaabbbb] - \right. \\ & \quad \left. 22680[aaaabaaab] + 139860[aaaabaabb] - 1451520[aaaababab] - 687960[aaaababbb] + \right. \\ & \quad \left. 49140[aaaabbaab] - 223020[aaaabbabb] - 1443960[aaaabbbab] + 778554[aaaabbbb] - \right. \\ & \quad \left. 136080[aaabaabb] - 544320[aaabaabab] - 982800[aaabaabbb] + 544320[aaababaab] + \right. \\ & \quad \left. 181440[aaabababb] + 1270080[aaababbb] - 1443960[aaabbbb] - 2033640[aaabbaabb] + \right. \\ & \quad \left. 3447360[aaabbabab] - 1648080[aaabbabbb] - 1648080[aaabbbbab] - \right. \\ & \quad \left. 982800[aaabbbabb] - 687960[aaabbbbab] - 271236[aaabbbbbb] + 483840[aabaabaab] + \right. \\ & \quad \left. 4354560[aabaababb] + 2540160[aabaabbab] - 223020[aabaabbb] + 3991680[aababaabb] - \right. \\ & \quad \left. 9979200[aabababab] + 3447360[aabababbb] + 2540160[aababbabb] + \right. \\ & \quad \left. 1270080[aababbab] + 585144[aababbbb] - 2033640[aabbaabbb] + 3991680[aabbababb] + \right. \\ & \quad \left. 4354560[aabbabbab] + 49140[aabbabbb] + 181440[aabbabab] - 136080[aabbabbb] + \right. \\ & \quad \left. 139860[aabbabbab] + 494424[aabbabbb] + 9036[aabbabbbb] - 9979200[abababbb] - \right. \\ & \quad \left. 1451520[abababbb] + 544320[abababbb] - 544320[ababbbab] - 31752[ababbbb] + \right. \\ & \quad \left. 483840[abbababb] + 40824[abbabbbb] - 22680[abbbabbb] - 9[abbbbbb], \right. \\ & \quad \left. -10[aaaaaaaaab] + 22995[aaaaaaaabb] - 94320[aaaaaaabab] - 1481880[aaaaaaabbb] + \right. \\ & \quad \left. 168840[aaaaaabaab] + 4140360[aaaaaababb] + 3837960[aaaaaabab] + \right. \\ & \quad \left. 15000510[aaaaaabbb] - 206640[aaaaabaaab] - 4135320[aaaaabaabb] - \right. \\ & \quad \left. 12640320[aaaaababab] - 34680240[aaaaababbb] - 1867320[aaaaabbaab] - \right. \end{aligned}$$

```

22 400 280 [aaaaabbabb] - 31 051 440 [aaaaabbbab] - 35 154 252 [aaaaabbbbb] +
97 650 [aaaabaaaab] + 4 296 600 [aaaabaaaabb] + 10 584 000 [aaaabaabab] +
9 689 400 [aaaabaabbb] + 12 398 400 [aaaababaab] + 88 603 200 [aaaabababb] +
70 459 200 [aaaababbab] + 69 394 500 [aaaabbbbb] - 390 600 [aaaabbaaab] -
21 942 900 [aaaabbaabb] + 79 531 200 [aaaabbabab] + 31 210 200 [aaaabbabbb] -
4 825 800 [aaaabbbaab] + 30 756 600 [aaaabbbabb] + 69 394 500 [aaaabbbbabb] +
15 000 510 [aaaabbbbbbb] - 17 337 600 [aaabaaabab] - 12 482 400 [aaabaaabbb] +
2 116 800 [aaabaabaab] - 14 212 800 [aaabaababb] + 2 116 800 [aaabaabbab] +
30 756 600 [aaabaabbbb] - 12 398 400 [aaababaabb] - 339 292 800 [aaabababab] -
