The Three-Colouring Invariant
Problem Prove that $O \neq \bigcirc$.
Proof Define an "invariant"

$$
\begin{aligned}
& I(D):=\left|\begin{array}{l}
0 \text { can be colored RGB } \\
\text { so shat ald colors are } \\
\text { usda and every crossing } \\
\text { is either mono- or tri-chromaticl }
\end{array}\right| \\
& E\{\text { True, False }\}
\end{aligned}
$$

$O \rightarrow$ False $\quad \rightarrow$ True





