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Twisting by 3-cocycles

One way that fusion categories get trickier is that a lot of information is encoded in the associator. For example, we can look at *G*-graded vector spaces with a nontrivial associator.

Associator

$$\omega_{\alpha,\beta,\gamma}:V_{\alpha\beta\gamma}=(V_{\alpha}\otimes V_{\beta})\otimes V_{\gamma}\to V_{\alpha}\otimes (V_{\beta}\otimes V_{\gamma})=V_{\alpha\beta\gamma}$$

assigns a scalar to every triple (α, β, γ) .

- Compatibility = ω is a 3-cocycle
- $\operatorname{Vec}(G,\omega)$ up to equivalence only depends on $\omega \in H^3(G,k^{\times})$.



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Full slides @ gmail.