184 262 400 [aabababbb] + 29 332 800 [aaababbaab] - 55 944 000 [aaababbabb] -
140 716 800 [aababbbab] - 31 051 440 [aaabbbbbbb] + 8 101 800 [aaabbaaabbb] +
23 889 600 [aaabbaabab] + 58 640 400 [aaabbaabbb] + 7 560 000 [aaabbabaab] -
45 057 600 [aaabbababb] - 46 872 000 [aaabbabbab] - 4 825 800 [aaabbabbbb] +
58 640 400 [aaabbbbaabb] - 184 262 400 [aaabbbbabab] - 12 482 400 [aaabbbbabbb] +
31 210 200 [aaabbbbaab] + 9 689 400 [aaabbbabb] - 34 680 240 [aaabbbbab] -
1 481 880 [aaabbbbbbb] - 58 968 000 [aababaabb] + 133 358 400 [aabababab] -
46 872 000 [aabababb] - 98 884 800 [aabababb] - 55 944 000 [aababbbab] -
22 400 280 [aababbb] + 81 194 400 [aababaabab] - 45 057 600 [aababaabbb] +
481 723 200 [aababababb] + 336 571 200 [aabababbab] + 79 531 200 [aabababbbb] -
178 718 400 [aababbaabb] + 336 571 200 [aababbabab] + 7 560 000 [aababbabbb] +
2 116 800 [aababbbabb] + 70 459 200 [aababbbab] + 3 837 960 [aababbbbbb] -
178 718 400 [aabbaabbab] - 21 942 900 [aabbaabbbb] + 481 723 200 [aabbababab] +
23 889 600 [aabbababbb] - 58 968 000 [aabbababb] + 29 332 800 [aabbabbbab] -
1 867 320 [aabbabbb] + 8 101 800 [aabbaabbb] - 12 398 400 [aabbbababb] -
14 212 800 [aabbbabbab] - 390 600 [aabbbabbb] + 88 603 200 [aabbbbabab] +
4 296 600 [aabbbbabbb] - 4 135 320 [aabbbbabbb] + 4 140 360 [aabbbbabbab] +
22 995 [aabbbbbb] - 726 485 760 [abababab] - 339 292 800 [ababababb] +
133 358 400 [abababbabb] - 12 640 320 [abababbbb] + 81 194 400 [ababbababb] +
12 398 400 [ababbbbbb] - 17 337 600 [ababbbbab] + 10 584 000 [ababbbabb] -
94 320 [ababbbbbb] + 2 116 800 [ababbbab] + 168 840 [ababbbbbb] -
206 640 [abbbabbb] + 97 650 [abbbabbbb] - 10 [abbbbbb] ] ,
h[b] LS[2 <a>, 0, -24 <aab>, -60 <aaab> + 60 <aabb>,
-120 <aaab> + 900 <aaabb> + 360 <aabab> - 120 <aabbb>, -210 <aaaaab> + 5460 <aaaabb> +
840 <aaabab> - 5460 <aaabbb> - 6300 <aababb> - 2520 <aabbab> + 210 <aabbbb>,
-336 <aaaaaab> + 24 360 <aaaaabb> - 5040 <aaaabab> - 81 760 <aaabbb> - 1680 <aaabaab> -
104 160 <aaababb> - 6720 <aaabbab> + 24 360 <aaabbb> - 40 320 <aabaabb> -
6720 <aababab> + 43 680 <aababbb> + 5040 <aabbabb> + 6720 <aabbabab> - 336 <aabbbbbb>,
-504 <aaaaaaab> + 92 232 <aaaaaabbb> - 57 456 <aaaaabab> - 758 520 <aaaaabbb> -
6048 <aaaabaab> - 884 520 <aaaababb> + 529 200 <aaaabbab> + 758 520 <aaaabbbb> -
143 640 <aaabaabb> - 75 600 <aaababab> + 1 643 040 <aaababbb> + 196 560 <aaabbaab> +
196 560 <aaabbabb> - 342 720 <aaabbbab> - 92 232 <aaabbbbbb> + 30 240 <aabaabab> +
362 880 <aabaabbb> + 937 440 <aabababb> + 453 600 <aabababab> - 219 240 <aababbbab> +
90 720 <aabbabab> - 136 080 <aabbabbb> - 30 240 <aabbabbb> - 15 120 <aabbbabab> +
504 <aabbbbbb>, -720 <aaaaaaaaab> + 315 000 <aaaaaaaaabb> - 337 680 <aaaaaabab> -
5 448 240 <aaaaaaabbb> + 15 120 <aaaaabaab> - 5 307 120 <aaaaababb> +
9 041 760 <aaaaabbbab> + 13 034 700 <aaaaabbbb> + 5040 <aaaabaaab> +
1 995 840 <aaaabaabb> - 1 542 240 <aaaababab> + 28 954 800 <aaaababbb> +
1 572 480 <aaaabbaab> - 1 020 600 <aaaabbabb> - 19 504 800 <aaaabbbab> -
5 448 240 <aaaabbbbbb> + 907 200 <aaabaaabb> + 181 440 <aaabaabab> - 327 600 <aaabaabbb> -
453 600 <aaababaab> + 23 360 400 <aaabababb> + 1 134 000 <aaababbab> -
16 203 600 <aaababbb> + 869 400 <aaabbaabb> + 5 670 000 <aaabbabab> +
12 146 400 <aaabbabb> - 5 493 600 <aaabbbab> - 1 915 200 <aaabbabbb> +
5 392 800 <aaabbbbab> + 315 000 <aaabbbbbb> + 7 106 400 <aabaababb> -
302 400 <aabaabbab> - 2 116 800 <aabaabbbb> + 1 965 600 <aababaabb> +

```

151 200 ⟨aabababab⟩ - 16 430 400 ⟨aabababbb⟩ + 756 000 ⟨aababbabb⟩ -  
 3 931 200 ⟨aababbbab⟩ + 922 320 ⟨aababbbb⟩ - 1 209 600 ⟨aabbaabbb⟩ -  
 2 268 000 ⟨aabbabbb⟩ - 453 600 ⟨aabbabbbab⟩ + 945 000 ⟨aabbabbbb⟩ - 302 400 ⟨aabbababab⟩ +  
 50 400 ⟨aabbbabbb⟩ + 75 600 ⟨aabbbbabb⟩ + 30 240 ⟨aabbbbabb⟩ - 720 ⟨aabbbbbb⟩ ,  
 - 990 ⟨aaaaaaaab⟩ + 1 001 880 ⟨aaaaaaaabb⟩ - 1 544 400 ⟨aaaaaaabab⟩ -  
 33 384 120 ⟨aaaaaaabbb⟩ + 300 960 ⟨aaaaaabaab⟩ - 24 643 080 ⟨aaaaaabbabb⟩ +  
 91 087 920 ⟨aaaaaababab⟩ + 160 512 660 ⟨aaaaaabbbb⟩ + 23 760 ⟨aaaaabaaab⟩ +  
 33 347 160 ⟨aaaaabaabb⟩ - 24 670 800 ⟨aaaaababab⟩ + 346 555 440 ⟨aaaaababbb⟩ -  
 2 494 800 ⟨aaaaabbaab⟩ - 99 708 840 ⟨aaaaabbabb⟩ - 437 865 120 ⟨aaaaabbbab⟩ -  
 160 512 660 ⟨aaaaabbbb⟩ + 6 514 200 ⟨aaaabaaabb⟩ - 6 930 000 ⟨aaaabaabab⟩ -  
 144 809 280 ⟨aaaabaabbb⟩ - 4 934 160 ⟨aaaababaab⟩ + 339 459 120 ⟨aaaabababb⟩ -  
 104 282 640 ⟨aaaababbab⟩ - 507 068 100 ⟨aaaabbbb⟩ - 3 381 840 ⟨aaaabbaaab⟩ +  
 6 486 480 ⟨aaaabbaabb⟩ + 246 652 560 ⟨aaaabbabab⟩ - 369 923 400 ⟨aaaabbabb⟩ -  
 66 749 760 ⟨aaaabbbab⟩ + 82 882 800 ⟨aaaabbbabb⟩ + 390 713 400 ⟨aaaabbbbab⟩ +  
 33 384 120 ⟨aaaabbbb⟩ - 3 548 160 ⟨aaabaaabab⟩ - 49 896 000 ⟨aaabaaabbb⟩ +  
 166 320 ⟨aaabaabaab⟩ + 30 602 880 ⟨aaabaabbb⟩ + 62 868 960 ⟨aaabaabbab⟩ +  
 60 221 700 ⟨aaabaabbbb⟩ + 41 746 320 ⟨aaababaabb⟩ - 9 646 560 ⟨aaabababab⟩ -  
 733 194 000 ⟨aaababbb⟩ - 54 054 000 ⟨aaababbaab⟩ + 140 956 200 ⟨aaababbabb⟩ +  
 135 550 800 ⟨aaababbbab⟩ + 124 795 440 ⟨aaababbbb⟩ - 10 810 800 ⟨aaabbaabab⟩ -  
 51 975 000 ⟨aaabbaabbb⟩ + 58 212 000 ⟨aaabbabaab⟩ - 111 018 600 ⟨aaabbababb⟩ -  
 59 459 400 ⟨aaabbabbab⟩ + 156 479 400 ⟨aaabbabbbb⟩ - 6 375 600 ⟨aaabbbaabb⟩ -  
 153 846 000 ⟨aaabbbabab⟩ + 13 490 400 ⟨aaabbabbbb⟩ + 71 656 200 ⟨aaabbbaaab⟩ -  
 6 375 600 ⟨aaabbabbab⟩ - 49 785 120 ⟨aaabbabbab⟩ - 1 001 880 ⟨aaabbbbbbb⟩ -  
 3 326 400 ⟨aabaabaabb⟩ + 4 989 600 ⟨aabaababab⟩ - 159 112 800 ⟨aabaababb⟩ -  
 19 126 800 ⟨aabaabbabb⟩ + 41 025 600 ⟨aabaabbbab⟩ + 9 979 200 ⟨aabaabbbbbb⟩ -  
 20 512 800 ⟨aababaabbb⟩ - 253 638 000 ⟨aababababb⟩ - 103 118 400 ⟨aabababbab⟩ +  
 178 239 600 ⟨aabababbb⟩ - 10 810 800 ⟨aababbaabb⟩ - 24 948 000 ⟨aababbabab⟩ +  
 123 631 200 ⟨aababbbab⟩ - 38 808 000 ⟨aababbbabb⟩ + 24 116 400 ⟨aababbbbab⟩ -  
 3 465 000 ⟨aababbbbbb⟩ + 21 621 600 ⟨aabbaabbab⟩ + 9 979 200 ⟨aabbaabbbb⟩ -  
 3 326 400 ⟨aabbababab⟩ + 21 621 600 ⟨aabbababb⟩ + 831 600 ⟨aababbabb⟩ +  
 14 968 800 ⟨aabbabbbab⟩ - 4 740 120 ⟨aabbabbbbb⟩ + 8 316 000 ⟨aabbbababb⟩ +  
 3 326 400 ⟨aabbbabbbab⟩ - 2 356 200 ⟨aabbbabbb⟩ + 831 600 ⟨aabbbbabab⟩ -  
 277 200 ⟨aabbbbabbb⟩ - 166 320 ⟨aabbbbabbb⟩ - 55 440 ⟨aabbbbbbab⟩ + 990 ⟨aabbbbbb⟩ ] +  
 h[a] LS[ -2 ⟨a⟩ + 2 ⟨b⟩ , 9 ⟨ab⟩ , 26 ⟨aab⟩ - 26 ⟨abb⟩ , 60 ⟨aaab⟩ - 255 ⟨aabb⟩ + 60 ⟨abbb⟩ ,  
 119 ⟨aaaab⟩ - 1504 ⟨aaabb⟩ + 118 ⟨aabab⟩ + 1504 ⟨aabb⟩ + 1386 ⟨ababb⟩ - 119 ⟨abbb⟩ ,  
 210 ⟨aaaaab⟩ -  $\frac{13839 \langle aaaabb \rangle}{2}$  + 1659 ⟨aaabab⟩ + 18 522 ⟨aaabbb⟩ + 21 063 ⟨aababb⟩ -  
 6720 ⟨aabbab⟩ -  $\frac{13839 \langle aabbbb \rangle}{2}$  - 12 180 ⟨ababbb⟩ + 210 ⟨abbb⟩ ,  
 $\frac{1012 \langle aaaaaab \rangle}{3}$  - 27 376 ⟨aaaaabb⟩ + 13 212 ⟨aaaabab⟩ +  $\frac{484 376 \langle aaaabbb \rangle}{3}$  -  
 340 ⟨aaabaab⟩ + 181 408 ⟨aaababb⟩ - 148 816 ⟨aaabbab⟩ -  $\frac{484 376 \langle aaabbb \rangle}{3}$  -  
 26 916 ⟨aabaabb⟩ + 12 872 ⟨aababab⟩ -  $\frac{1 028 600 \langle aababbb \rangle}{3}$  - 340 ⟨aabbabb⟩ +  
 $\frac{402 608 \langle aabbbab \rangle}{3}$  + 27 376 ⟨aabbbbb⟩ - 167 024 ⟨abababb⟩ + 68 916 ⟨ababbb⟩ +  
 41 880 ⟨ababbb⟩ -  $\frac{1012 \langle abbbbbb \rangle}{3}$  , 504 ⟨aaaaaaab⟩ - 97 794 ⟨aaaaaaabb⟩ +  
 78 192 ⟨aaaaaabab⟩ + 1 143 972 ⟨aaaaabbb⟩ - 6102 ⟨aaaabaab⟩ + 1 149 570 ⟨aaababb⟩ -  
 1 860 336 ⟨aaababbab⟩ - 2 427 975 ⟨aaabbbab⟩ - 557 154 ⟨aaabaabb⟩ + 326 484 ⟨aaababab⟩ -

$$\begin{aligned}
& 5 \ 320 \ 692 \langle aaababbb \rangle + 96 \ 768 \langle aaabbaab \rangle + 579 \ 042 \langle aaabbabb \rangle + 4 \ 391 \ 208 \langle aaabbbab \rangle + \\
& 1 \ 143 \ 972 \langle aaabbbbb \rangle + 71 \ 568 \langle aabaabab \rangle + 1 \ 043 \ 784 \langle aabaabbb \rangle - 4 \ 026 \ 888 \langle aabababb \rangle + \\
& 954 \ 072 \langle aababbab \rangle + 3 \ 437 \ 514 \langle aababbbb \rangle - 1 \ 227 \ 744 \langle aabbabab \rangle + 2 \ 463 \ 948 \langle aabbabb \rangle - \\
& 172 \ 368 \langle aabbbabb \rangle - 1 \ 560 \ 384 \langle aabbbbab \rangle - 97 \ 794 \langle aabbbb \rangle + 3 \ 458 \ 448 \langle abababbb \rangle - \\
& 603 \ 288 \langle ababbabb \rangle - 312 \ 984 \langle ababbbb \rangle - 338 \ 688 \langle abbabbbb \rangle + 504 \langle abbbbbb \rangle, \\
& 717 \langle aaaaaaaab \rangle - 324 \ 384 \langle aaaaaaab \rangle + 382 \ 116 \langle aaaaaabab \rangle + 7 \ 058 \ 696 \langle aaaaaabbb \rangle - \\
& 60 \ 120 \langle aaaaabaab \rangle + 5 \ 841 \ 996 \langle aaaaababb \rangle - 17 \ 291 \ 472 \langle aaaaabbab \rangle - \\
& 28 \ 052 \ 508 \langle aaaaabbbb \rangle + 708 \langle aaaaabaab \rangle - 6 \ 466 \ 266 \langle aaaaabaabb \rangle + \\
& 4 \ 676 \ 484 \langle aaaababab \rangle - 60 \ 359 \ 292 \langle aaaababbb \rangle + 2 \ 485 \ 224 \langle aaaabbaab \rangle + \\
& 18 \ 300 \ 042 \langle aaaabbabb \rangle + 80 \ 577 \ 576 \langle aaaabbbab \rangle + 28 \ 052 \ 508 \langle aaaabbb \rangle + \\
& 322 \ 524 \langle aaabaaabb \rangle + 1 \ 777 \ 536 \langle aaabaabab \rangle + 31 \ 408 \ 644 \langle aaabaabb \rangle - \\
& 500 \ 760 \langle aaababaab \rangle - 57 \ 463 \ 236 \langle aaabababb \rangle + 24 \ 087 \ 852 \langle aaababbab \rangle + \\
& 88 \ 411 \ 800 \langle aaababbbb \rangle + 3186 \langle aaabbaabb \rangle - 48 \ 619 \ 548 \langle aaabbabab \rangle + \\
& 61 \ 931 \ 760 \langle aaabbabb \rangle - 6 \ 713 \ 832 \langle aaabbbaab \rangle - 26 \ 692 \ 800 \langle aaabbabb \rangle - \\
& 79 \ 228 \ 920 \langle aaabbabb \rangle - 7 \ 058 \ 696 \langle aaabbbbbb \rangle + 5 \ 905 \ 656 \langle aabaababb \rangle - \\
& 18 \ 975 \ 528 \langle aabaabbab \rangle - 21 \ 879 \ 990 \langle aabaabbbb \rangle - 5 \ 251 \ 896 \langle aababaabb \rangle + \\
& 2 \ 484 \ 648 \langle aabababab \rangle + 127 \ 246 \ 440 \langle aabababbb \rangle - 35 \ 206 \ 380 \langle aabababb \rangle - \\
& 47 \ 469 \ 240 \langle aababbbab \rangle - 27 \ 018 \ 084 \langle aababbb \rangle - 544 \ 500 \langle aabbaabbb \rangle + \\
& 8 \ 532 \ 180 \langle aabbababb \rangle + 14 \ 016 \ 060 \langle aabbabbab \rangle - 34 \ 193 \ 190 \langle aabbabbb \rangle + \\
& 36 \ 240 \ 840 \langle aabbbbab \rangle - 1 \ 244 \ 200 \langle aabbbabbb \rangle + 5 \ 396 \ 340 \langle aabbbabb \rangle + \\
& 13 \ 376 \ 712 \langle aabbbbbb \rangle + 324 \ 384 \langle aabbbbbb \rangle + 41 \ 505 \ 480 \langle ababababb \rangle - \\
& 41 \ 156 \ 520 \langle abababbb \rangle - 27 \ 341 \ 760 \langle abababbb \rangle + 17 \ 321 \ 520 \langle abababbb \rangle + \\
& 1 \ 239 \ 804 \langle ababbbbbb \rangle + 1 \ 833 \ 228 \langle ababbbbbb \rangle + 917 \ 100 \langle abbbabbb \rangle - 717 \langle abbbbbb \rangle, \\
& 2 \ 033 \ 361 \langle aaaaaaaab \rangle \\
990 \langle aaaaaaaab \rangle - \frac{2 \ 033 \ 361 \langle aaaaaaaab \rangle}{2} + 1 \ 629 \ 243 \langle aaaaaaabab \rangle + \\
& 39 \ 463 \ 116 \langle aaaaaabbb \rangle - 429 \ 165 \langle aaaaaabaab \rangle + 24 \ 186 \ 162 \langle aaaaaababb \rangle - \\
& 133 \ 096 \ 128 \langle aaaaaabbab \rangle - 271 \ 774 \ 239 \langle aaaaaabbb \rangle + 15 \ 642 \langle aaaaabaaab \rangle - \\
& 55 \ 553 \ 124 \langle aaaaabaabb \rangle + 49 \ 696 \ 416 \langle aaaaababab \rangle - 559 \ 390 \ 128 \langle aaaaababb \rangle + \\
& 35 \ 365 \ 176 \langle aaaaabbaab \rangle + 322 \ 291 \ 728 \langle aaaaabbabb \rangle + 1 \ 091 \ 473 \ 944 \langle aaaaabbbab \rangle + \\
& 500 \ 213 \ 142 \langle aaaaabbbb \rangle + 8 \ 362 \ 266 \langle aaaabaaabb \rangle + 24 \ 425 \ 544 \langle aaaabaabab \rangle + \\
& 532 \ 704 \ 546 \langle aaaabaaabb \rangle - 14 \ 825 \ 580 \langle aaaababaab \rangle - 645 \ 712 \ 254 \langle aaaabababb \rangle + \\
& 310 \ 072 \ 158 \langle aaaababbab \rangle + 1 \ 589 \ 948 \ 085 \langle aaaabbb \rangle - 1 \ 013 \ 760 \langle aaaabbaab \rangle - \\
& 11 \ 791 \ 791 \langle aaaabbaabb \rangle - 1 \ 055 \ 072 \ 502 \langle aaaabbabab \rangle + 988 \ 567 \ 470 \langle aaaabbbab \rangle - \\
& 236 \ 741 \ 868 \langle aaaabbaab \rangle - 1 \ 097 \ 809 \ 680 \langle aaaabbabb \rangle - 2 \ 161 \ 650 \ 480 \langle aaaabbbab \rangle - \\
& 271 \ 774 \ 239 \langle aaaabbb \rangle - 1 \ 602 \ 480 \langle aaabaaabab \rangle - 38 \ 307 \ 720 \langle aaabaaabb \rangle + \\
& 384 \ 120 \langle aaabaabaab \rangle + 151 \ 412 \ 184 \langle aaabaababb \rangle - 667 \ 138 \ 032 \langle aaabaabbab \rangle - \\
& 940 \ 795 \ 845 \langle aaabaabbb \rangle - 173 \ 235 \ 744 \langle aaababaabb \rangle + 108 \ 772 \ 092 \langle aaabababab \rangle + \\
& 2 \ 680 \ 680 \ 420 \langle aaababbb \rangle - 23 \ 732 \ 280 \langle aaabbaab \rangle - 1 \ 082 \ 098 \ 710 \langle aaababbab \rangle - \\
& 1 \ 969 \ 678 \ 260 \langle aaababbab \rangle - 1 \ 102 \ 938 \ 606 \langle aaabbb \rangle + 24 \ 021 \ 360 \langle aaabbaabab \rangle - \\
& 157 \ 919 \ 190 \langle aaabbaabbb \rangle + 144 \ 195 \ 480 \langle aaabbabaab \rangle + 321 \ 529 \ 230 \langle aaabbabbb \rangle + \\
& 1 \ 047 \ 953 \ 610 \langle aaabbabbab \rangle - 1 \ 437 \ 458 \ 715 \langle aaabbabb \rangle + 1 \ 271 \ 160 \langle aaabbbaabb \rangle + \\
& 2 \ 047 \ 971 \ 420 \langle aaabbabbab \rangle + 68 \ 565 \ 420 \langle aaabbabb \rangle + 234 \ 463 \ 680 \langle aaabbbaab \rangle + \\
& 614 \ 361 \ 330 \langle aaabbabb \rangle + 1 \ 051 \ 036 \ 668 \langle aaabbabb \rangle + 39 \ 463 \ 116 \langle aaabbbb \rangle - \\
& 69 \ 662 \ 340 \langle aabaabaab \rangle + 54 \ 469 \ 800 \langle aabaababab \rangle - 495 \ 252 \ 120 \langle aabaabbb \rangle + \\
& 247 \ 466 \ 340 \langle aabaabbabb \rangle + 1 \ 022 \ 557 \ 800 \langle aabaabbb \rangle + 317 \ 914 \ 740 \langle aabaabbb \rangle + \\
& 295 \ 573 \ 080 \langle aababaabb \rangle + 1 \ 415 \ 868 \ 300 \langle aababababb \rangle - 542 \ 381 \ 400 \langle aabababbab \rangle - \\
& 2 \ 317 \ 991 \ 940 \langle aababbb \rangle + 38 \ 016 \ 000 \langle aababbaab \rangle + 171 \ 741 \ 240 \langle aababbbab \rangle - \\
& 1 \ 451 \ 213 \ 280 \langle aababbb \rangle + 1 \ 650 \ 500 \ 280 \langle aababbbab \rangle + 1 \ 010 \ 597 \ 940 \langle aababbbab \rangle + \\
& 182 \ 038 \ 626 \langle aababbb \rangle - 24 \ 110 \ 460 \langle aabbaabbb \rangle + 45 \ 456 \ 840 \langle aabbaabbb \rangle - \\
& 414 \ 307 \ 080 \langle aabbababab \rangle + 53 \ 420 \ 400 \langle aabbabbb \rangle - 58 \ 366 \ 440 \langle aabbabbbab \rangle + \\
& 674 \ 146 \ 440 \langle aabbabbbab \rangle + 316 \ 863 \ 162 \langle aabbabbb \rangle - 256 \ 964 \ 400 \langle aabbabbbab \rangle - \\
& 575 \ 902 \ 800 \langle aabbabbb \rangle + 185 \ 952 \ 690 \langle aabbabbb \rangle - 714 \ 930 \ 480 \langle aabbabbbab \rangle + \\
& 11 \ 799 \ 480 \langle aabbabbb \rangle - 67 \ 854 \ 600 \langle aabbabbb \rangle - 94 \ 773 \ 360 \langle aabbabbbab \rangle -
\end{aligned}$$